

Λ_b Polarization Measurement at ATLAS

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Λ_b Production at LHC

- Due to the parity conservation in the strong interactions, at LHC Λ_b can be produced with polarization orthogonal to the production plane

... but why polarization ?

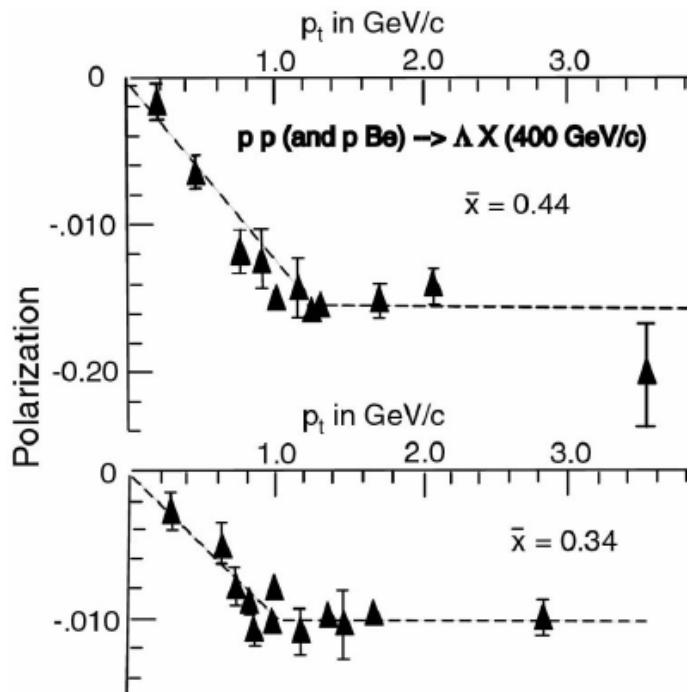
Large number of unanswered questions about the role of spin in production of hyperons at high energies which we wish to explore

Λ hyperon (uds)

- Why is the polarization so large ?
- Why is the shape so unusual ?

Λ_b hyperon (udb)

- Are the mechanisms of Λ and Λ_b polarization different ?
- Are the s and b production mechanisms similar ?
- Does the polarization depend on quark mass?



Λ_b Decay

- The considered decay, $\Lambda_b \rightarrow J/\psi(\mu\mu) \Lambda(p\pi)$, is characterized by 4 helicity amplitudes and the asymmetry parameter α_b caused by the parity non conservation of the weak interactions
- $1/2 \rightarrow 1/2 + 1$

$$a_+ = A(1/2, 0)$$

$$a_- = A(-1/2, 0)$$

$$b_+ = A(-1/2, -1)$$

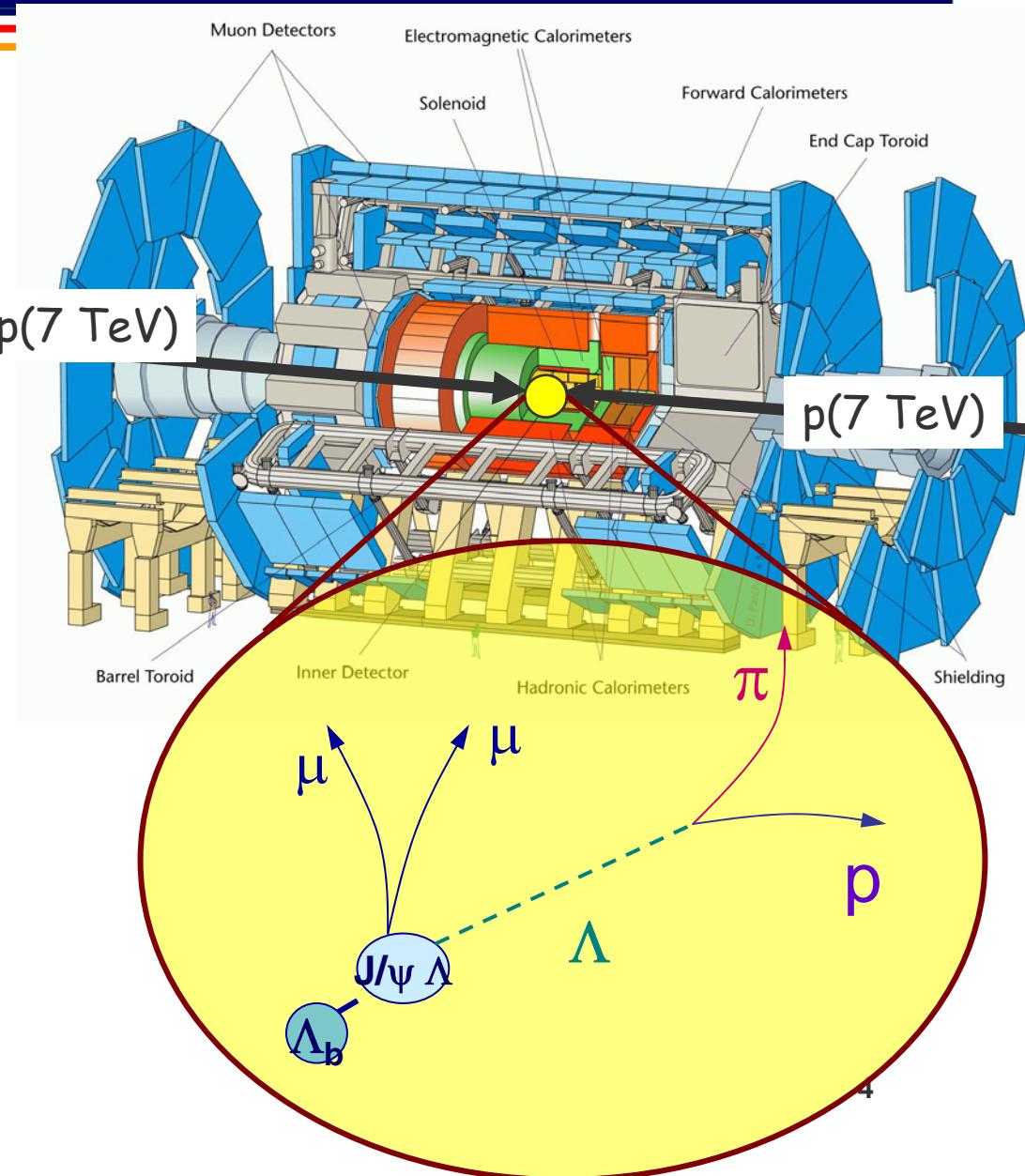
$$b_- = A(1/2, 1)$$

$$\alpha_b = \frac{|a_+|^2 - |a_-|^2 + |b_+|^2 - |b_-|^2}{|a_+|^2 + |a_-|^2 + |b_+|^2 + |b_-|^2}$$

- helicity amplitudes and asymmetry parameter α_b not yet measured
- they can, in principle, be predicted using PQCD, and thus be a tool to test theoretical models and to search for new physics
- Other interesting studies for this decay channel
 - Lifetime of Λ_b hyperon
 - CP violation in baryons

Λ_b in ATLAS

- For Low luminosity operations
 $L = 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$
- + $\int L = 10 \text{ fb}^{-1} \rightarrow O(10^{12}) \Lambda_b$ per year
- In the first 3 years $O(10^5) \Lambda_b \rightarrow J/\psi (\mu^+ \mu^-) \Lambda (\pi p)$
(ATLAS TDR estimation)
- The world's biggest sample so far is $\sim O(10^2) \Lambda_b \rightarrow J/\psi (\mu \mu) \Lambda (\pi p)$

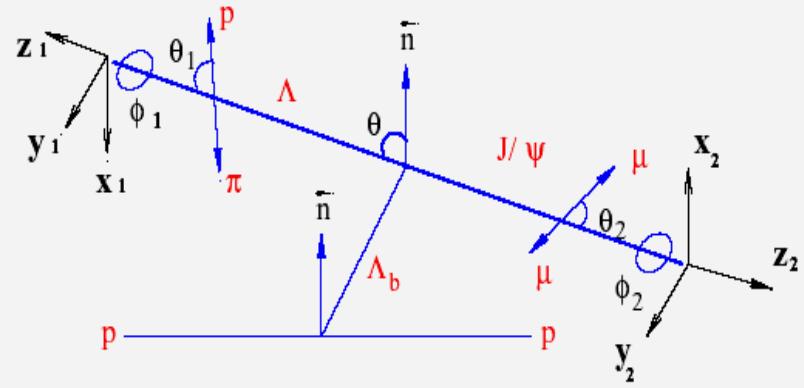


Measurement of $\Lambda_b \rightarrow J/\psi \Lambda$

The Λ_b polarization (P_b) and decay parameters can be determined from the angular distributions p.d.f. of the cascade decay

$$w(\Omega, \Omega_1, \Omega_2) = \frac{1}{(4\pi)^3} \sum_{i=0}^{i=19} f_{1i} f_{2i}(P_b, \alpha_\Lambda) F_i(\theta, \theta_1, \theta_2, \phi_1, \phi_2)$$

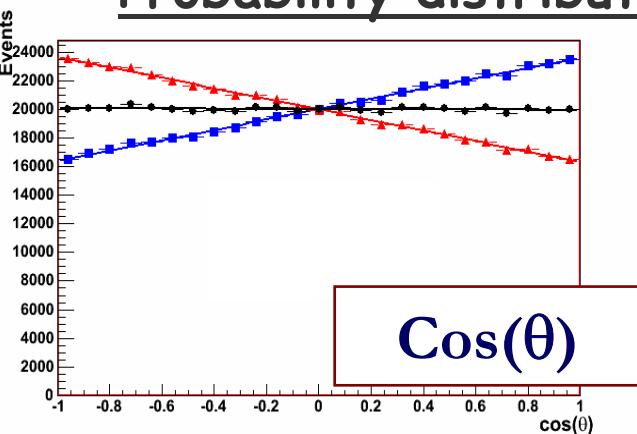
$\Lambda_b \rightarrow J/\psi(\mu\mu)\Lambda(\pi p)$ p.d.f. depends on 5 angles + 6 parameters of 4 complex helicity amplitudes and polarization P_b ($\rightarrow 7$ unknowns).



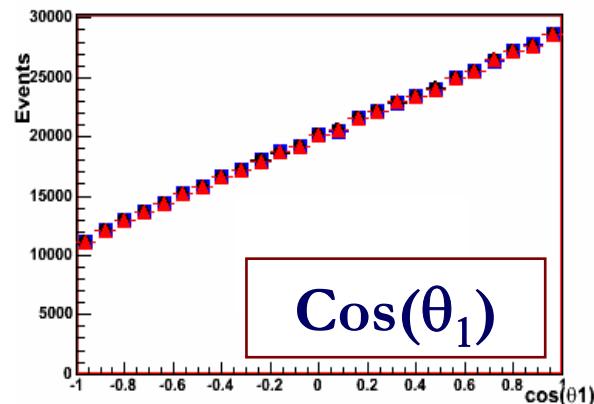
i	f_{1i}	f_{2i}	F_i
0	$a_+ a_+^* + a_- a_-^* + b_+ b_+^* + b_- b_-^*$	1	1
1	$a_+ a_+^* - a_- a_-^* + b_+ b_+^* - b_- b_-^*$	P_b	$\cos \theta$
2	$a_+ a_+^* - a_- a_-^* - b_+ b_+^* + b_- b_-^*$	α_Λ	$\cos \theta_1$
3	$a_+ a_+^* + a_- a_-^* - b_+ b_+^* - b_- b_-^*$	$P_b \alpha_\Lambda$	$\cos \theta \cos \theta_1$
4	$-a_+ a_+^* - a_- a_-^* + \frac{1}{2} b_+ b_+^* + \frac{1}{2} b_- b_-^*$	1	$d_{00}^2(\theta_2)$
5	$-a_+ a_+^* + a_- a_-^* + \frac{1}{2} b_+ b_+^* - \frac{1}{2} b_- b_-^*$	P_b	$d_{00}^2(\theta_2) \cos \theta$
6	$-a_+ a_+^* + a_- a_-^* - \frac{1}{2} b_+ b_+^* + \frac{1}{2} b_- b_-^*$	α_Λ	$d_{00}^2(\theta_2) \cos \theta_1$
7	$-a_+ a_+^* - a_- a_-^* - \frac{1}{2} b_+ b_+^* - \frac{1}{2} b_- b_-^*$	$P_b \alpha_\Lambda$	$d_{00}^2(\theta_2) \cos \theta \cos \theta_1$
8	$-3\text{Re}(a_+ a_-^*)$	$P_b \alpha_\Lambda$	$\sin \theta \sin \theta_1 \sin^2 \theta_2 \cos \phi_1$
9	$3\text{Im}(a_+ a_-^*)$	$P_b \alpha_\Lambda$	$\sin \theta \sin \theta_1 \sin^2 \theta_2 \sin \phi_1$
10	$-\frac{3}{2}\text{Re}(b_- b_+^*)$	$P_b \alpha_\Lambda$	$\sin \theta \sin \theta_1 \sin^2 \theta_2 \cos(\phi_1 + 2\phi_2)$
11	$\frac{3}{2}\text{Im}(b_- b_+^*)$	$P_b \alpha_\Lambda$	$\sin \theta \sin \theta_1 \sin^2 \theta_2 \sin(\phi_1 + 2\phi_2)$
12	$-\frac{3}{\sqrt{2}}\text{Re}(b_- a_+^* + a_- b_+^*)$	$P_b \alpha_\Lambda$	$\sin \theta \cos \theta_1 \sin \theta_2 \cos \theta_2 \cos \phi_2$
13	$\frac{3}{\sqrt{2}}\text{Im}(b_- a_+^* + a_- b_+^*)$	$P_b \alpha_\Lambda$	$\sin \theta \cos \theta_1 \sin \theta_2 \cos \theta_2 \sin \phi_2$
14	$-\frac{3}{\sqrt{2}}\text{Re}(b_- a_-^* + a_+ b_+^*)$	$P_b \alpha_\Lambda$	$\cos \theta \sin \theta_1 \sin \theta_2 \cos \theta_2 \cos(\phi_1 + \phi_2)$
15	$\frac{3}{\sqrt{2}}\text{Im}(b_- a_-^* + a_+ b_+^*)$	$P_b \alpha_\Lambda$	$\cos \theta \sin \theta_1 \sin \theta_2 \cos \theta_2 \sin(\phi_1 + \phi_2)$
16	$\frac{3}{\sqrt{2}}\text{Re}(a_- b_+^* - b_- a_+^*)$	P_b	$\sin \theta \sin \theta_2 \cos \theta_2 \cos \phi_2$
17	$-\frac{3}{\sqrt{2}}\text{Im}(a_- b_+^* - b_- a_+^*)$	P_b	$\sin \theta \sin \theta_2 \cos \theta_2 \sin \phi_2$
18	$\frac{3}{\sqrt{2}}\text{Re}(b_- a_-^* - a_+ b_+^*)$	α_Λ	$\sin \theta_1 \sin \theta_2 \cos \theta_2 \cos(\phi_1 + \phi_2)$
19	$-\frac{3}{\sqrt{2}}\text{Im}(b_- a_-^* - a_+ b_+^*)$	α_Λ	$\sin \theta_1 \sin \theta_2 \cos \theta_2 \sin(\phi_1 + \phi_2)$

What angular distributions do we expect?

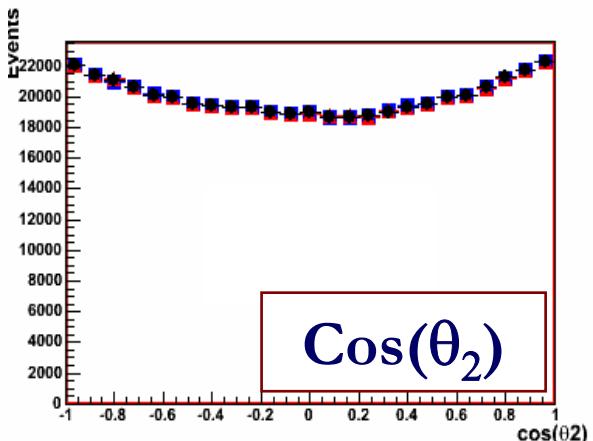
Probability distributions:



$\text{Cos}(\theta)$

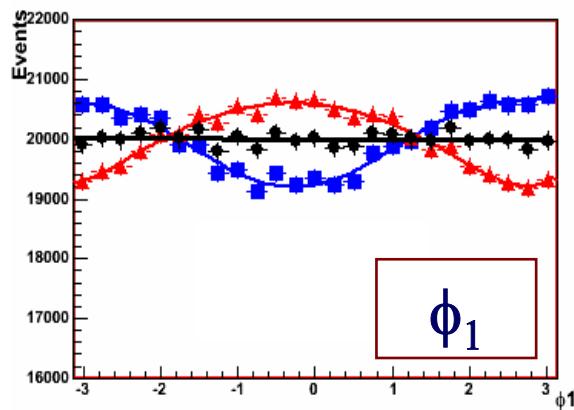


$\text{Cos}(\theta_1)$

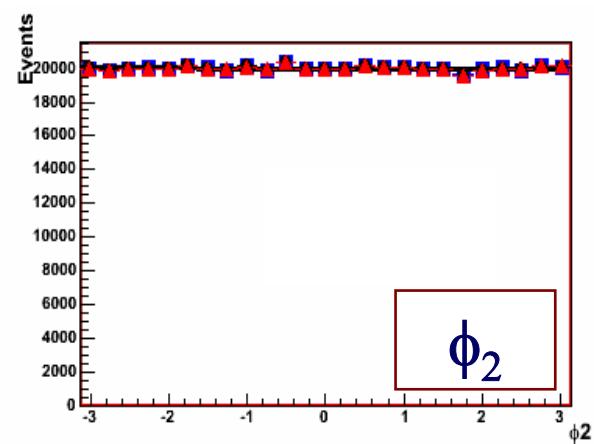


$\text{Cos}(\theta_2)$

$P = 0\%$
 $P = -40\%$
 $P = 40\%$



ϕ_1



ϕ_2

A Model for Λ_b Decay

- The general amplitude for the decay $\Lambda_b \rightarrow \Lambda J/\psi$ is given by:

$$M = \bar{\Lambda}(p_\Lambda) \varepsilon_\mu^*(p_{J/\psi}) \left[A_1 \gamma^\mu \gamma_5 + A_2 \frac{p_{\Lambda_b}^\mu}{m_{\Lambda_b}} \gamma_5 + B_1 \gamma^\mu + B_2 \frac{p_{\Lambda_b}^\mu}{m_{\Lambda_b}} \right] \Lambda_b(p_{\Lambda_b}),$$

- ε_μ^* - polarization vector of the vector meson (J/ψ)
- A_1, A_2, B_1, B_2 - complex decay amplitudes are calculable within the framework of PQCD models using factorization theorems (*Phys. Rev. D65:074030, 2002, hep-ph/0112145*)
- Helicity amplitudes related to A_1, A_2, B_1, B_2 :

$$a_+ = -0.0176 - 0.4290i$$

$$a_- = 0.0867 + 0.2454i$$

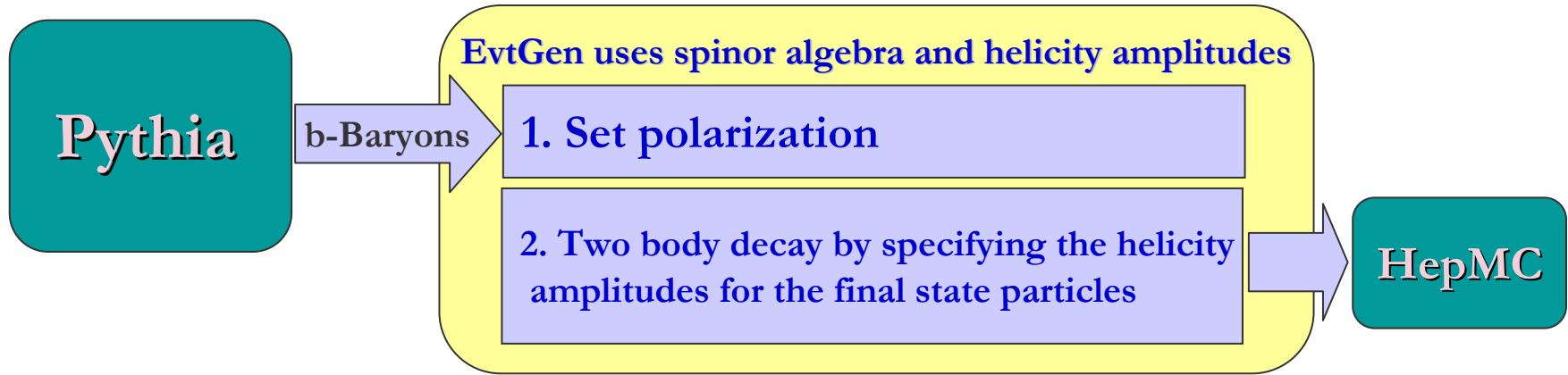
$$b_+ = -0.0810 - 0.2837i$$

$$b_- = 0.0296 + 0.8124i$$

$$\alpha_b = -0.457$$

Generation of Polarized Λ_b

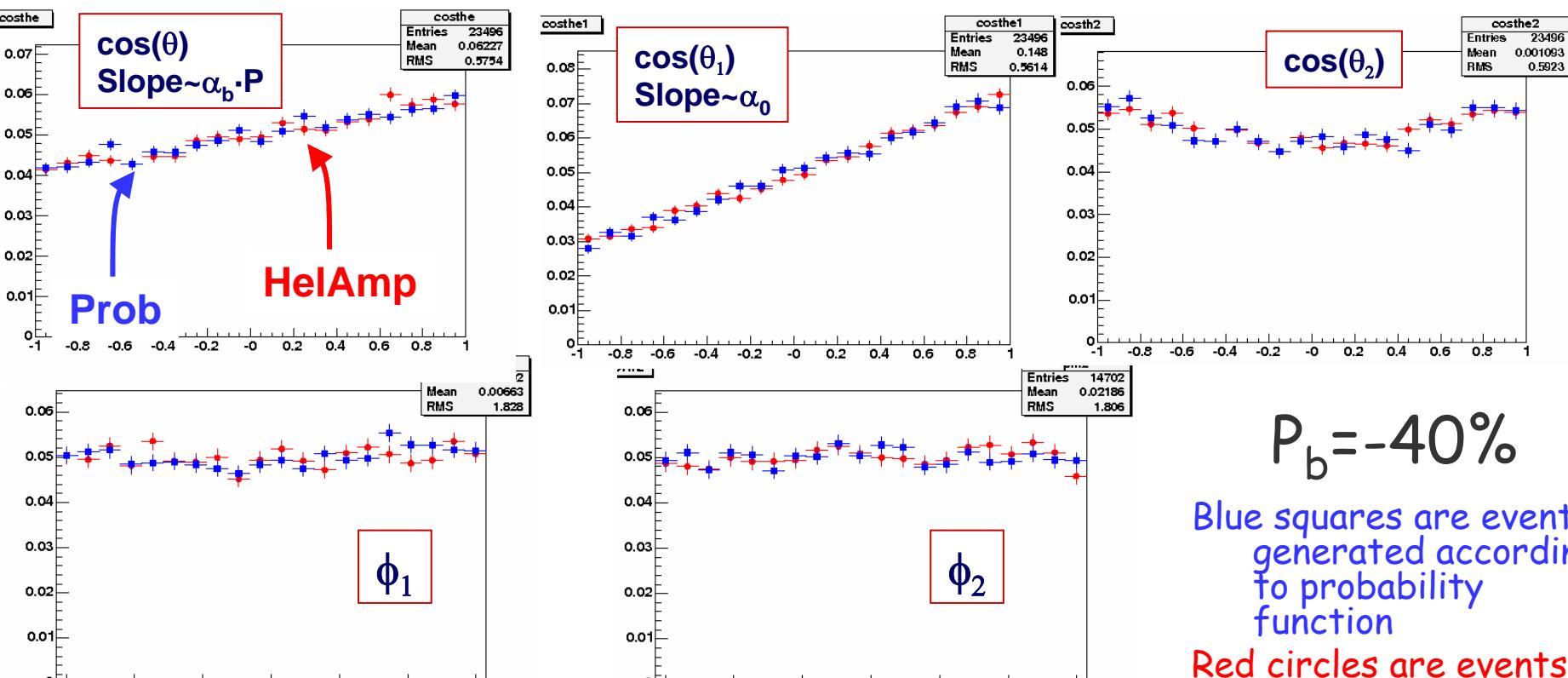
- In order to study the feasibility of measuring Λ_b polarization in ATLAS we have developed a way to make polarized Λ_b in EvtGen
- EvtGen: originally written in BaBar and CLEO, now also in MC/LCG project
 - ◆ package providing a framework for implementation of processes relevant to B physics
 - ◆ uses spinor algebra and helicity amplitudes
 - ▶ it's possible to set the polarization of the particle before the particle is decayed
 - ▶ .. and obtain the correct angular distributions



◆ First ever adaptation of EvtGen as a generator of polarized Λ_b baryons

EvtGen Cross Check

- 5 angular distributions are generated using both the probability function and using the full amplitude feature in EvtGen



$$P_b = -40\%$$

Blue squares are events generated according to probability function

Red circles are events generated with helicity amplitudes in EvtGen

Very good agreement between the angular distributions generated with EvtGen and the probability density function!

Data Simulation, Reconstruction and Analysis

Events generated with Pythia/EvtGen

- ◆ several input models
- ◆ Production cuts:
 - ◆ $p_T(\mu_1) > 2.5\text{GeV}$, $p_T(\mu_2) > 4.0\text{GeV}$,
 - ◆ $p_T(\pi/p) > 0.5 \text{ GeV}$, $|\eta| < 2.7$

Full simulation in ATLAS detector with Geant4

Recostruction

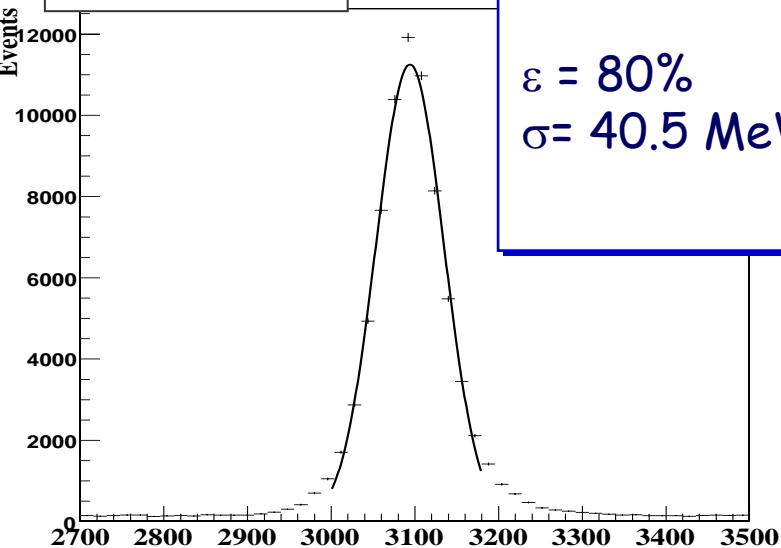
- ◆ Dedicated algorithm for low p_T muons developed
 - ◆ Better efficiency for J/ψ identification
- ◆ Inner Detector tracking and vertexing algorithms for Λ and Λ_b identification
- ◆ Angular distributions determination

Analysis

- ◆ MC toy for "fast" predictions
- ◆ Maximum Likelihood method to measure P_b and Λ_b decay parameters

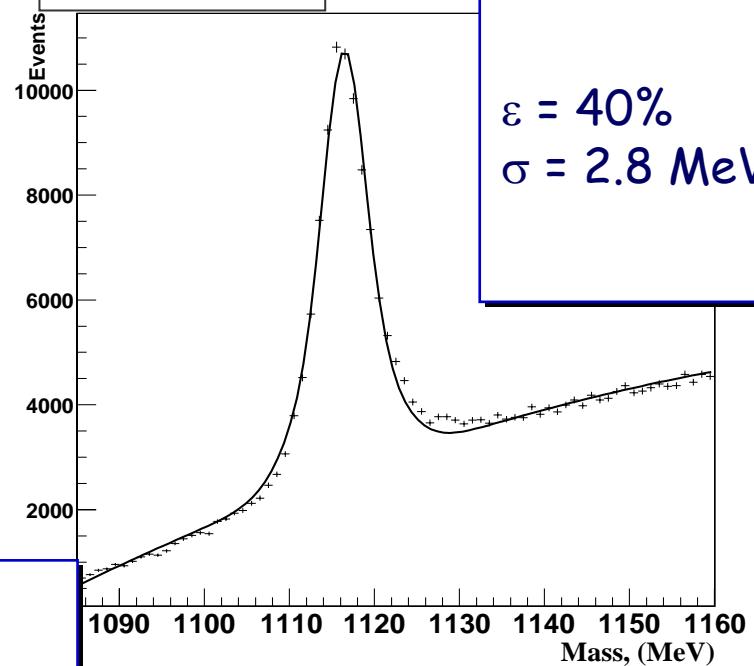
Event Reconstruction

J/ ψ mass



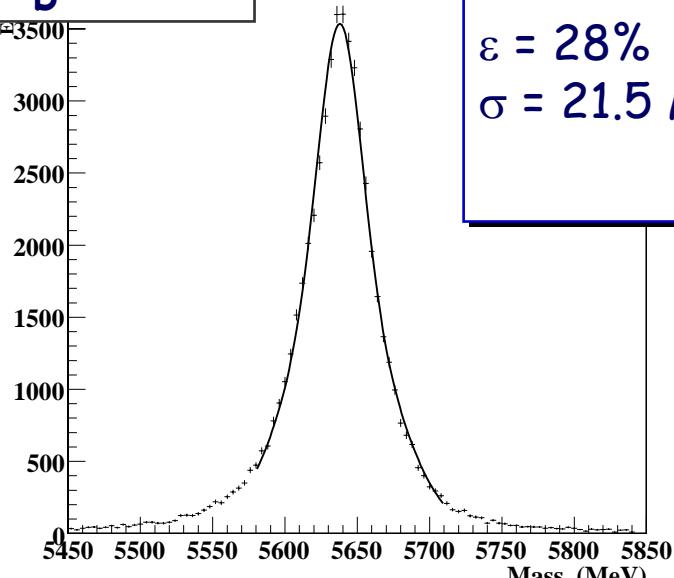
$$\varepsilon = 80\% \\ \sigma = 40.5 \text{ MeV}$$

Λ mass



$$\varepsilon = 40\% \\ \sigma = 2.8 \text{ MeV}$$

Λ_b mass

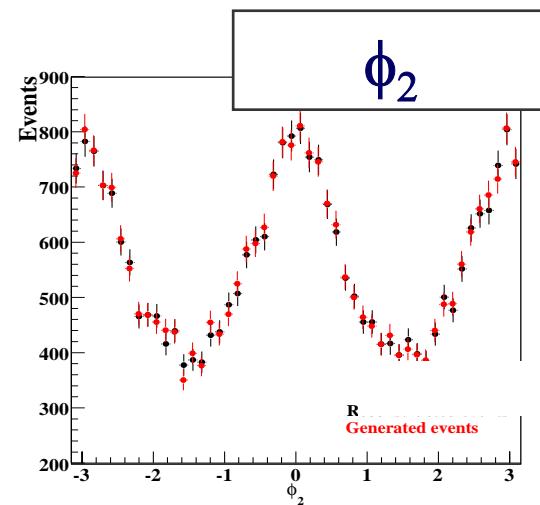
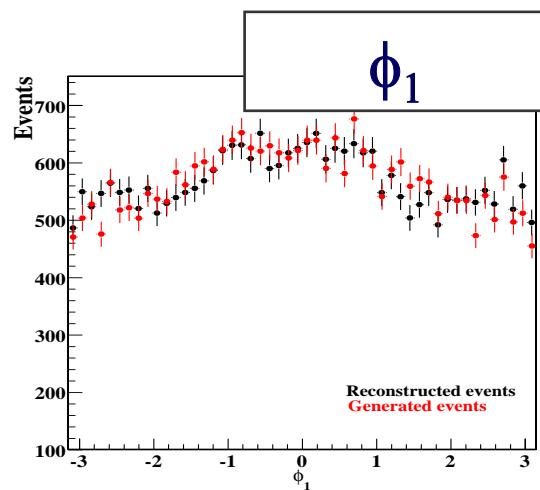
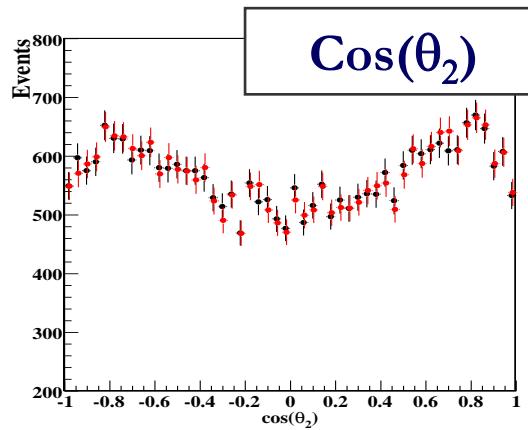
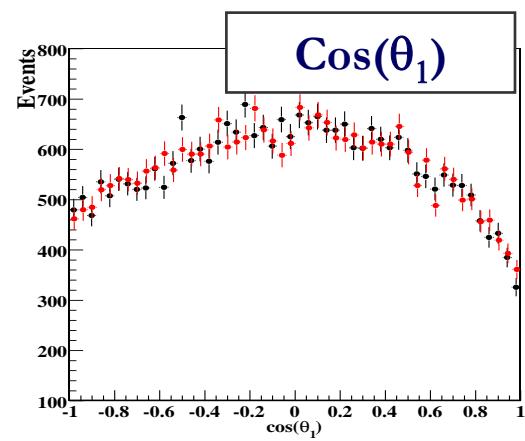
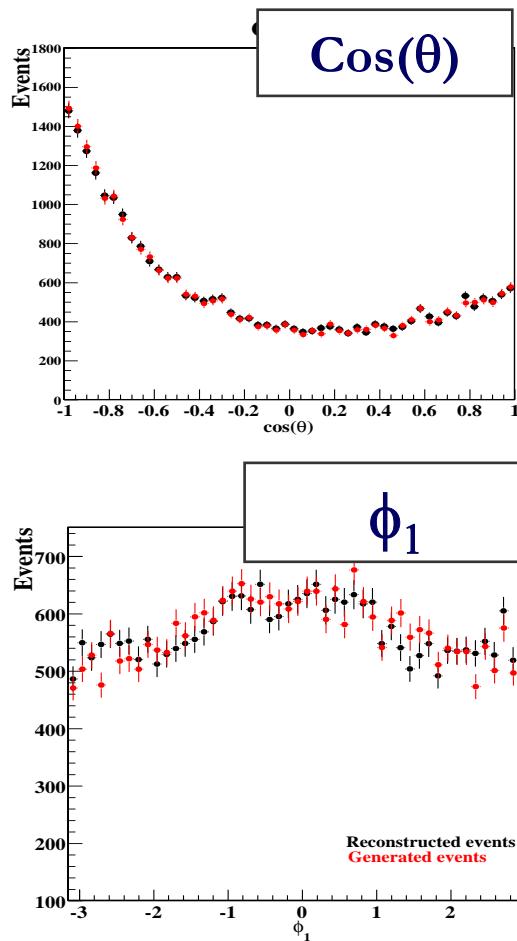


$$\varepsilon = 28\% \\ \sigma = 21.5 \text{ MeV}$$

$\varepsilon = \text{rec efficiency}$
 σ from Gaussian fits

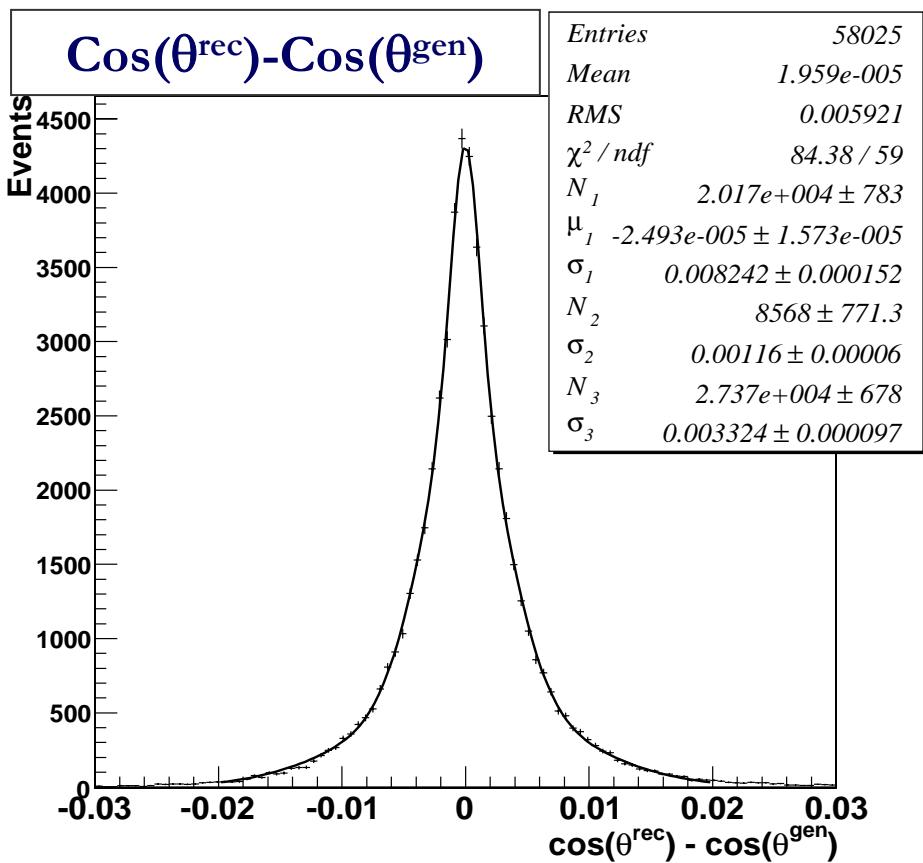
Angular distributions in ATLAS detector

ATLAS acceptance modifies the angular distributions and increases the difficulty of the measurement



P=-100%
Reconstructed angle
vs
Generated angle

Angular Resolutions



Angles	Gaussian fit σ (mrad)
$\cos\theta$	2
$\cos\theta_1$	21
ϕ_1	32
$\cos\theta_2$	3
ϕ_2	13

Maximum Likelihood Results

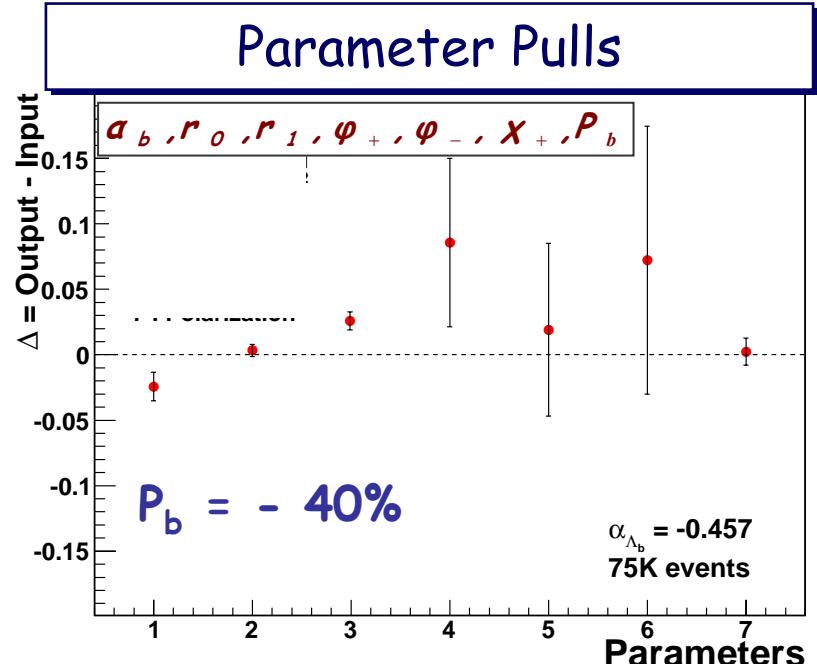
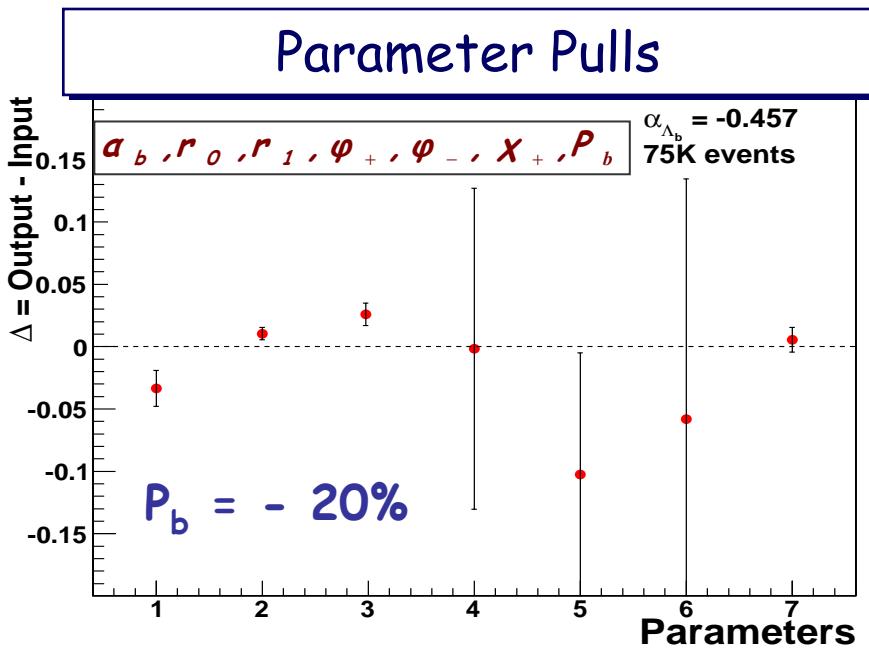
- In the problem we have 9 parameters: P and four complex amplitudes

$$a_+ = |a_+|e^{ia_+}, a_- = |a_-|e^{ia_-}, b_+ = |b_+|e^{ib_+}, b_- = |b_-|e^{ib_-}$$

- The normalization + global phase constraint \rightarrow 7 independent parameters

$$a_b; r_0 = |a_+|^2 + |a_-|^2; r_1 = |a_+|^2 - |a_-|^2; \varphi_+ = a_+ - \beta_+; \varphi_- = a_- - \beta_-; X_+ = \beta_+ - \beta_-; P_b$$

- The ML results (Toy MC sample + angular resolution from reconstruction + detector acceptance)
 - only statistical uncertainties are shown

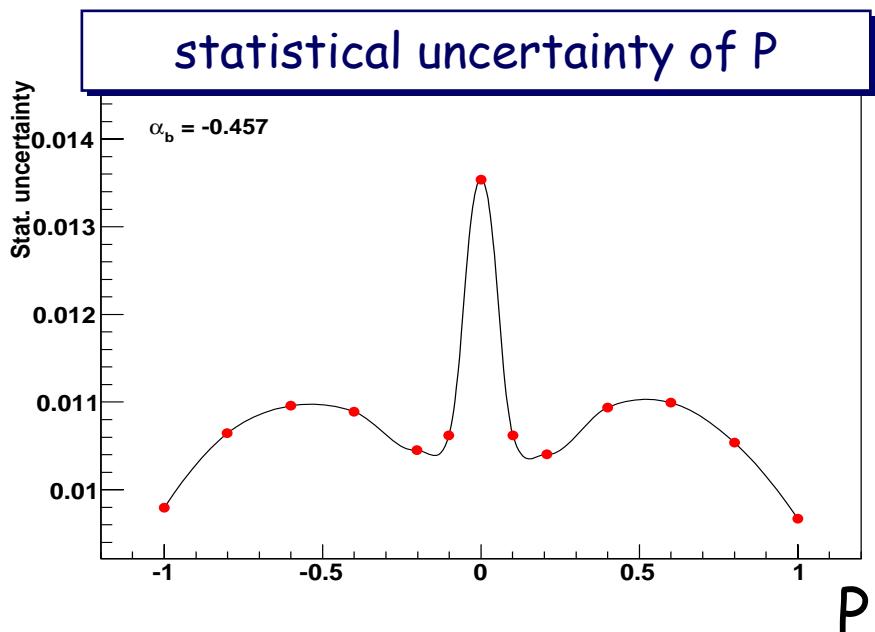
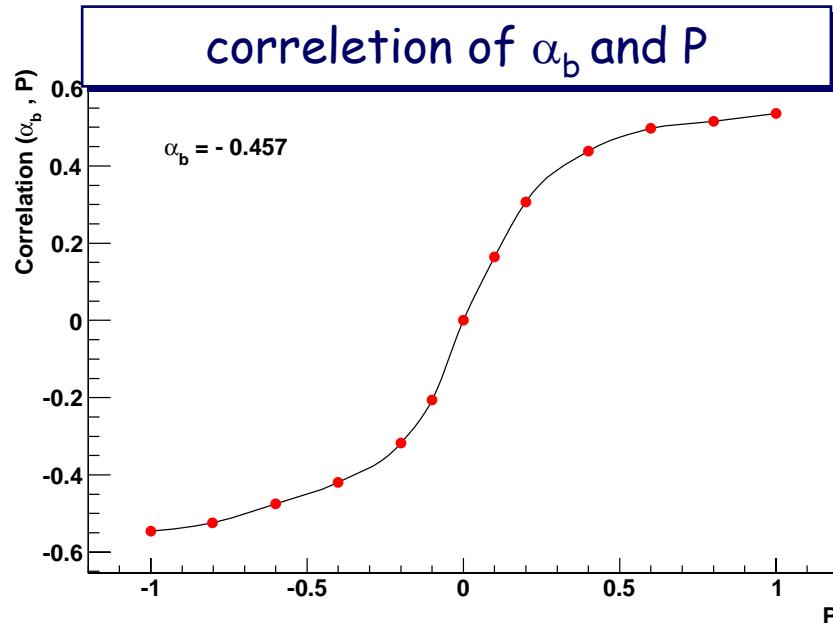
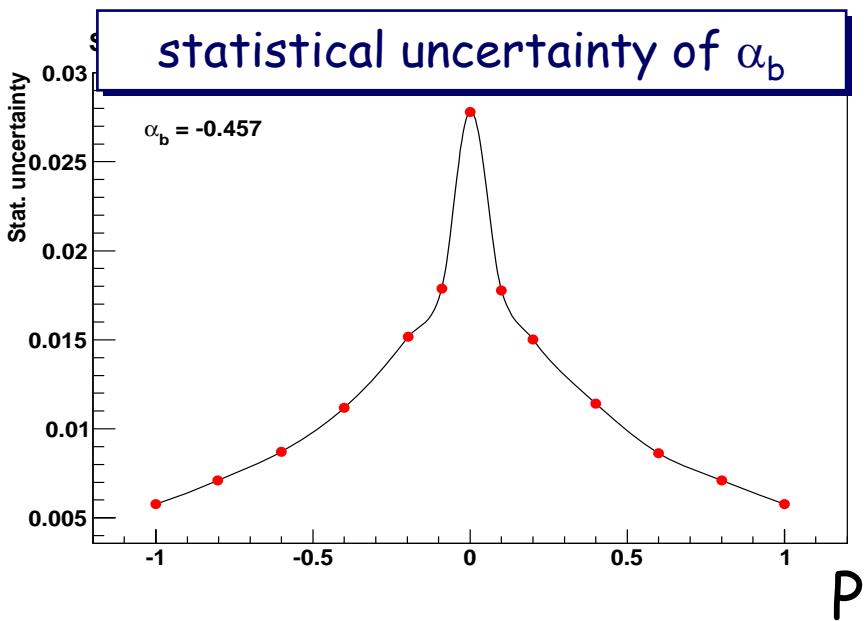


Decoupling P and α_b

- ◆ $\alpha_b P \cos(\theta)$ - dominant term
- ◆ The 5 angle method allows to decouple P and α_b .

Estimating the statistical uncertainties

- 1) α_b can be measured with good precision even if $P \sim 0$.
- 2) Small uncertainty (P), even for $P \sim 0$.



Summary and Outlook

- We have done an extensive study of the feasibility of measuring Λ_b parameters in ATLAS:
 - ◆ Generator model in EvtGen for producing polarized Λ_b in ATLAS
 - ◆ Λ_b reconstruction from their decay into Λ 's and J/ψ
 - ◆ Polarization and amplitudes extraction from the decay angles
 - ◆ Effects of angular resolution on the determination of the parameters
 - ◆ Correlations between α_b and polarization
- Future plans
 - ◆ make background studies
 - ◆ continue to develop likelihood fitting procedures
 - ◆ incorporate trigger in analysis
 - ◆ make Lifetime feasibility studies
 - ◆ develop plans for CP studies



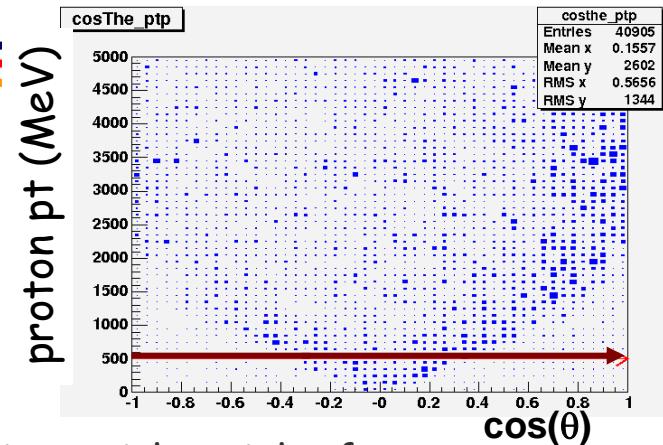
Back-up Slides

Acceptance Effects

Cuts @ Generator Level:

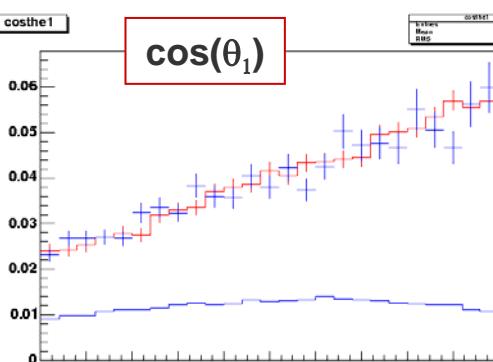
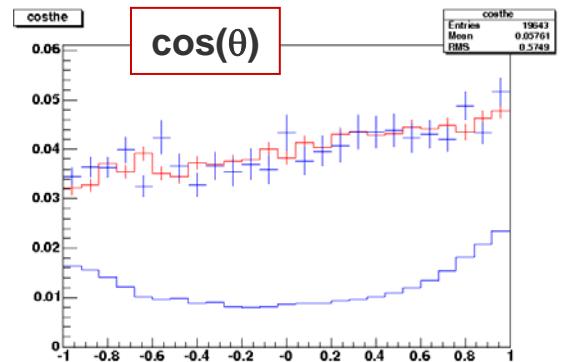
$p_T(p, \pi) > 0.5$ GeV
 $p_T(\mu) > 2.5, 4$ GeV
 $|\eta| < 2.7$

ATLAS acceptance modifies the angular distributions

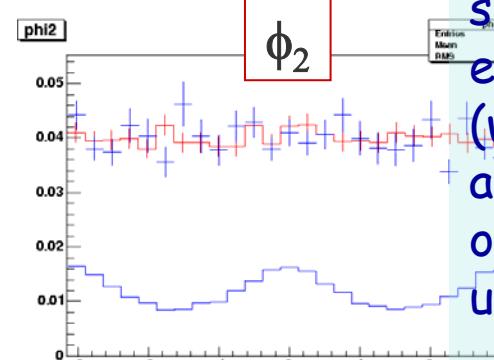
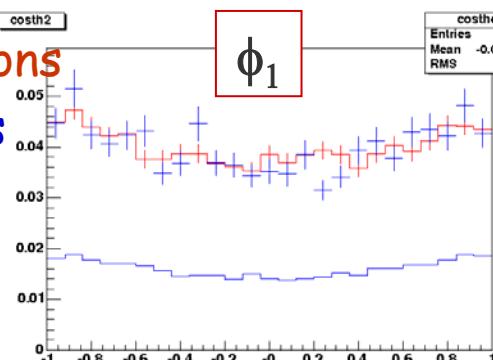


cut

It's possible to correct distorted angular distributions with weight factors



generated distributions
generated after cuts
+ after corrections



To calculate the corrections, phase space events (without any model or cuts) are used⁸

Maximum Likelihood (ML) Method

ML Method :

$$w(\Omega, \Omega_1, \Omega_2) = \frac{1}{(4\pi)^3} \sum_{i=0}^{i=19} f_{1i} f_{2i}(P_b, \alpha_\Lambda) F_i(\theta, \theta_1, \theta_2, \phi_1, \phi_2)$$

$$w_{obs}(\vec{\theta}', \vec{A}, \vec{\alpha}) = \frac{\int w(\vec{\theta}, \vec{A}, \vec{\alpha}) T(\vec{\theta}, \vec{\theta}') d\vec{\theta}}{\iint w(\vec{\theta}, \vec{A}, \vec{\alpha}) T(\vec{\theta}, \vec{\theta}') d\vec{\theta} d\vec{\theta}'}$$

θ' : Measured angles
 θ : Generated angles

where:

$$\vec{\theta} = \begin{pmatrix} \theta \\ \theta_1 \\ \phi_1 \\ \theta_2 \\ \phi_2 \end{pmatrix}, \vec{A} = \begin{pmatrix} a^+ \\ a^- \\ b^+ \\ b^- \end{pmatrix}, \vec{\alpha} = \begin{pmatrix} \alpha_\Lambda \\ P \end{pmatrix}$$

$$T(\vec{\theta}, \vec{\theta}') = \varepsilon(\vec{\theta}, \vec{\theta}') R(\vec{\theta}, \vec{\theta}')$$

$R(\theta, \theta')$ is the resolution
 $\varepsilon(\theta, \theta')$ is the acceptance correction

Acceptance correction normalization : $\int F_i(\vec{\theta}) \varepsilon(\vec{\theta}) d\vec{\theta}$
 $i=0 \dots 19$

Backgrounds

- Dominated by J/ψ from b-hadrons + Λ from heavier hadrons and fragmentation
- fake μ and combinatorial background found negligible in similar topologies ($B^0 \rightarrow J/\psi K_s$)
- real J/ψ from cascade decay estimated at percent level (ex. $\Xi_b^{-,0} \rightarrow \Xi^{-,0} J/\psi \rightarrow \Lambda \pi^{-,0} J/\psi$)
- $B^0 \rightarrow J/\psi K_s$ where a proton mass is given to a p rejected with mass constraints
- for non direct Λ_b from Σ_b ; try to reconstruct Σ_b to reduce the dilution of polarization