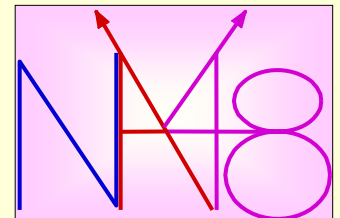


# Results on direct CP Violation in $K^{\pm} \rightarrow 3\pi$ decays from the NA48/2 experiment at CERN

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On behalf of the NA48/2 collaboration:  
*Cambridge, CERN, Chicago, Dubna, Edinburgh, Ferrara,  
Firenze, Mainz, Northwestern, Perugia, Pisa, Saclay,  
Siegen, Torino, Vienna*

New Trends in High Energy Physics  
Yalta, 10-17 September 2005



# Outline

- Direct CP violation in  $K^\pm \rightarrow 3\pi$  decays
- NA48/2 experimental setup
- Measurement principle
- Systematic effects
- Preliminary result in  $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$  decay
- Outlook for  $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$  analysis
- Neutral mode "Cusp effect"
- Conclusions

# Brief history of CP violation

**1964** - CP violation in  $K^0$  (Cronin, Christenson, Fitch, Turlay)

**1993-99** - **Direct** CP violation in  $K^0$  (NA31, NA48, KTeV)

**2001** - CP violation in  $B^0$  mixing (Babar, Belle)

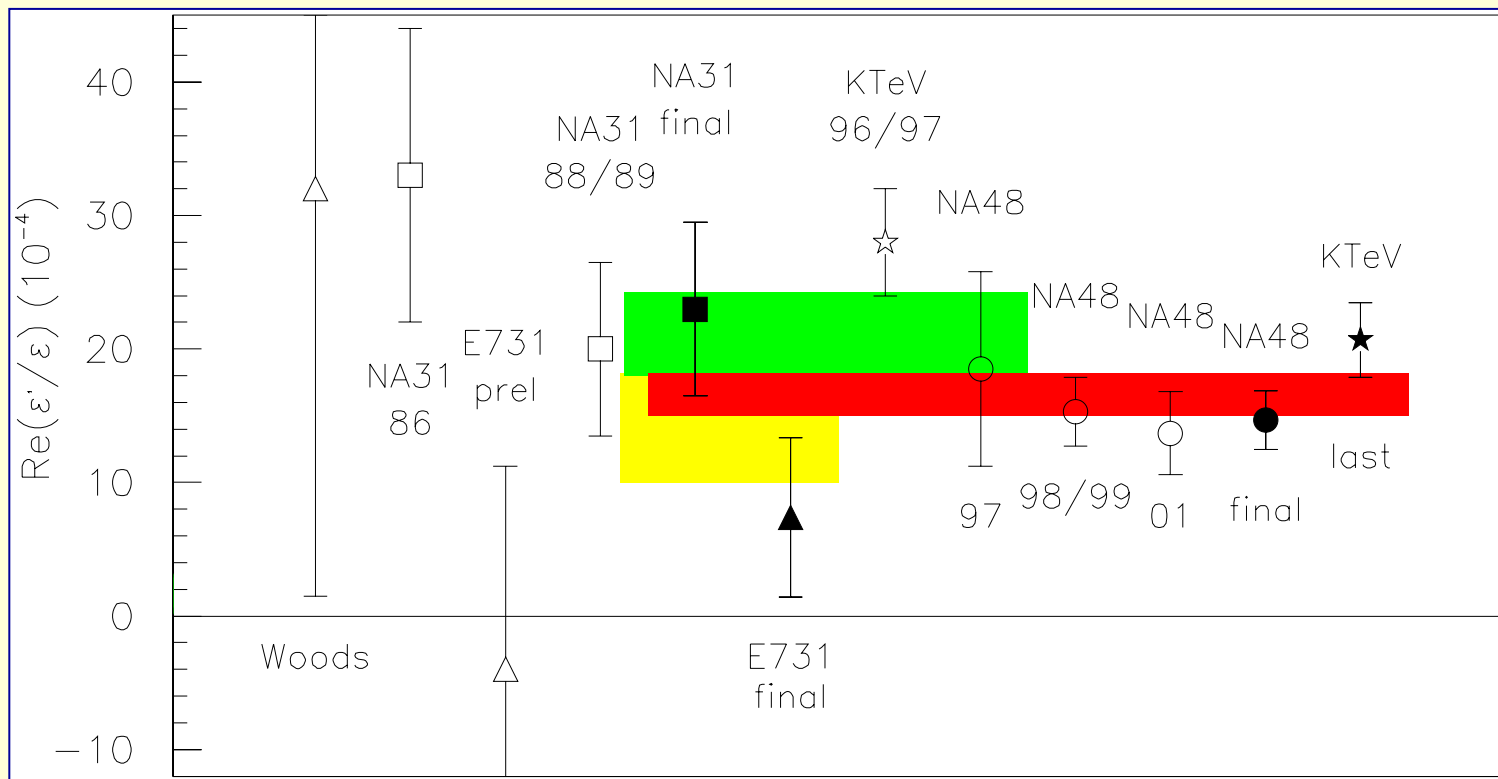
**2004** - **Direct** CP violation in  $B^0$  (Belle, Babar)

Direct CP Violation, also known as CPV in decay amplitudes, is the most “straightforward” CP effect

- Hard to detect experimentally
- Hard to connect to the parameters of the underlying fundamental theory (i.e. SM)

**But it is a crucial window to physics beyond SM**  
because possible non-SM enhancements to heavy quark loops  
are just at the core of DCPV processes

# Direct CPV in $K^0 \rightarrow \pi\pi$ decays

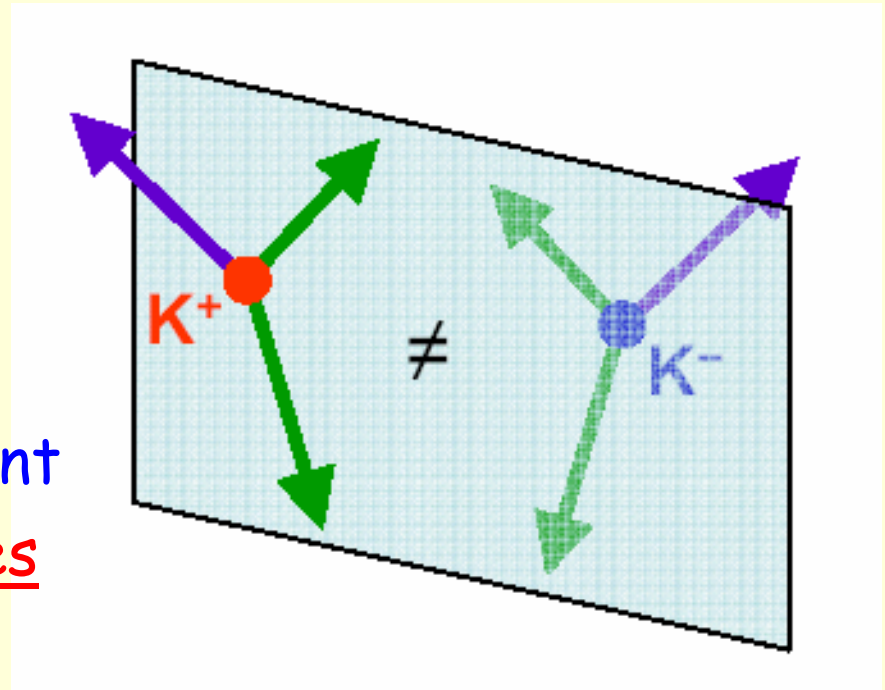


Final NA48 result  
 $\varepsilon'/\varepsilon = (14.7 \pm 2.2) \times 10^{-4}$

# CP violation in $K_{3\pi}^{\pm}$ decays

- Potentially large statistics
- Simple selection
- Low background

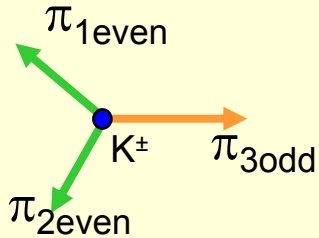
No absolute K flux measurement  
Compare only Dalitz plot shapes



Complementary observables in Kaons:  $\varepsilon'/\varepsilon \leftrightarrow A_g \leftrightarrow$  rare decays  
Look for **direct** CP violation in  $K^{\pm}$   
(only direct CPV in  $K^{\pm}$  possible - **no mixing**)

# Direct CP violation observable $A_g$

$$|M(u,v)|^2 \sim 1 + gu + hu^2 + kv^2$$



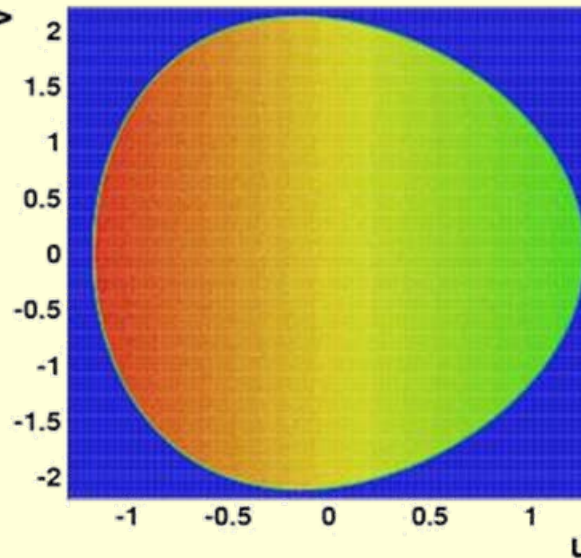
$$U = \frac{s_3 - s_0}{m_\pi^2}$$

$$V = \frac{s_2 - s_1}{m_\pi^2}$$

$$s_i = (P_K - p_{\pi i})^2$$

$$s_0 = \frac{1}{3} \sum s_i$$

$i=3$  odd pion



$$\underline{K^\pm \rightarrow \pi^\pm \pi^+ \pi^-}$$

$$\text{BR} = 5.57\% ; g = -0.2154 \pm 0.035$$

$$\underline{K^\pm \rightarrow \pi^\pm \pi^0 \pi^0}$$

$$\text{BR} = 1.73\% ; g = 0.652 \pm 0.031$$

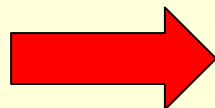
$$|h|, |k| \ll |g|$$

$$A_g = \frac{g_+ - g_-}{g_+ + g_-} = \frac{\Delta g}{2g} = -0.43$$

$A_g < 5 \times 10^{-5}$  compatible with SM

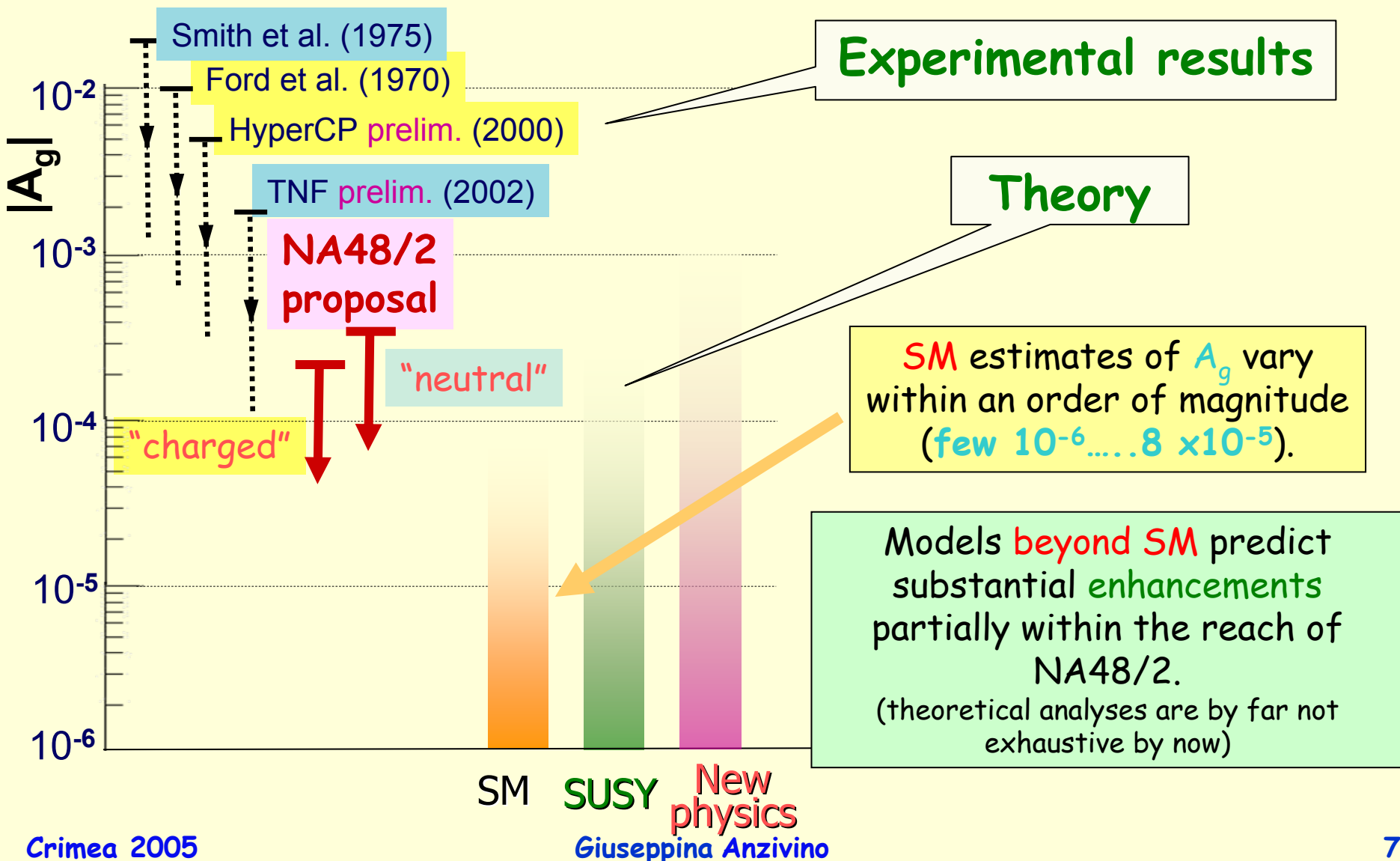
$A_g > 1 \times 10^{-4}$  SUSY/new physics

$$A_g \neq 0$$



Direct CP violation

# Experimental and theoretical status



# Goals and method

## ➤ Primary NA48/2 goals:

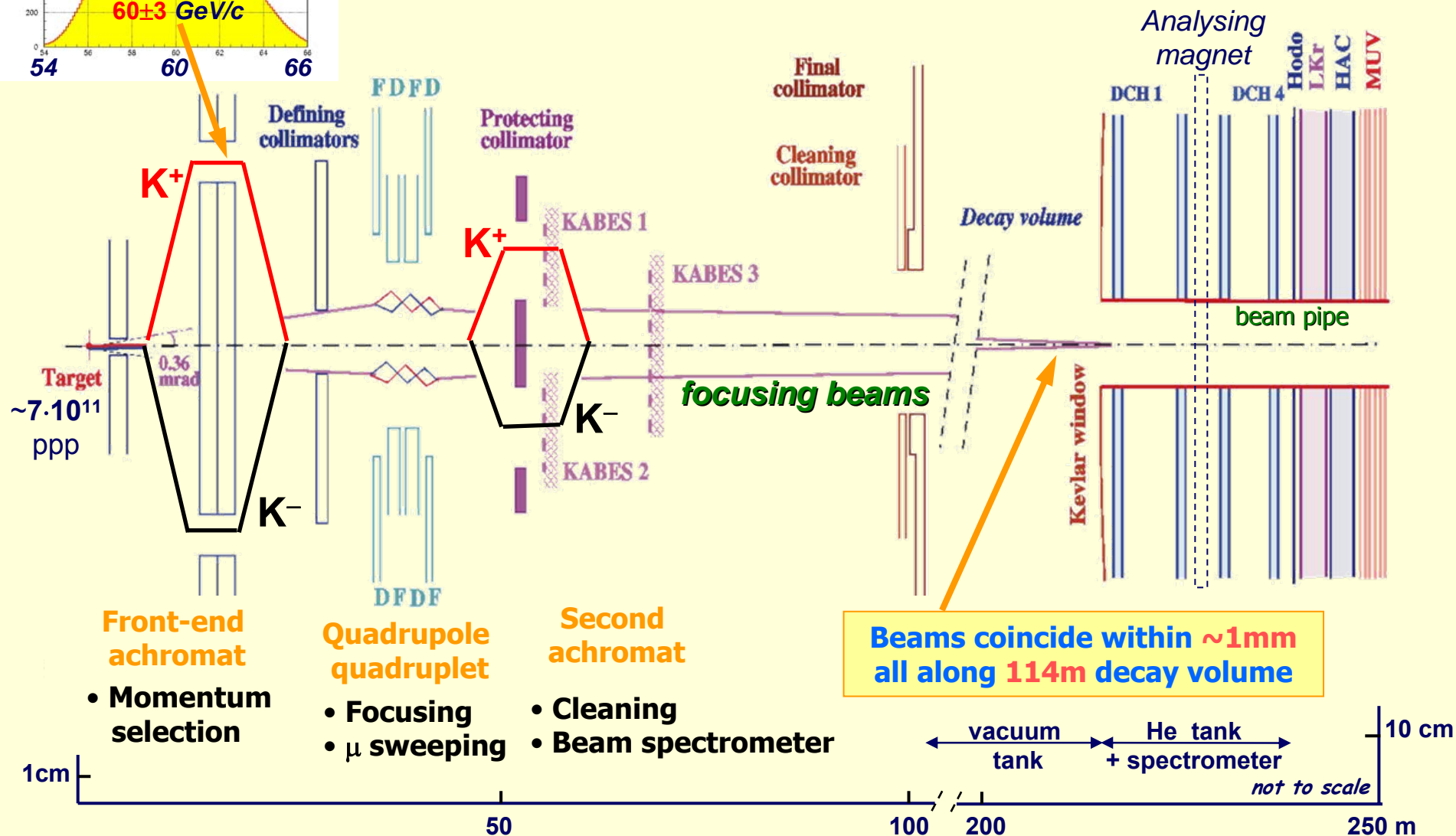
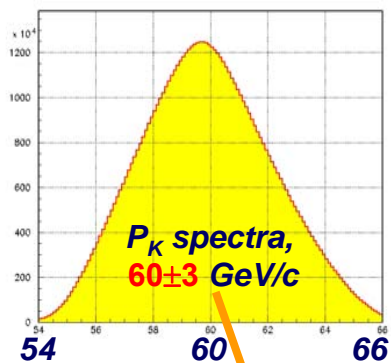
- Measure slope asymmetries in "charged" and "neutral" modes with precisions  $\delta A_g < 2.2 \times 10^{-4}$ , and  $\delta A_g^0 < 3.5 \times 10^{-4}$ , respectively.
- Statistics required for this measurement:  $> 2 \times 10^9$  in "charged" mode and  $> 10^8$  in "neutral" mode.

## ➤ NA48/2 method:

- Two simultaneous  $K^+$  and  $K^-$  beams, superimposed in space, with narrow momentum spectra;
- Detect asymmetry exclusively considering slopes of ratios of normalized u distributions;
- Equalise averaged  $K^+$  and  $K^-$  acceptances by frequently alternating the polarities of the relevant magnets.



# Experimental setup



# The NA48 detector

## Main detector components:

### ❖ Magnetic spectrometer (4 DCHs):

4 views: redundancy  $\Rightarrow$  efficiency

$$\sigma(p)/p = 1.0\% + 0.044\% p \text{ [GeV/c]}$$

### ❖ Hodoscope: fast trigger and precise time measurement (150ps)

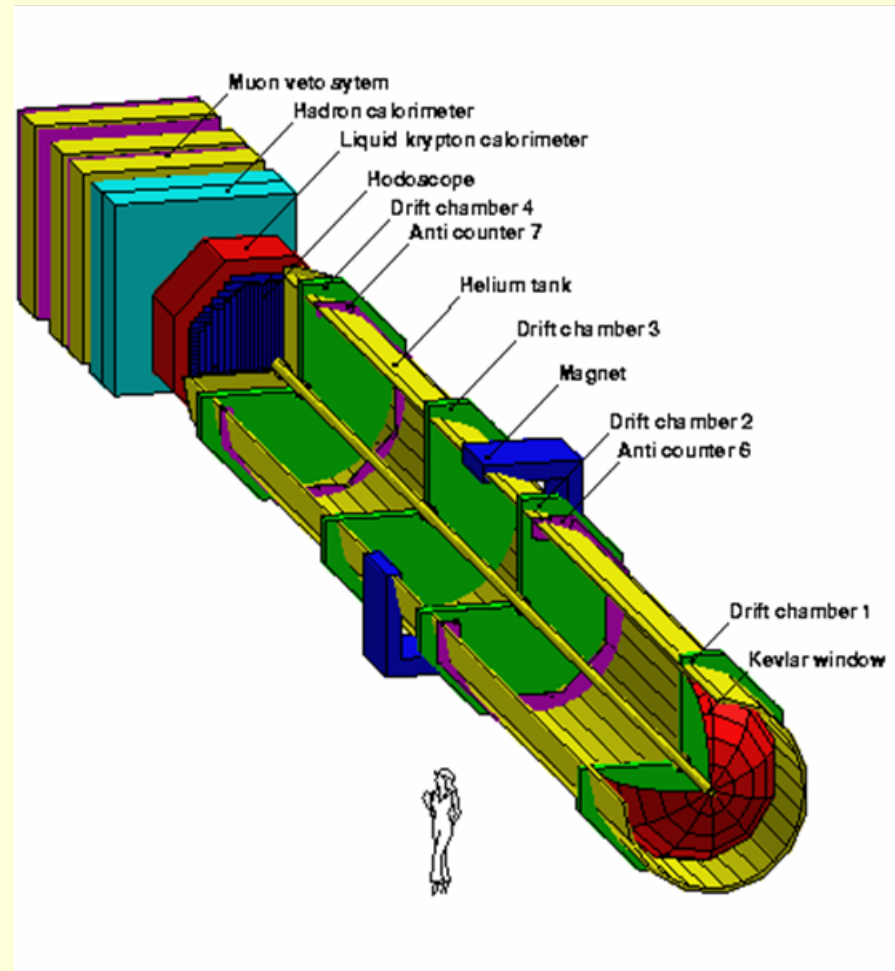
### ❖ Liquid Krypton e.m. calorimeter:

High granularity, quasi-homogeneous

$$\sigma(E)/E = 3.2\%/ \sqrt{E} + 9\%/E + 0.42\% \text{ [GeV]}$$

$e/\pi$  discrimination

### ❖ Hadron calorimeter, photon vetos, muon veto counters





Crimea 2005



Giuseppina Anzivino



# Data taking: completed

**2003** run: ~ 50 days

**2004** run: ~ 60 days

Total statistics in 2 years:

- $K^\pm \rightarrow \pi^+ \pi^- \pi^\pm$ :  $\sim 3.5 \cdot 10^9$

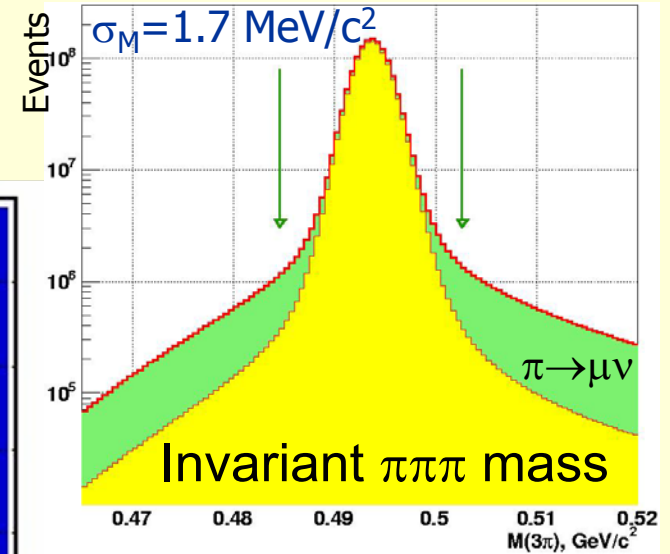
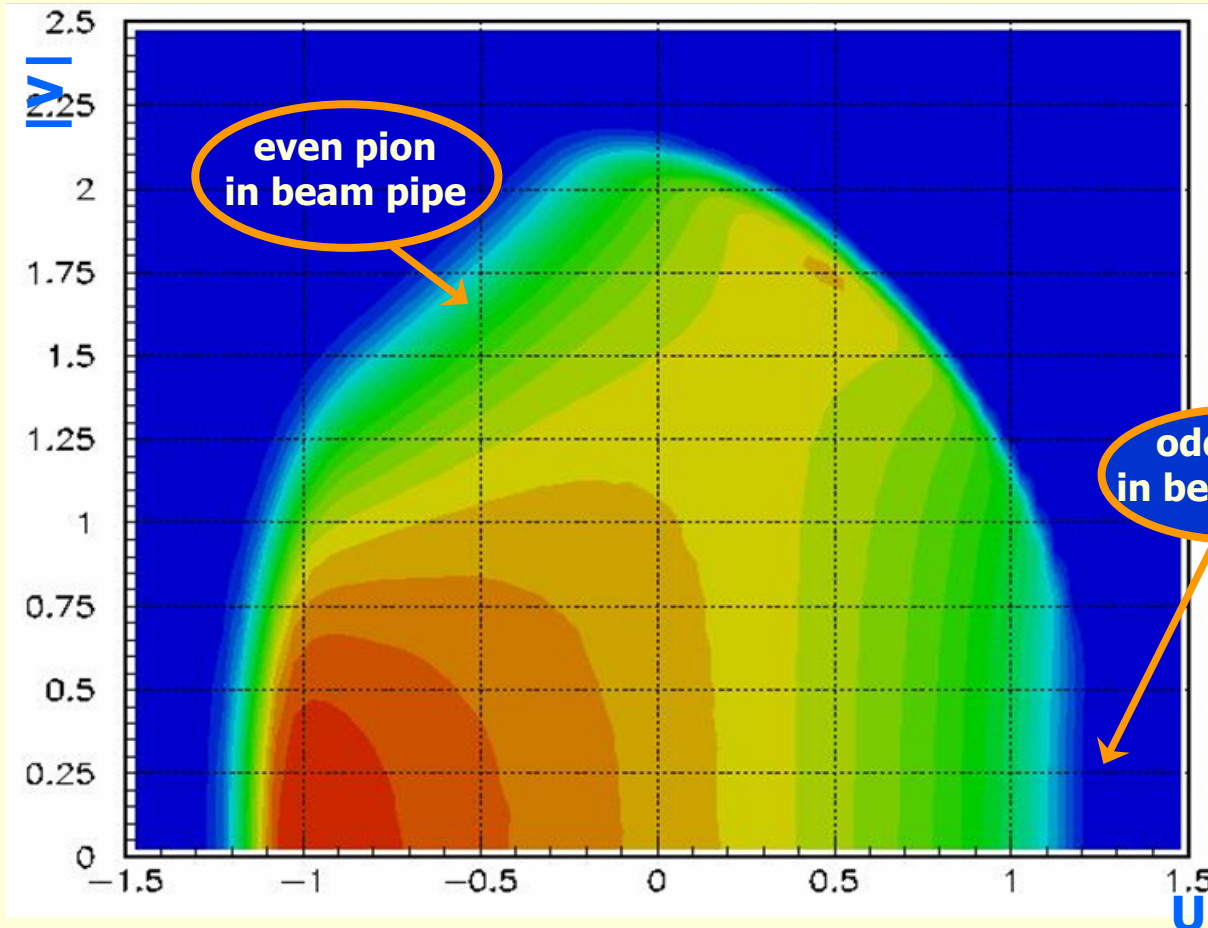
- $K^\pm \rightarrow \pi^0 \pi^0 \pi^\pm$ :  $\sim 2 \cdot 10^8$

~ 200 TB of data recorded

The result based on **2003**  $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$  sample will be presented here

# Accepted statistics

**Data-taking 2003:**  
 **$1.61 \times 10^9$   $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$  events**

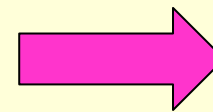


**$K^+$ :  $1.03 \times 10^9$  events**  
 **$K^-$ :  $0.58 \times 10^9$  events**  
 **$K^+/K^- \approx 1.8$**

# Method to extract $A_g$

- Build  $u$  projections of the Dalitz plot for  $K^+$  and  $K^-$ :  $N^+(u), N^-(u)$
- Make the ratio of these two distributions:  $R(u)$
- Fit a linear function to this ratio to extract  $\Delta g = g^+ - g^-$

$$R(u) = \frac{N^+(u)}{N^-(u)} \propto \frac{1 + g^+ u}{1 + g^- u} \approx 1 + \Delta g u$$



$$A_g = \frac{\Delta g}{2g}$$

This holds only if the acceptance for

$K^+$  and  $K^-$  is the same

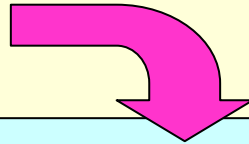
$$\delta A_g < 2.2 \cdot 10^{-4}$$

$$\delta \Delta g < 0.9 \cdot 10^{-4}$$

The **magnetic fields** (achromat and spectrometer) are *intrinsic sources of charge asymmetry* in the detector!!!

# Instrumental asymmetries

In real life



- ✓ Detector acceptance asymmetries
- ✓ Time variation of detector response
- ✓ Charge-dependent beam optics
- ✓ Time variation of beams' properties
- ✓ Spurious magnetic fields
- ✓ Charge-asymmetric interactions

# Strategy of data taking

**Beam line** (achromat) polarity (**A**) reversed on weekly basis  
**Spectrometer magnet** polarity (**B**) reversed on daily basis

Example: August 6 to September 7, 2003

Week 1	<b>Achromat –</b>	<b>B+</b> <b>B-</b> <b>B+</b> <b>B-</b> <b>B+</b> <b>B-</b>	<b>Supersample 1</b> <b>12 subsamples</b>
Week 2	<b>Achromat +</b>	<b>B+</b> <b>B-</b> <b>B+</b> <b>B-</b> <b>B+</b> <b>B-</b>	
Week 3	<b>Achromat –</b>	<b>B+</b> <b>B-</b> <b>B+</b> <b>B-</b> <b>B+</b> <b>B-</b>	<b>Supersample 2</b> <b>12 subsamples</b>
Week 4	<b>Achromat +</b>	<b>B+</b> <b>B-</b> <b>B+</b> <b>B-</b> <b>B+</b> <b>B-</b>	
Week 5	<b>Achromat –</b>	<b>B+</b> <b>B-</b>	<b>Supersample 3</b> <b>4 subsamples</b>
	<b>Achromat +</b>	<b>B+</b> <b>B-</b>	



# Acceptance cancellation

Detector left-right asymmetry cancels  
in 4 ratios of  $K^+/K^-$  distributions:

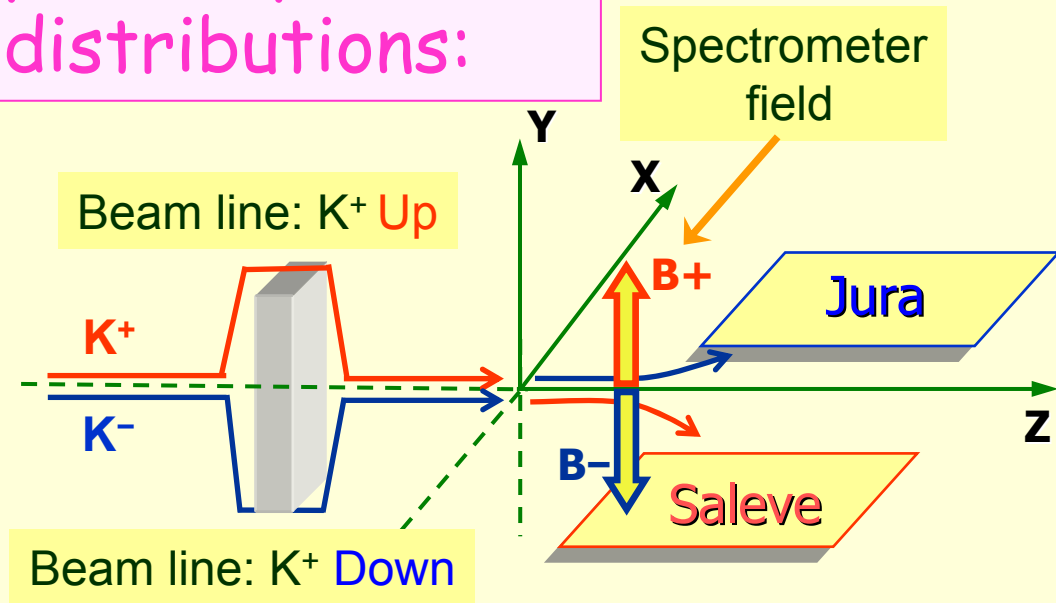
(same deviation by spectrometer  
in numerator and denominator)

$$R_{US} = \frac{N(A+B+K^+)}{N(A+B-K^-)}$$

$$R_{UJ} = \frac{N(A+B-K^+)}{N(A+B+K^-)}$$

$$R_{DS} = \frac{N(A-B+K^+)}{N(A-B-K^-)}$$

$$R_{DJ} = \frac{N(A-B-K^+)}{N(A-B+K^-)}$$



Indexes correspond to

- beamline polarity (U / D)
- direction of kaon deviation in spectrometer (S / J)

# Quadruple ratio

$$R = R_{US} R_{UJ} R_{DS} R_{DJ} \sim 1 + 4\Delta g \cdot u$$

## 3-fold cancellation of systematic biases:

- 1) Global **time**-variable biases ( $K^+$ ,  $K^-$  simultaneously recorded)
- 2) **Beam** line biases ( $K^+$  beam up /  $K^-$  beam up etc.)
- 3) **Detector** asymmetries ( $K^+$  toward Saleve /  $K^-$  toward Saleve etc.)
- 4) Effects of **permanent stray fields** (earth, vacuum tank magnetisation) cancel

The result is sensitive only to time variation of asymmetries in experimental conditions with a characteristic time smaller than corresponding field-alternation period (beam-week, detector-day)

# Monte Carlo simulation

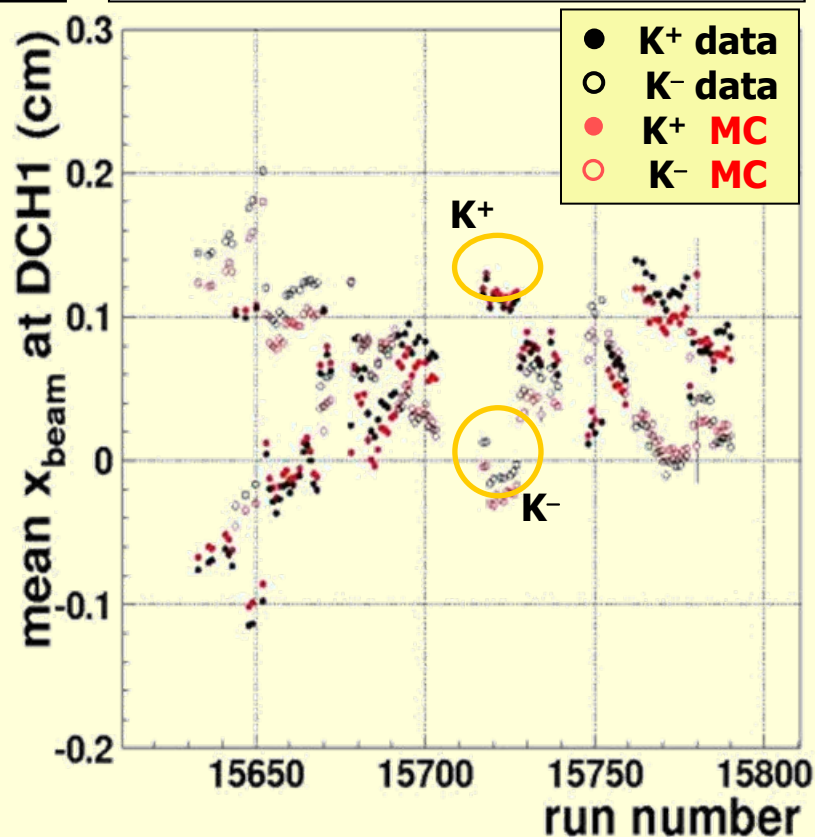
Due to acceptance cancellations, the analysis does not rely on Monte-Carlo to calculate acceptance

Still MC is used to study systematics.

MC features:

- Based on GEANT
- Full detector geometry and material description
- Local DCH inefficiencies simulated
- Variations of beam geometry and DCH alignment are followed
- Simulated statistics similar to experimental one.

Example of data/MC agreement: mean beam positions @DCH1



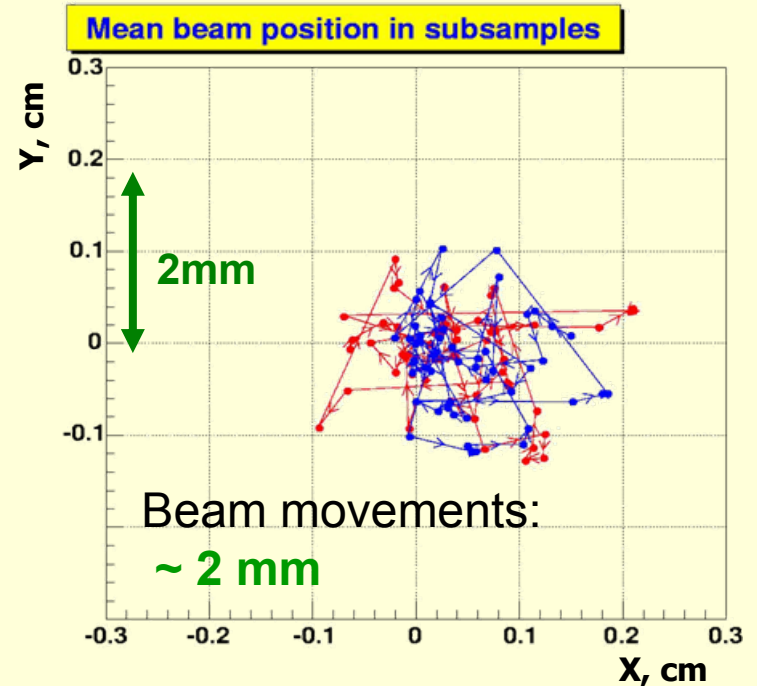
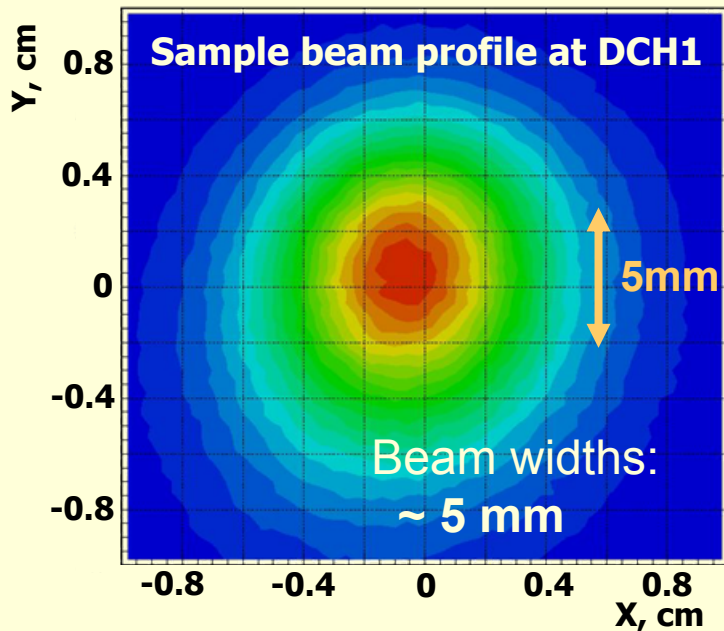
# Beam systematics

## Time variations of beam geometry

Acceptance largely defined by central beam hole edge.

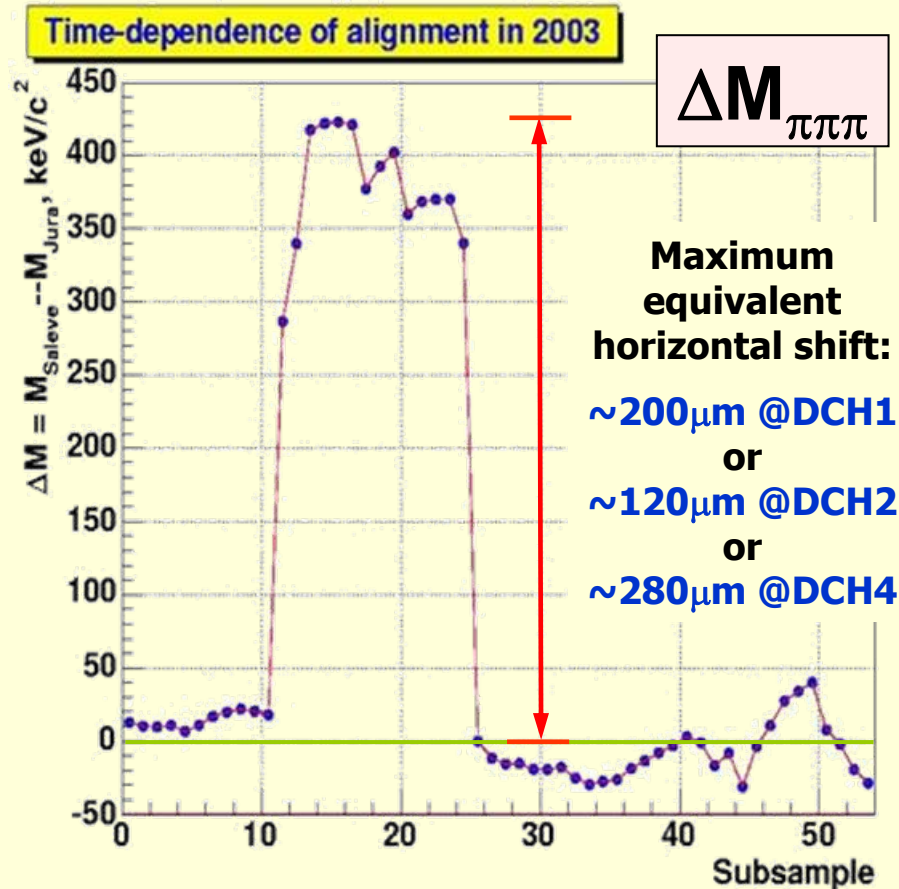
Acceptance **cut** defined by (larger) **"virtual pipe"** centered on averaged beam positions as a function of **charge, time and K momentum**

Effects due to beam movements and not perfect overlap corrected



# Spectrometer systematics

Time variations of spectrometer geometry - Alignment is fine tuned by forcing mean reconstructed invariant  $\pi\pi\pi$  masses to be equal for  $K^+$  and  $K^-$



E.g. sensitivity to DCH4 horizontal shift:  $\Delta M/\Delta x \approx 1.5 \text{ keV}/\mu\text{m}$

## Momentum scale

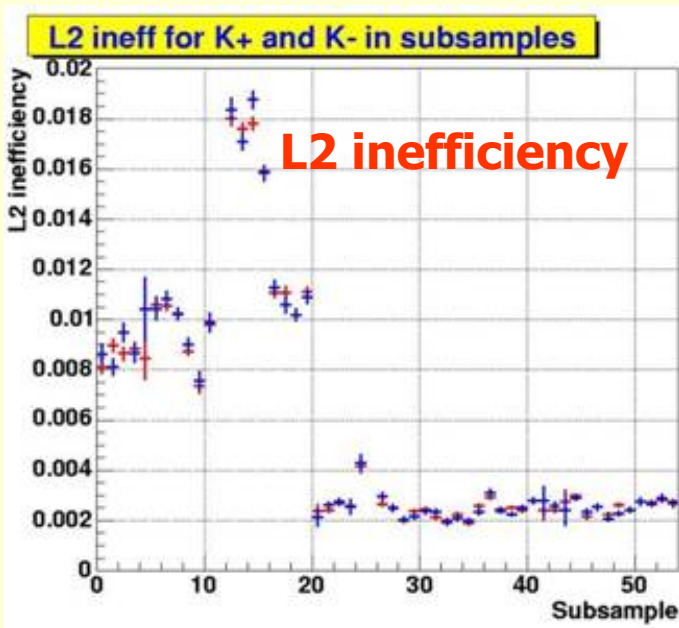
variation due to limited control of spectrometer magnet current ( $10^{-3}$ ) cancels due to **simultaneous beams**

In addition, it is **adjusted** by forcing mean reconstructed invariant  $\pi\pi\pi$  masses to PDG value of  $M_{K^+}$

# Trigger systematics

**L1 trigger** (2 hodoscope hits): **stable** and **small** inefficiency:  $1-e \approx 0.7 \cdot 10^{-3}$ , **charge-symmetric**, **flat** in  $u$  **NO CORRECTION NEEDED**

**L2 trigger** (online vertex reconstruction on DCH data): **time-varying** inefficiency (local DCH inefficiencies)  $1-e \approx 0.2\%$  to  $1.8\%$ , **flat** in  $u$  within measurement precision  $u$ -dependent **CORRECTION APPLIED**

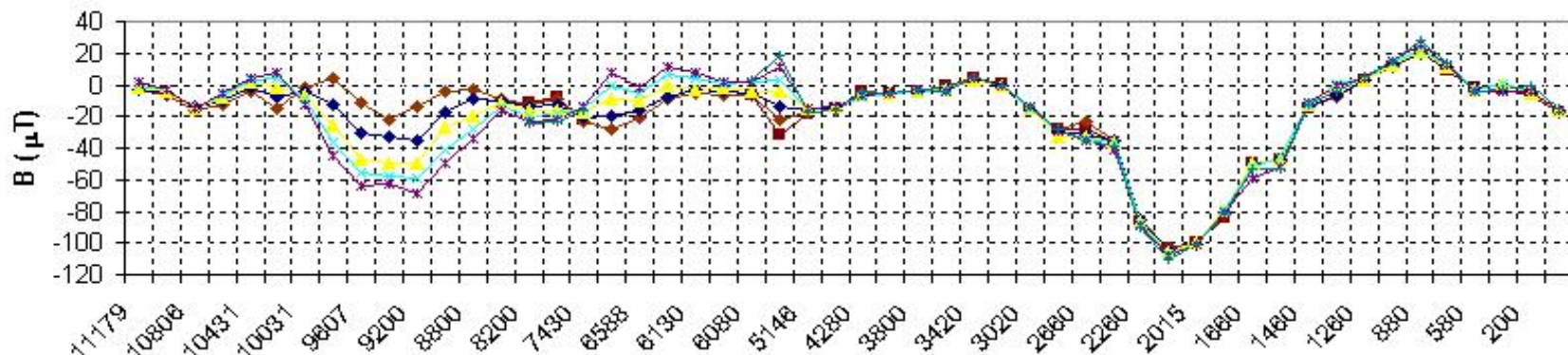


	L2 correction $\delta \Delta g \times 10^4$
SS0	$0.5 \pm 1.8$
SS1	$1.4 \pm 1.0$
SS2	$-0.2 \pm 1.2$
SS3	$-4.5 \pm 1.9$

statistical uncertainty  
from control sample



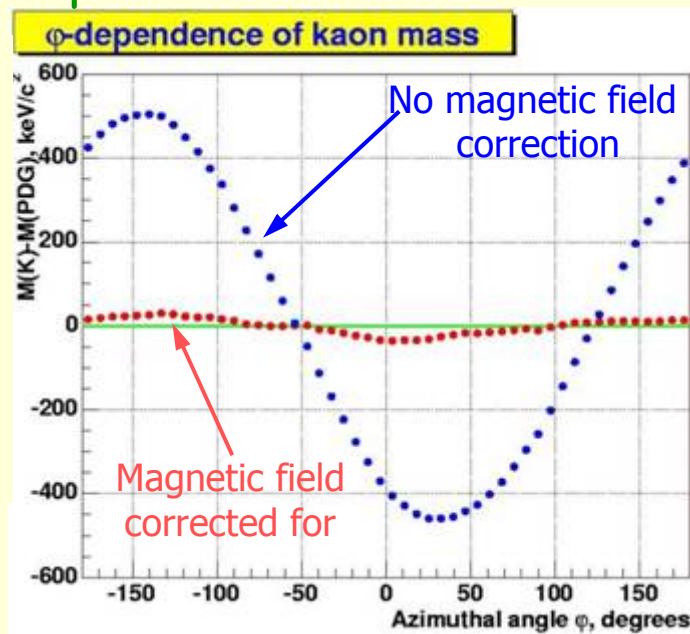
# Other systematics



Residual effects of **stray magnetic fields** (magnetised vacuum tank, earth field) minimised by explicit **field map correction**

## Further systematic effects studied

- Bias due to **resolution** in  $u$  calculation
- Sensitivity to **fitting interval and method**
- Effects connected to  $\pi \rightarrow \mu \nu$  decay
- Effects due to event **pile-up**
- $\pi^+/\pi^-$  interactions in material
- Track **charge misidentification**



# Systematics summary and result

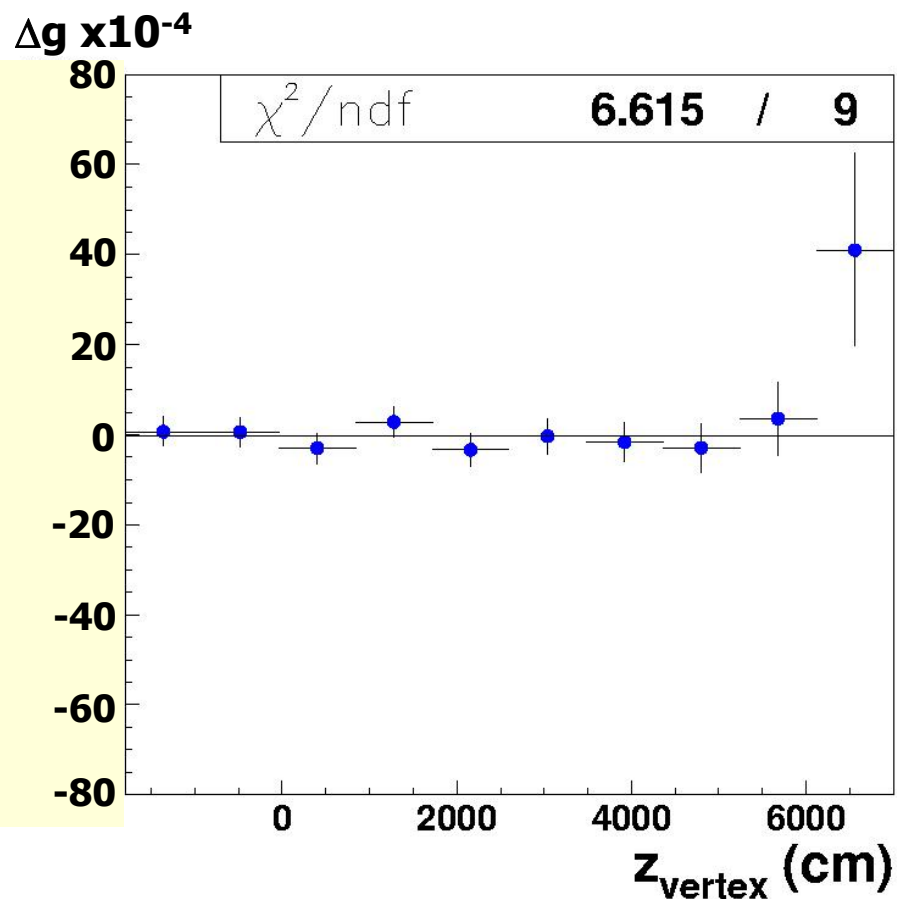
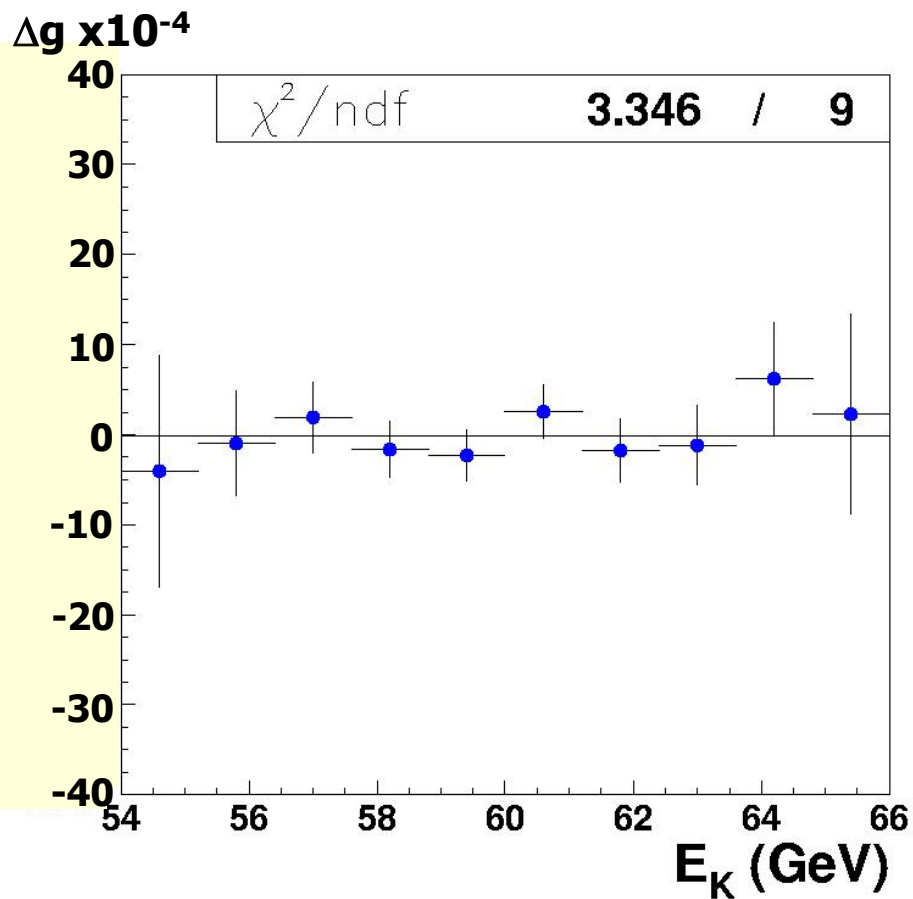
Conservative estimations of systematic errors	Effect on $\Delta \times 10^4$
Acceptance and beam geometry	0.5
Spectrometer alignment	0.1
Analyzing magnet field	0.1
$\pi^\pm \rightarrow \mu\nu$ decay	0.4
U calculation and fitting	0.5
Pile-up	0.3
Syst. errors of statistical nature	
Trigger efficiency: L2	0.8
Trigger efficiency: L1	0.4
<b>Total systematic error</b>	<b>1.3</b>

Combined preliminary result:  
 in  $\Delta g \times 10^4$  units  
 (3 independent analyses)  
 Including L2 trigger correction

	Raw	Corrected for L2 eff
SS0	0.0 $\pm$ 1.5	0.5 $\pm$ 2.4
SS1	0.9 $\pm$ 2.0	2.2 $\pm$ 2.2
SS2	-2.8 $\pm$ 2.2	-3.0 $\pm$ 2.5
SS3	2.0 $\pm$ 3.4	-2.6 $\pm$ 3.9
<b>Total</b>	<b>-0.2<math>\pm</math>1.0</b>	<b>-0.2<math>\pm</math>1.3</b>
$\chi^2$	2.2/3	3.2/3



# Result stability



# Preliminary result (2003 data)

slope difference

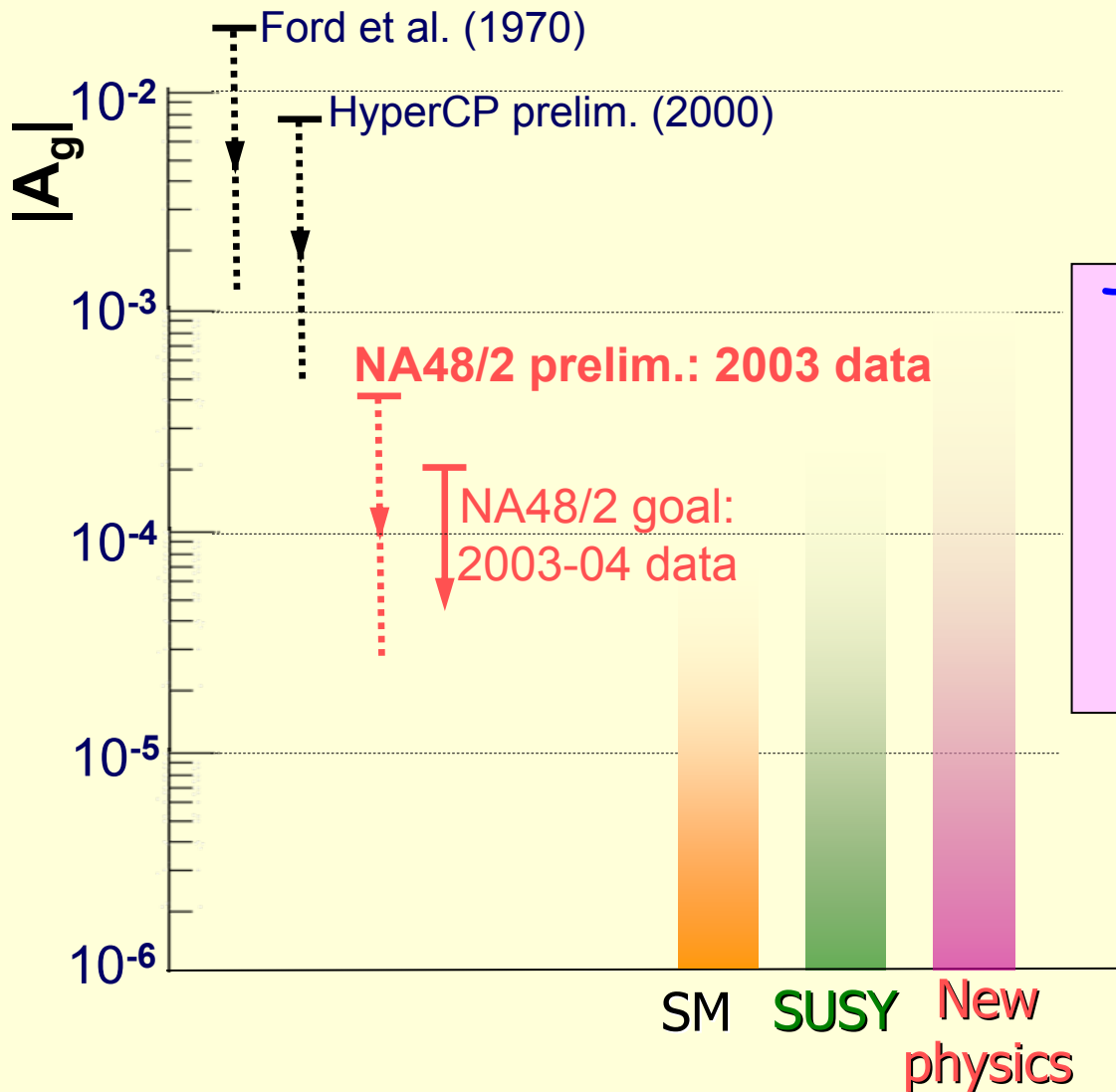
$$\Delta g = (-0.2 \pm 1.0_{\text{stat.}} \pm 0.9_{\text{stat. (trig.)}} \pm 0.9_{\text{syst.}}) \times 10^{-4}$$
$$\Delta g = (-0.2 \pm 1.7) \times 10^{-4}$$

charge asymmetry

$$A_g = (0.5 \pm 2.4_{\text{stat.}} \pm 2.1_{\text{stat. (trig.)}} \pm 2.1_{\text{syst.}}) \times 10^{-4}$$
$$A_g = (0.5 \pm 3.8) \times 10^{-4}$$

- This is a preliminary result with **conservative** estimate of systematic uncertainties
- Extrapolated statistical uncertainty 2003+2004:  $\delta A_g = 1.6 \times 10^{-4}$
- Expect **smaller systematic effects** in 2004 data  
(due to more frequent polarity alternation, better L2 performance).

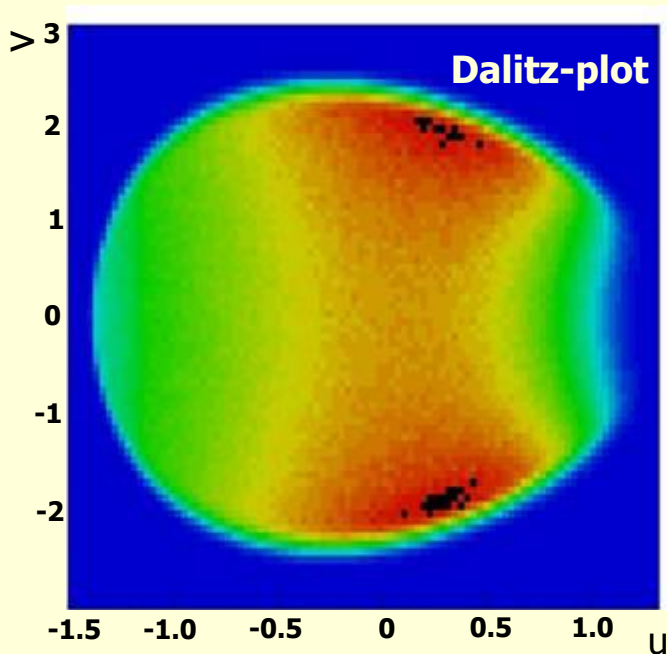
# Comparison $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$



This preliminary result is already an order of magnitude better than previous experiments

# $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$ analysis

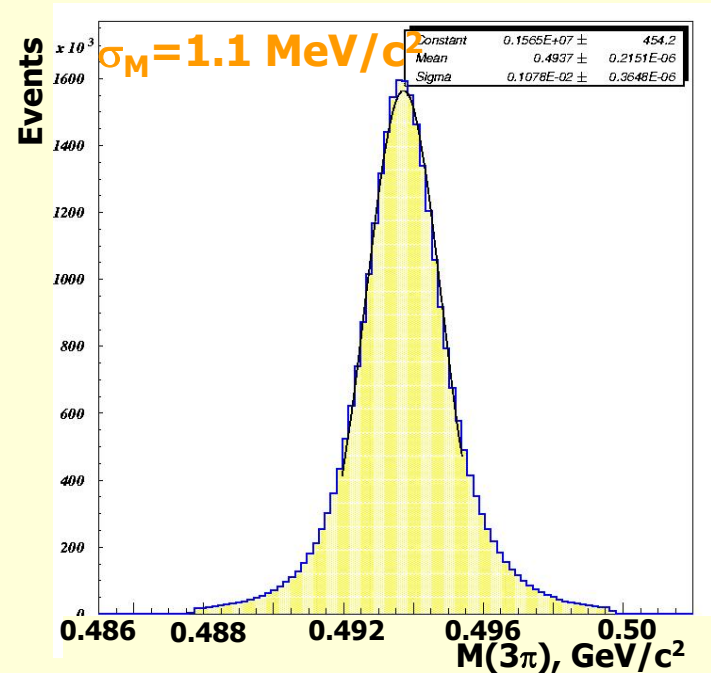
“neutral” mode wrt “charged”



- ❖ Same strategy of analysis
- ❖ Only the Lkr used to define u
- ❖ Totally different systematics
- ❖ Statistical precision in  $A_g^0$  similar
  - ✓ Ratio of “neutral” to “charged” statistics:  $N^0/N^\pm \sim 1/20$  ( $J=1/4.5$ )
  - ✓ Ratio of slopes:  $|g^0/g^\pm| \approx 3$
  - ✓ More favourable Dalitz-plot distribution (gain factor  $f \sim 1.5$ )

# Status of analysis

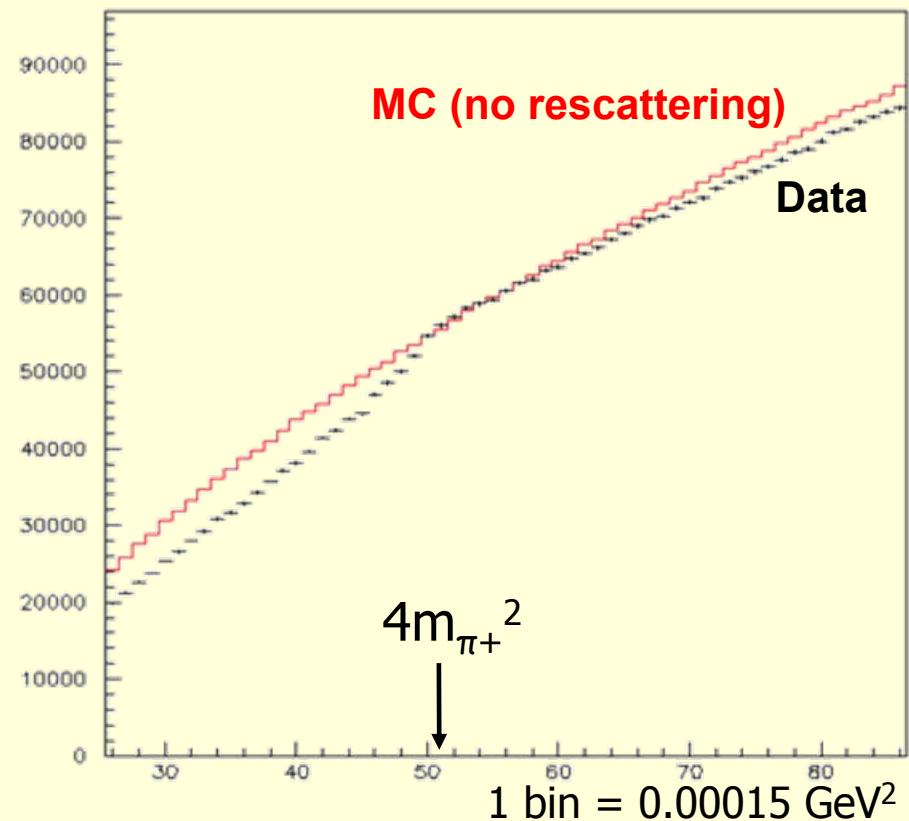
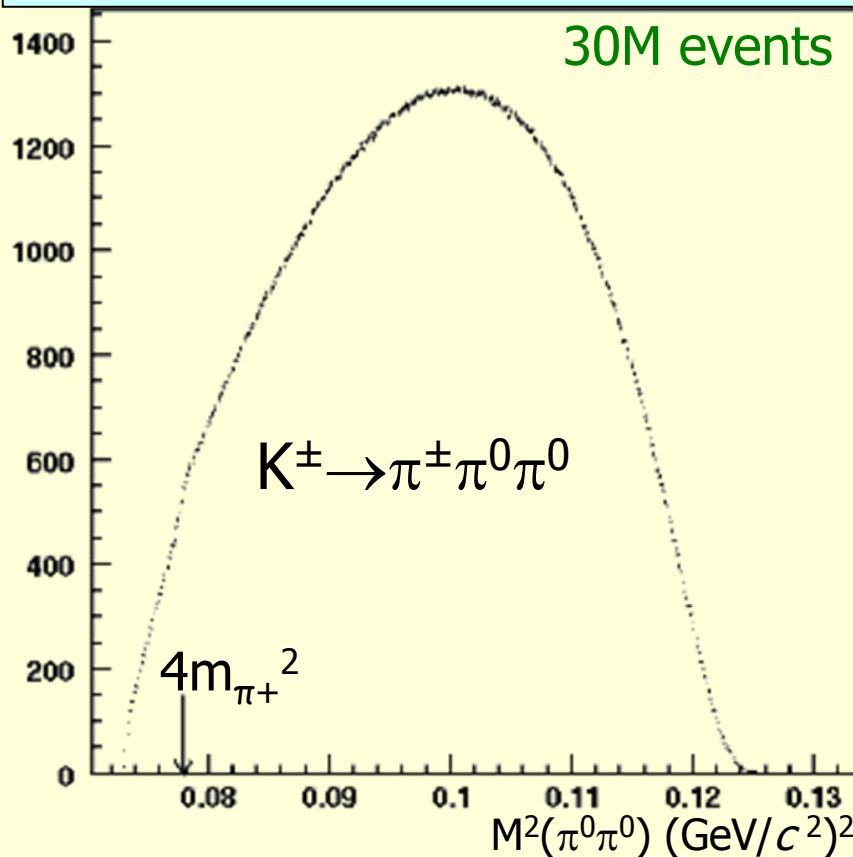
- Statistics analyzed:  
 $50 \times 10^6$  events
- Statistical error with analyzed data:  
 $\delta A_g(\text{stat}) = 1.7 \times 10^{-4}$
- Extrapolation to 2003+2004 data ( $115 \times 10^6$ )  
 $\delta A_g(\text{stat}) = 1.1 \times 10^{-4}$



Preliminary results will be announced soon

# Observation of $\pi\pi$ scattering effect in $K \rightarrow 3\pi$ decays

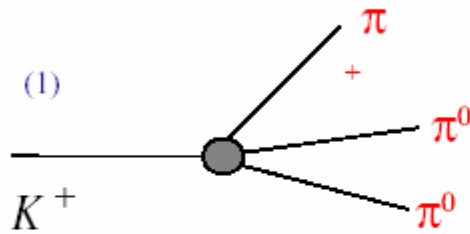
Thanks to the large statistics in the neutral mode we can see (for the first time) the contribution of the **charge exchange process**  $\pi^+\pi^- \rightarrow \pi^0\pi^0$  in the  $K^\pm \rightarrow \pi^0\pi^0\pi^\pm$  decay. This effect stimulated some theoretical work



# $(a_0 - a_2)$ determination in $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$

Two processes contribute to  $K^+ \rightarrow \pi^+ \pi^0 \pi^0$

- 1) Direct emission of  $\pi^+ \pi^0 \pi^0$
- 2)  $\pi^0 \pi^0$  produced in charged pions rescattering

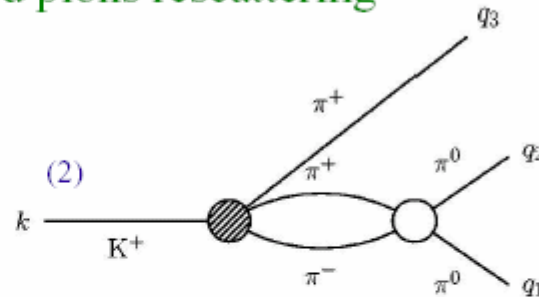


$$\mathcal{M}_0 = 1 + gu/2$$

$$u = 2m_K(m_K/3 - E_{\text{odd}}^*)/m_\pi^2$$

$$g = 0.638 \pm 0.020$$

(present PDG value)



$$\mathcal{M}_1 \propto (a_0 - a_2)$$

- Small Pionium formation also expected

$$d\Gamma/dm_{\pi\pi} \propto |\mathcal{M}_0 + \mathcal{M}_1|^2$$

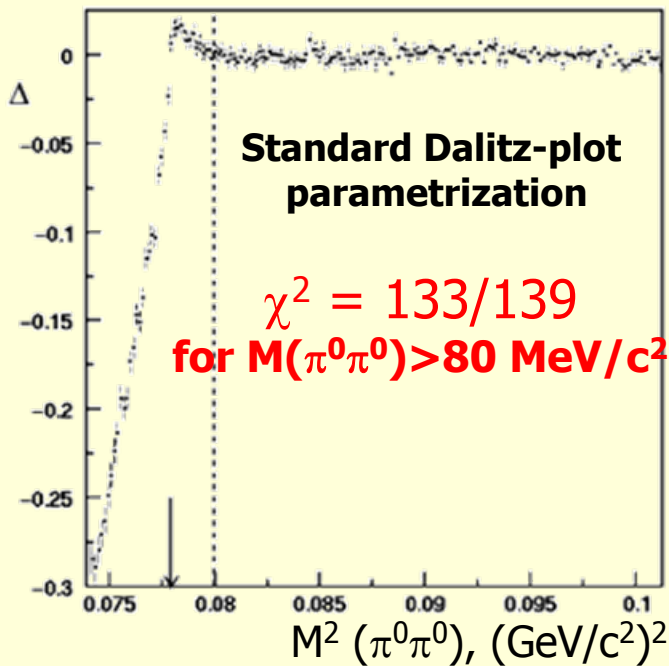
**Interference is expected**

*N. Cabibbo, hep-ph/0405001 Phys. Rev. Lett. 93, 121801 (2004) one loop calculation*

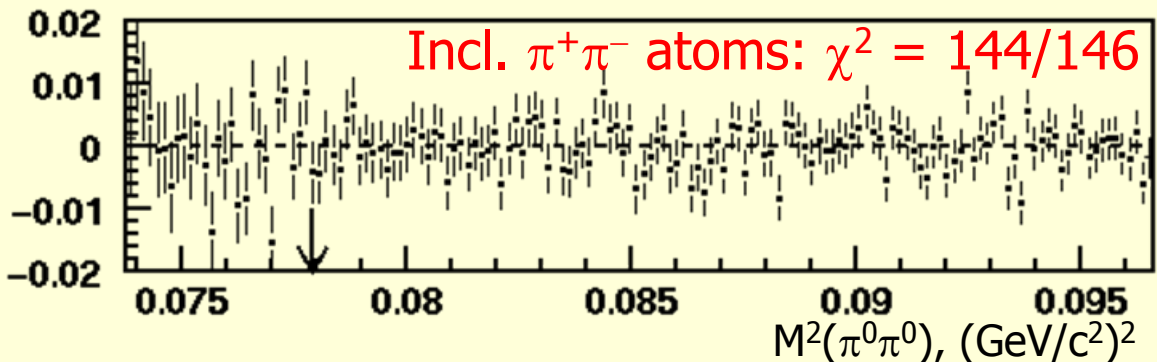
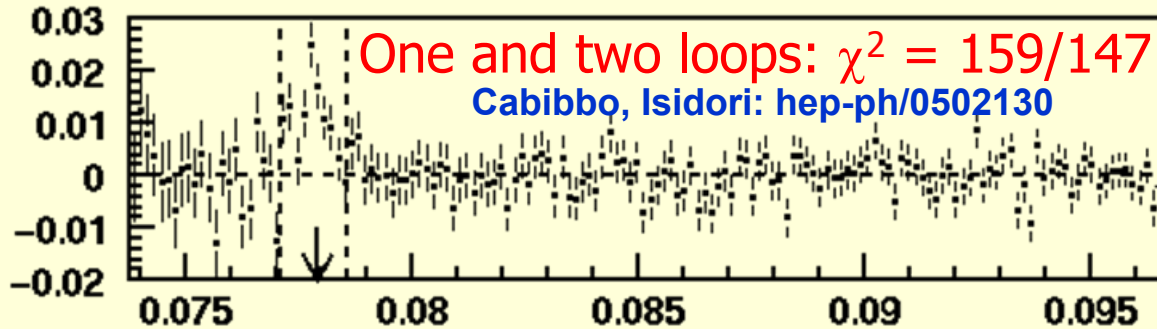
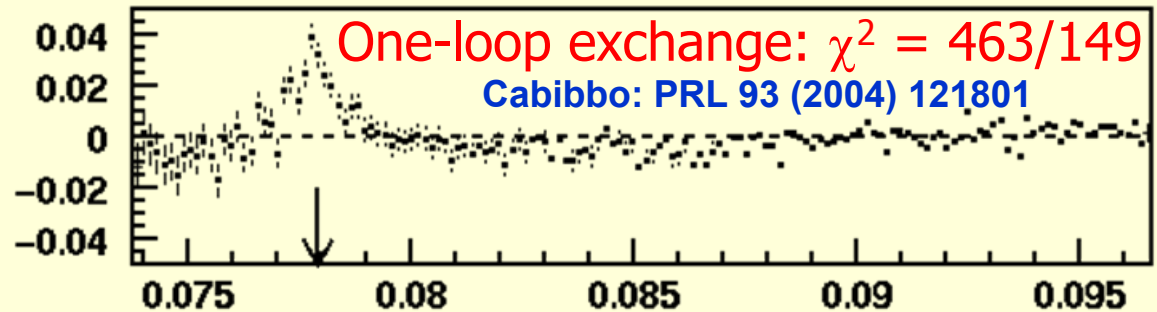
*N. Cabibbo and G. Isidori, hep-ph/0502130 Phys. Rev. Lett. 93, 121801 (2005) two loops*

# Fits to the "cusp" effect in $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$

$$\Delta = (\text{data} - \text{fit}) / \text{data}$$

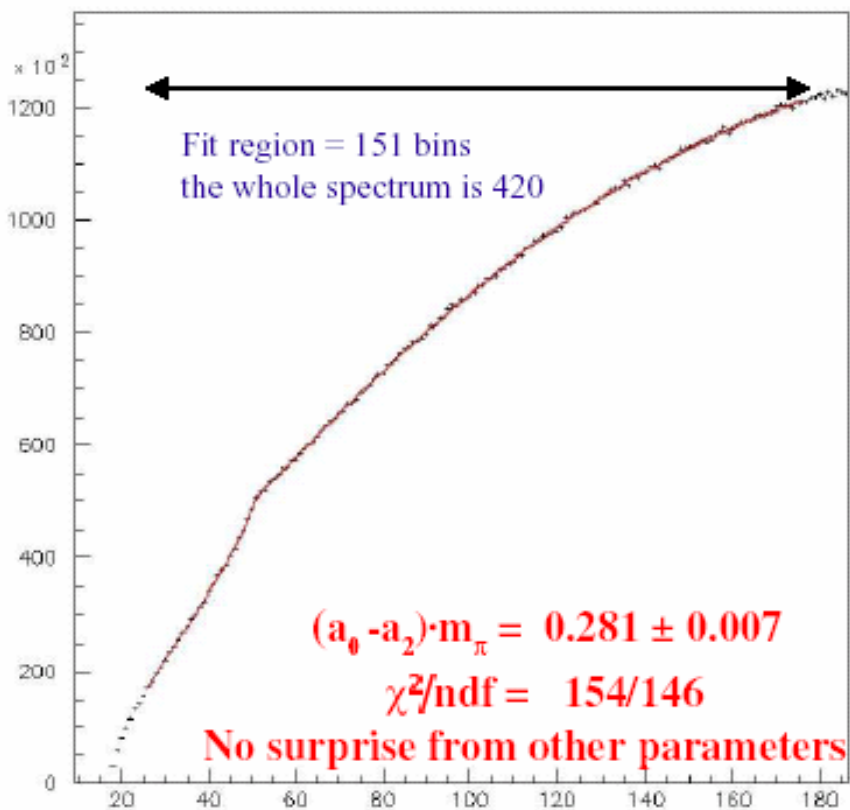


The best fit obtained with two loops adding a small amount of pionium to improve the  $\chi^2$





# Preliminary result



the pionium contribution has been fixed to the prediction:  
Z.K. Silagadze, hep-ph/9411382

$$\frac{K^+ \rightarrow \pi^+ + \text{pionium}}{K^+ \rightarrow \pi^+ \pi^+ \pi^-} \approx 7.4 \times 10^{-6}$$

$(a_0 - a_2)m_+$   $\longrightarrow$  has low sensitivity to pionium

$$(a_0 - a_2)m_+ = 0.281 \pm 0.007(\text{stat}) \pm 0.014(\text{syst}) \pm 0.014(\text{theor})$$

In agreement with theory  $(a_0 - a_2)m_+ = 0.265 \pm 0.004$  (Colangelo 2001)

# Conclusions

- Preliminary NA48/2 result (only 2003 data) on direct CP-violating charge asymmetry in  $K^{\pm} \rightarrow \pi^{\pm}\pi^+\pi^{-}$  decays is  
 $A_g = (0.5 \pm 2.4_{\text{stat.}} \pm 2.1_{\text{stat. (trig.)}} \pm 2.1_{\text{syst.}}) \times 10^{-4}$
- x 10 times better precision than previous measurements
- Further room to decrease systematic error (trigger efficiency)
- 2004 data contains another  $2 \times 10^9$   $K^{\pm} \rightarrow \pi^{\pm}\pi^+\pi^{-}$  events, possibly with higher quality → Design goal within reach
- $K^{\pm} \rightarrow \pi^{\pm}\pi^0\pi^0$  neutral asymmetry: complementary, comparable sensitivity
- “Cusp” effect: determination of the  $\pi\pi$  scattering lengths
- A lot of other interesting results coming (other CP asymmetries, rare decays)

SPARE SLIDES

# $K_{3\pi}^{\pm}$ decays

$BR(K^{\pm} \rightarrow \pi^{\pm} \pi^+ \pi^-) = 5.57\%$   
"charged"

Kinematic variables

## Lorentz-invariants

$$u = (s_3 - s_0) / m_{\pi}^2;$$

$$v = (s_2 - s_1) / m_{\pi}^2;$$

$$s_i = (P_K - P_{\pi_i})^2, \quad i=1,2,3 \quad (3=\text{odd } \pi);$$

$$s_0 = (s_1 + s_2 + s_3) / 3.$$

## Centre of mass frame

$$u = 2m_K \cdot (m_K/3 - E_{\text{odd}}) / m_{\pi}^2;$$

$$v = 2m_K \cdot (E_1 - E_2) / m_{\pi}^2.$$

$BR(K^{\pm} \rightarrow \pi^{\pm} \pi^0 \pi^0) = 1.73\%$

"neutral"

Matrix element

parameterized in terms of slopes

$$|M(u,v)|^2 \sim 1 + gu + hu^2 + kv^2$$

Measured quantity  
sensitive to

direct CP violation:

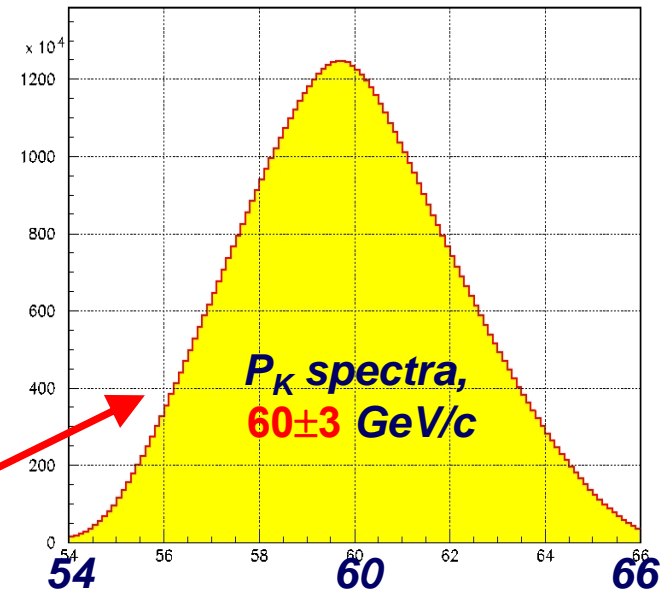
Slope asymmetry:

$$A_g = (g_+ - g_-) / (g_+ + g_-)$$

# NA48/2 narrow-band beams

simultaneous, coaxial, focused

Beam	Positive	Negative
Primary proton momentum	400 GeV/c	
Duty cycle	5.2 s / 16.8 s	
Protons on target per	10 <sup>12</sup>	
Production angle	0	
Beam acceptance	±0.36 mrad	
Beam momentum	(60 ± 3) GeV/c	
Beamline length	102 m	
p / $\bar{p}$ per cycle (10 <sup>6</sup> )	8.6	0.9
$\pi^+$ / $\pi^-$ per cycle (10 <sup>6</sup> )	33.2	24.6
K <sup>+</sup> / K <sup>-</sup> per cycle (10 <sup>6</sup> )	3.1	1.8
Decay region	115 m	



⇒ Pion decay products stay in beam pipe...

# Theoretical predictions of $A_g$

Standard Model	L.Maiani, N.Paver '95	$(2.3 \pm 0.6) \times 10^{-6}$
	A. Bel'kov '95	$< 4 \times 10^{-4}$
	G.D'Ambrosio, G.Isidori '98	$< 10^{-5}$
	E.Shabalin '01	$< 3 \times 10^{-5}$
	E.Gamiz, J.Prades, I.Scimemi '03	$(-2.4 \pm 1.2) \times 10^{-5}$
	E.Shabalin '05 (La Thuile'05)	$< 8 \times 10^{-5}$
SUSY	G.D'Ambrosio, G.Isidori, G.Martinelli	$\sim 10^{-4}$
New physics	E.Shabalin '98 [Weinberg model of extended Higgs doublet]	$\sim 4 \times 10^{-4}$
	I.Scimemi '04	$> 3 \times 10^{-5}$

# More cancellations

(1) **Double ratio** cancellation of **global time instabilities** (rate effects, *simultaneous beams*):

$$R_U = R_{US} \times R_{UJ} \quad \Rightarrow \quad R(u) = n \cdot (1 + 2 \Delta g_U u)$$

$$R_D = R_{DS} \times R_{DJ} \quad \Rightarrow \quad R(u) = n \cdot (1 + 2 \Delta g_D u)$$

(2) **Double ratio** cancellation of **beam geometry difference** effects:

$$R_S = R_{US} \times R_{DS} \quad \Rightarrow \quad R(u) = n \cdot (1 + 2 \Delta g_S u)$$

$$R_J = R_{UJ} \times R_{DJ} \quad \Rightarrow \quad R(u) = n \cdot (1 + 2 \Delta g_J u)$$

(3) Fit with **quadruple ratio**:

$$R = R_{US} \times R_{UJ} \times R_{DS} \times R_{DJ} \quad \Rightarrow \quad R(u) = n \cdot (1 + 4 \Delta g u)$$

↓ Normalization    ↓ Slope difference

The fit result is sensitive only to **time variation** of **asymmetries** in experimental conditions on a time-scale of  $\sim 1$  subsample

# Break down of $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ statistics

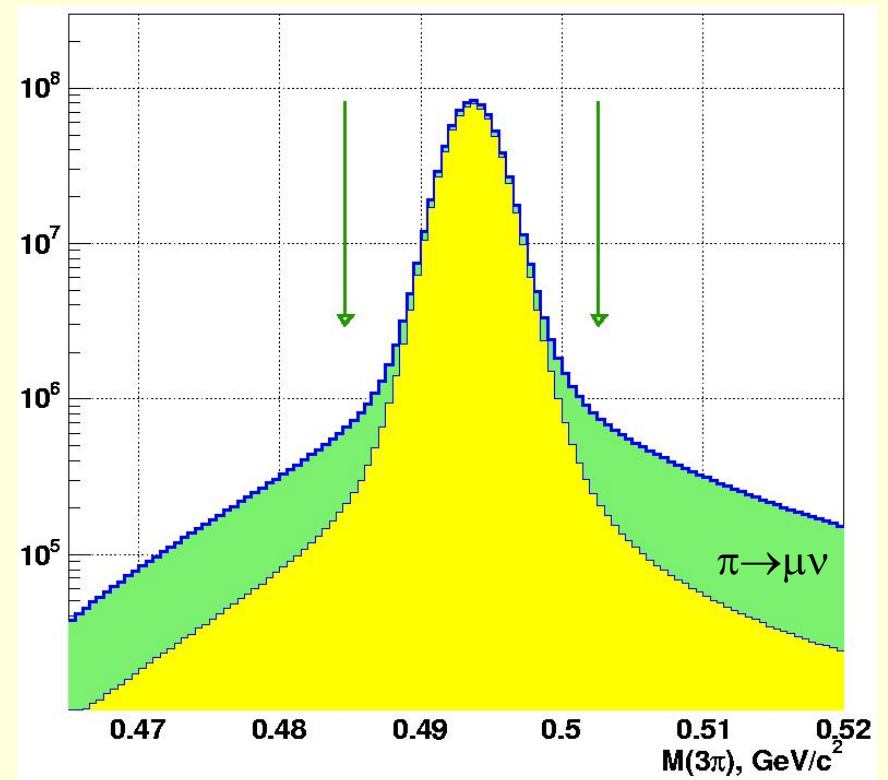
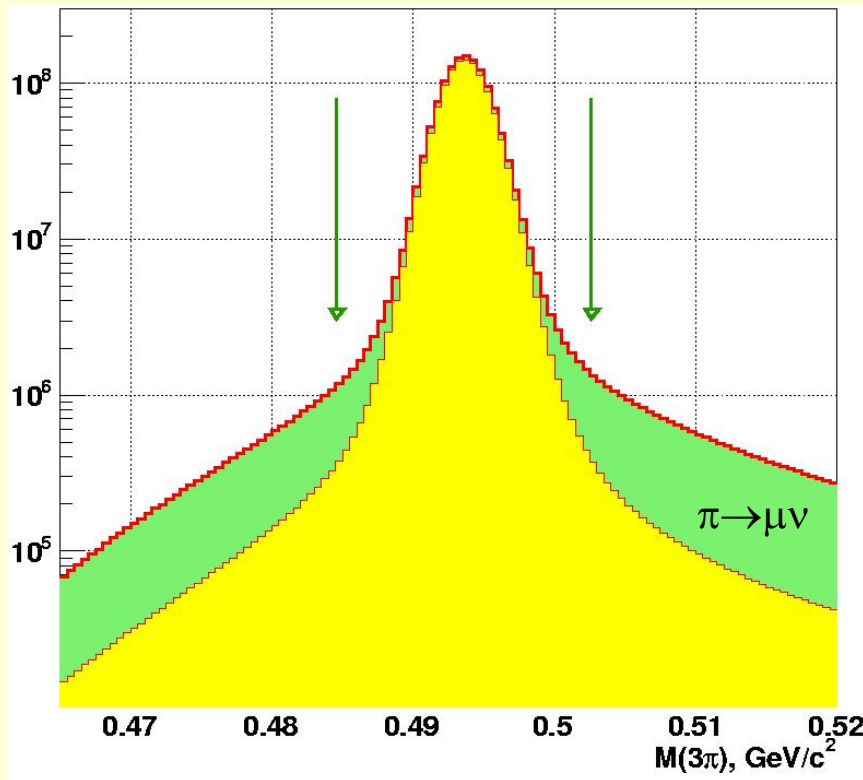
## Statistics selected for $A_g$ measurement, events $\times 10^6$

	Dates	Sub-samples	Achromat A+		Achromat A-	
			$K^+$	$K^-$	$K^+$	$K^-$
0	22.06-25.07	26	229.6	125.9	201.0	114.0
1	6.08-20.08	12	122.5	68.1	135.1	75.4
2	20.08-3.09	12	147.2	81.8	105.5	58.9
3	3.09-7.09	4	40.6	22.6	54.5	30.4
Total		54	Total events selected			1613.2



# Invariant $\pi\pi\pi$ mass

$$\sigma_M = 1.7 \text{ MeV}/c^2$$



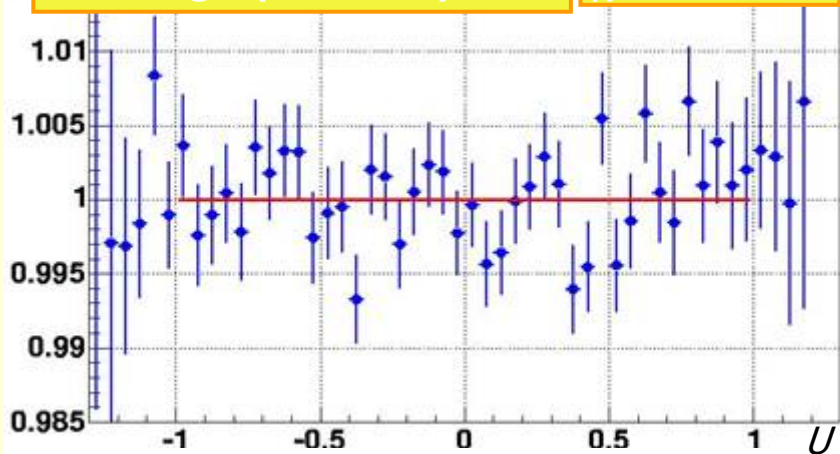
$K^+$  :  $1.03 \times 10^9$  events

No significant  
background

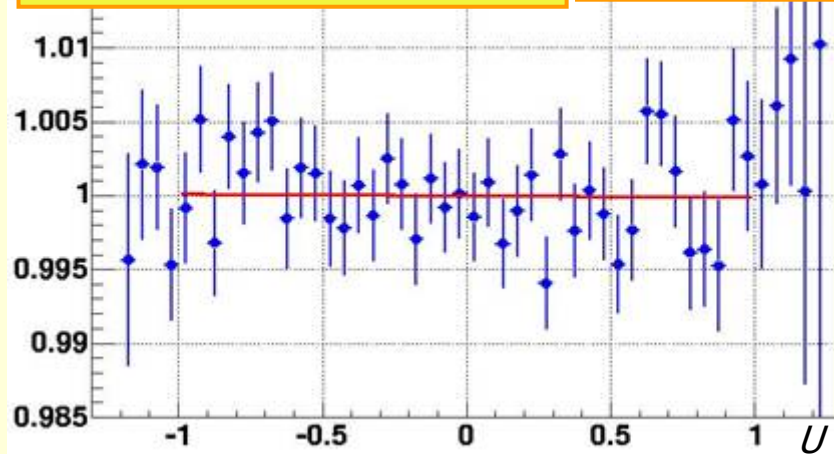
$K^-$  :  $0.58 \times 10^9$  events

# Fit linearity - four supersamples

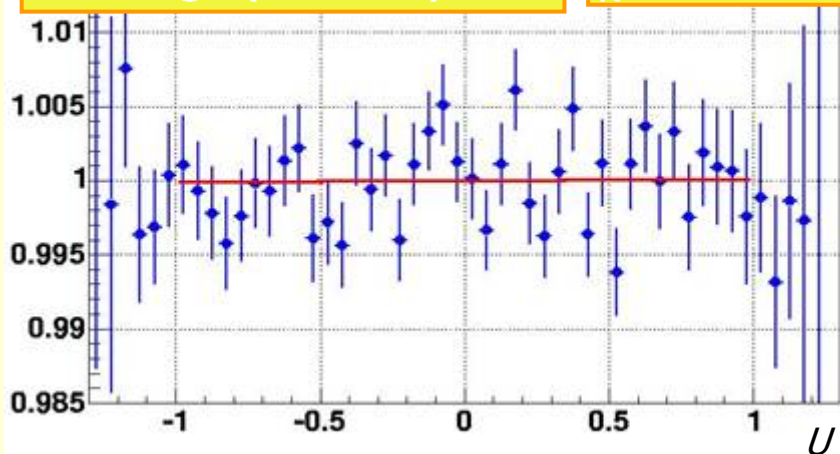
SS0:  $\Delta g = (0.6 \pm 2.4) \times 10^{-4}$   $\chi^2 = 39.7/38$



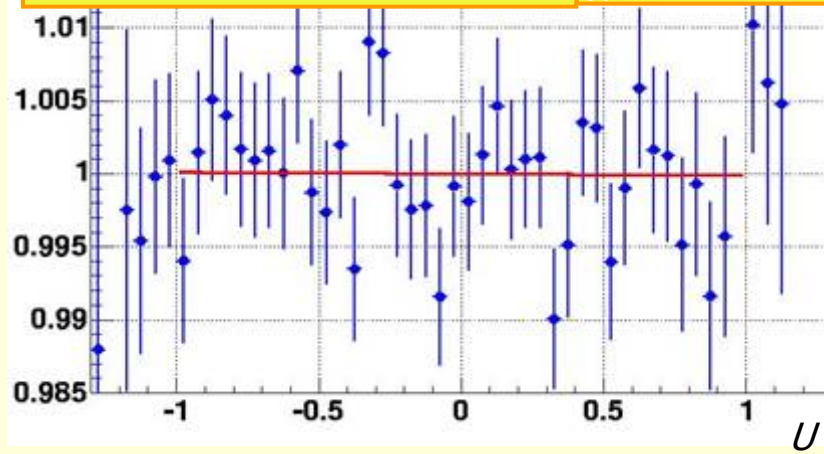
SS2:  $\Delta g = (-3.1 \pm 2.5) \times 10^{-4}$   $\chi^2 = 29.5/38$



SS1:  $\Delta g = (2.3 \pm 2.2) \times 10^{-4}$   $\chi^2 = 38.1/38$



SS3:  $\Delta g = (-2.9 \pm 3.9) \times 10^{-4}$   $\chi^2 = 32.9/38$

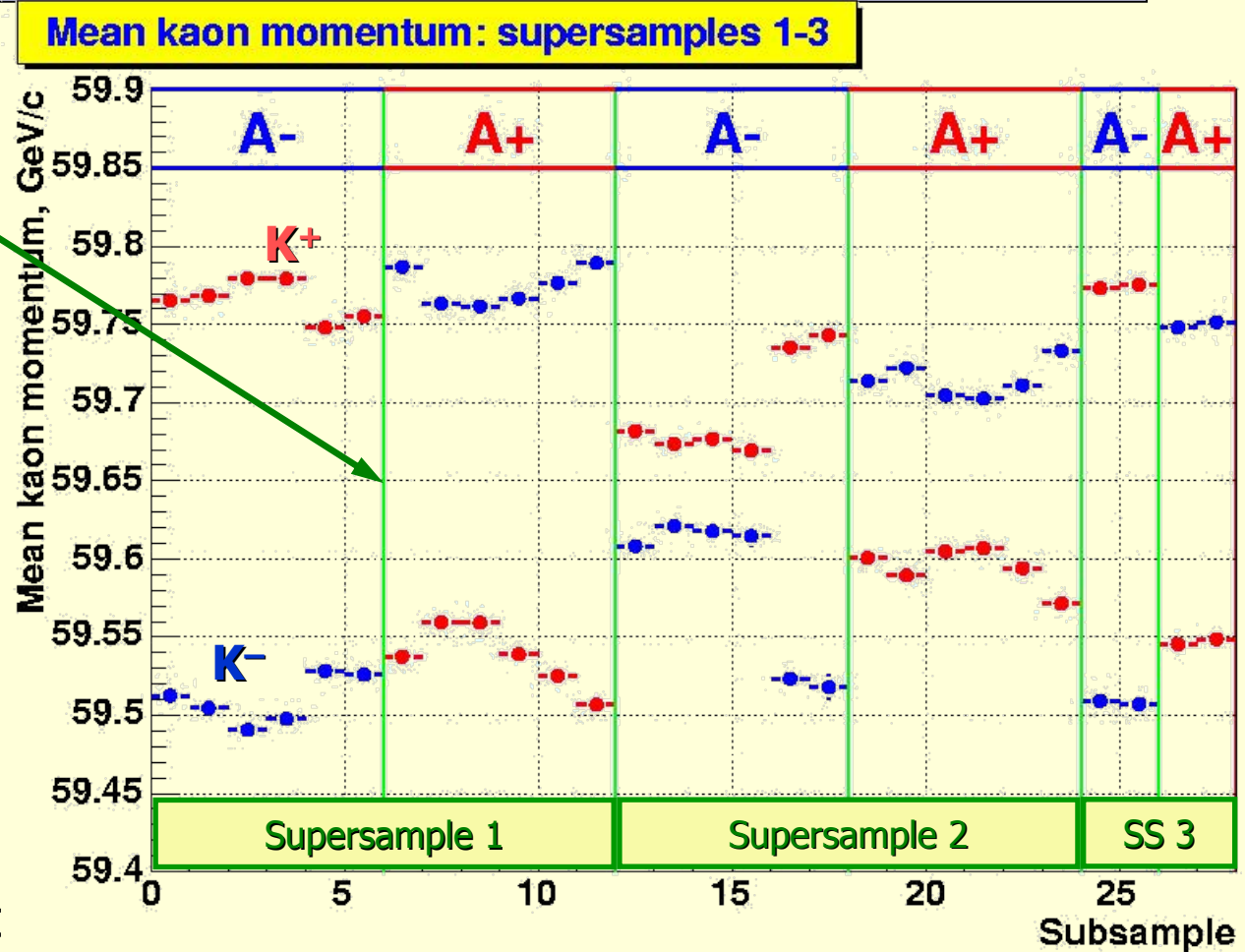


# Cancellation of beam spectra

Achromat reversal  
reverses  $K^+$  and  $K^-$   
beam spectra

Systematic differences  
of  $K^+$  and  $K^-$  acceptance  
due to beam spectra  
mostly cancel in  $R_U * R_D$

Systematic check:  
Reweighting  $K^+$  events  
so as to equalise  
momentum spectra  
leads to negligible effect  
 $\delta\Delta g = 0.03 \times 10^{-4}$



# Theoretical predictions

**Weinberg (1966)**

Effective field theory for  
strong interaction at low E

$$a_0 m_{\pi^+} = \frac{7m_{\pi^+}^2}{16\pi f_{\pi}^2} = 0.159$$

$$a_2 m_{\pi^+} = \frac{-m_{\pi^+}^2}{8\pi f_{\pi}^2} = -0.045$$

Most recently

**Colangelo (2001)**

$\chi$ pt -theory two loops

*Ref: hep-ph/0103088*

$$a_0 m_{\pi^+} = 0.220 \pm 0.005$$

$$a_2 m_{\pi^+} = -0.0444 \pm 0.0010$$

$$(a_0 - a_2) m_{\pi^+} = 0.265 \pm 0.004$$

- **2% level of accuracy:** quite unusual for hadronic physics  
experiments have not yet reached the same level

# Experimental status

1977: measurement by Genève/Saclay experiment @ **20% accuracy**

2003: **BNL E865** extracts  $a_0$  at **5% accuracy** by measuring the form factors of the decay  $K \rightarrow \pi\pi e\nu$  with 400,000 events

$$a_0 m = 0.216 \pm 0.013 (\text{stat.}) \pm 0.002 (\text{syst.}) \pm 0.002 (\text{theor.})$$

*Ref. Pislak et al. (2003) hep-ex/0301040*

Present: Cern experiment **DIRAC**, with a sophisticated technique, aims to measure the pionium lifetime @ **10% accuracy**

$$\tau \sim 40 \cdot (\mathbf{a}_0 - \mathbf{a}_2)^2 \cdot 10^{-15} \text{ sec}$$