

RQM & CQMs

GBE CQM  
OGE CQM  
II CQM

Spectra

Ew Structure

PF ew FFs  
Diff. RCQMs  
PF vs. IF

Decays

$\pi$ ,  $\eta$ , K

Multiplets

PDG  
Systematics  
QM Classif.  
Wave Functions  
Decays

Summary

# Baryon Resonances and Strong Decays

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## Theoretical Framework

### Point form QM and relativistic CQM

## Baryon Spectroscopy

## Electroweak Nucleon and Hyperon Structure

## Hadronic Decays

## Multiplet Classification of Baryons

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## Relativistic quantum mechanics (RQM)

i.e. **quantum theory** respecting **Poincaré invariance**  
 (theory on  $\mathcal{H}$  corresponding to a finite number of particles,  
 not a field theory)

### Invariant mass operator

$$\hat{M} = \hat{M}_{free} + \hat{M}_{int}$$

### Eigenvalue equations

$$\begin{aligned} \hat{M} |P, J, \Sigma\rangle &= M |P, J, \Sigma\rangle \quad , & \hat{M}^2 &= \hat{P}^\mu \hat{P}_\mu \\ \hat{P}^\mu |P, J, \Sigma\rangle &= P^\mu |P, J, \Sigma\rangle \quad , & \hat{P}^\mu &= \hat{M} \hat{V}^\mu \end{aligned}$$

## Interacting mass operator

$$\hat{M} = \hat{M}_{free} + \hat{M}_{int}$$

$$\hat{M}_{free} = \sqrt{\hat{H}_0^2 - \hat{\vec{P}}_{free}^2}$$

$$\hat{M}_{int} = \sum_{i < j}^3 \hat{V}_{ij} = \sum_{i < j} [\hat{V}_{ij}^{conf} + \hat{V}_{ij}^{hf}]$$

fulfilling the **Poincaré algebra**

$$\begin{aligned} [\hat{P}_i, \hat{P}_j] &= 0, & [\hat{J}_i, \hat{H}] &= 0, & [\hat{P}_i, \hat{H}] &= 0, \\ [\hat{K}_i, \hat{H}] &= -i\hat{P}_i, & [\hat{J}_i, \hat{J}_j] &= i\epsilon_{ijk}\hat{J}_k, & [\hat{J}_i, \hat{K}_j] &= i\epsilon_{ijk}\hat{K}_k, \\ [\hat{J}_i, \hat{P}_j] &= i\epsilon_{ijk}\hat{P}_k, & [\hat{K}_i, \hat{K}_j] &= -i\epsilon_{ijk}\hat{J}_k, & [\hat{K}_i, \hat{P}_j] &= -i\delta_{ij}\hat{H} \end{aligned}$$

$\hat{H}, \hat{P}_i$  ... time and space translations,

$\hat{J}_i$  ... rotations,  $\hat{K}_i$  ... Lorentz boosts

## Goldstone-Boson-Exchange CQM

$$H_0 = \sum_{i=1}^3 \sqrt{\vec{p}_i^2 + m_i^2}$$

$$V_{conf}(\vec{r}_{ij}) = V_0 + C r_{ij}$$

$$V_{hf}(\vec{r}_{ij}) = \left[ \sum_{F=1}^3 V_{\pi}(\vec{r}_{ij}) \lambda_i^F \lambda_j^F + \sum_{F=4}^7 V_{K}(\vec{r}_{ij}) \lambda_i^F \lambda_j^F + V_{\eta}(\vec{r}_{ij}) \lambda_i^8 \lambda_j^8 + \frac{2}{3} V_{\eta'}(\vec{r}_{ij}) \right] \vec{\sigma}_i \cdot \vec{\sigma}_j$$

L.Ya. Glozman, W. Plessas, K. Varga, and R.F. Wagenbrunn: Phys. Rev. D **58**, 094030 (1998)

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## One-Gluon-Exchange CQM

(Relativistic version of the Bhaduri-Cohler-Nogami OGE CQM)

$$H_0 = \sum_{i=1}^3 \sqrt{\vec{p}_i^2 + m_i^2}$$

$$V_{conf} = V_0 + Cr_{ij}$$

$$V_{hf} = -\frac{2b}{3r_{ij}} + \frac{\alpha_s}{9m_i m_j} \Lambda^2 \frac{e^{-\Lambda r_{ij}}}{r_{ij}} \vec{\sigma}_i \cdot \vec{\sigma}_j$$

L. Theussl, R.F. Wagenbrunn, B. Desplanques, and W. Plessas: Eur. Phys. J. A **12**, 91 (2001)

## Instanton-Induced CQM

(Relativistic CQM by the Bonn group)

$$H_0 = \sum_{i=1}^3 \sqrt{\vec{p}_i^2 + m_i^2}$$

$$V_{conf} = V_0 + Cr_{ij}$$

$$V_{hf} = V'_{t\text{Hooft}}$$

Relativistic framework: Bethe-Salpeter equation

U. Löring, B.Ch. Metsch, and H.R. Petry: Eur. Phys. J. A **10**, 395 (2001); ibid. 447 (2001)

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# Eigenvalue Spectra

of

# Invariant Mass Operator



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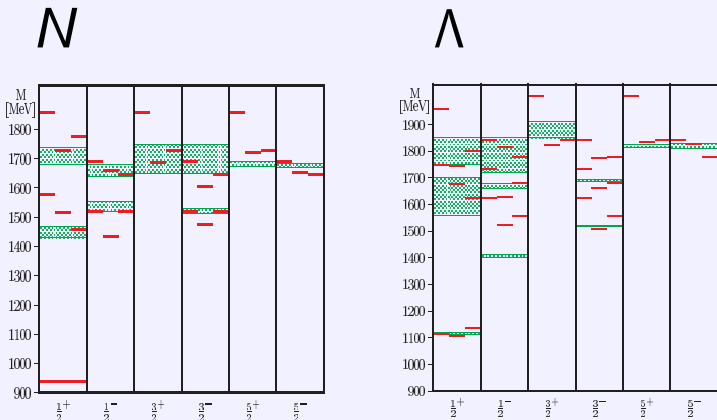
## Decays

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## Summary



left: **OGE CQM**

middle: **II CQM**

right: **GBE CQM**

W. Plessas: Few-Body Syst. Suppl. **15**, 139 (2003)

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**Electromagnetic and Axial Nucleon Form Factors**

as well as

**Electric Radii and Magnetic Moments of Hyperons**

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- ▶ **Electron** scattering on the nucleons

$$G_E^p, G_M^p, r_E^p, \mu^p; G_E^n, G_M^n, r_E^n, \mu^n$$

- ▶ **Neutrino** scattering on the nucleon

$$G_A, G_P$$

- ▶ **Electron** scattering on the hyperons

$$r_E^Y, \mu^Y$$

## Poincaré algebra

$$\begin{aligned}
 [P_i, P_j] &= 0, & [J_i, H] &= 0, & [P_i, H] &= 0, \\
 [K_i, H] &= -iP_i, & [J_i, J_j] &= i\epsilon_{ijk}J_k, & [J_i, K_j] &= i\epsilon_{ijk}K_k, \\
 [J_i, P_j] &= i\epsilon_{ijk}P_k, & [K_i, K_j] &= -i\epsilon_{ijk}J_k, & [K_i, P_j] &= -i\delta_{ij}H
 \end{aligned}$$

## Point form

$J_i$  and  $K_i$  interaction-free (6 out of 10 generators)

$P^\mu = (H, \vec{P})$  **interaction-dependent**

## Instant form

$J_i$  and  $P_i$  interaction-free (6 out of 10 generators)

$P^0 = H$  and  $K_i$  **interaction-dependent**

## Covariant predictions of the GBE CQM:

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### Spectra

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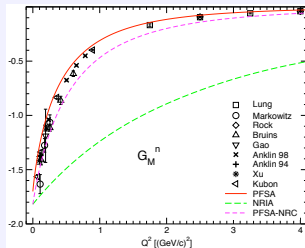
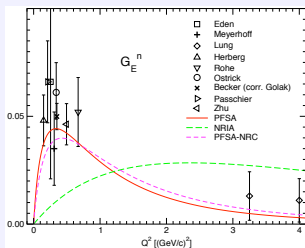
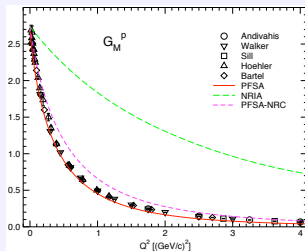
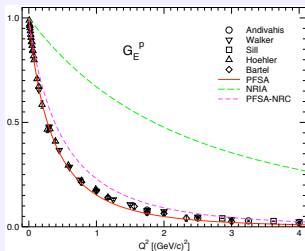
### Decays

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### Multiplets

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## Electric radii

Baryon	GBE PFSA	Experiment
$p$	0.82	$0.7569 \pm 0.0139$
$n$	-0.13	$-0.1161 \pm 0.0022$
$\Sigma^-$	0.72	$0.61 \pm 0.12 \pm 0.09$

## Magnetic moments

Baryon	GBE PFSA	Experiment
$p$	2.70	2.792847351
$n$	-1.70	-1.91304273
$\Lambda$	-0.64	$-0.613 \pm 0.004$
$\Sigma^+$	2.38	$2.458 \pm 0.010$
$\Sigma^-$	-0.93	$-1.160 \pm 0.025$
$\Xi^0$	-1.25	$-1.250 \pm 0.014$
$\Xi^-$	-0.70	$-0.6507 \pm 0.0025$
$\Delta^+$	2.08	$2.7^{+1.0}_{-1.3} \pm 1.5 \pm 3$
$\Delta^{++}$	4.17	3.7 - 7.5
$\Omega^-$	-1.59	$-2.020 \pm 0.05$

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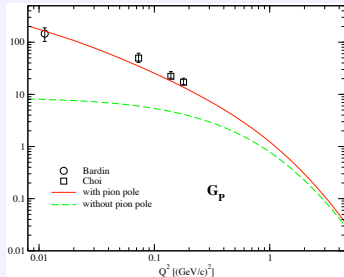
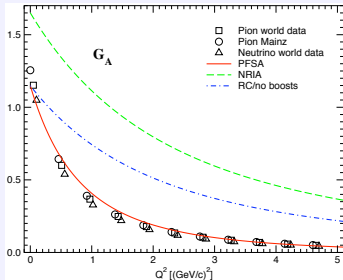
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## Covariant predictions of the GBE CQM:



## Different Quark Model Predictions:

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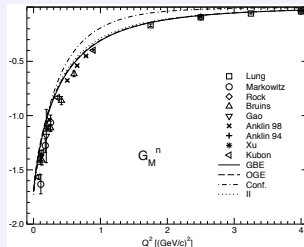
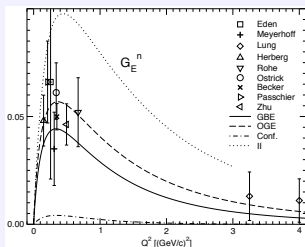
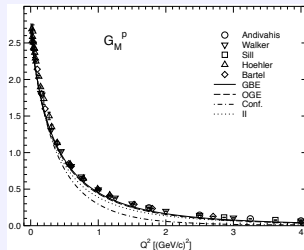
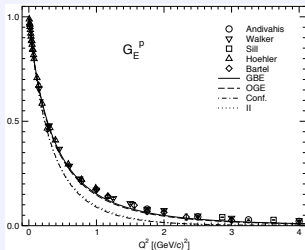
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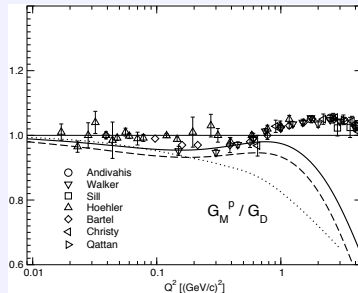
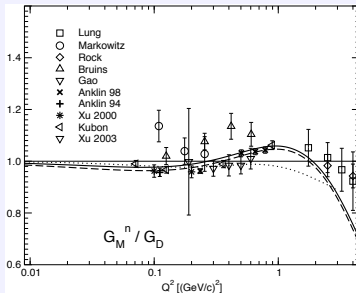
$\pi$ ,  $\eta$ ,  $K$

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solid: GBE CQM

dashed: OGE CQM

dotted: II CQM

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# Point Form vs. Instant Form Calculations of Nucleon Electromagnetic Form Factors

## Point-Form vs. Instant-Form Spectator Approximation:

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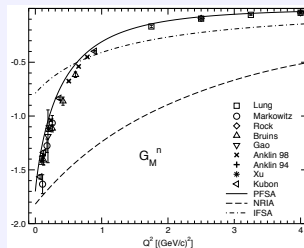
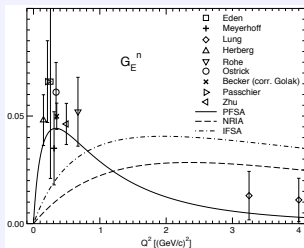
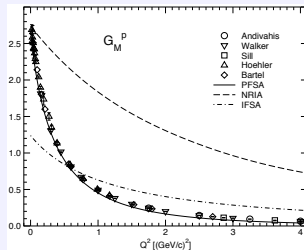
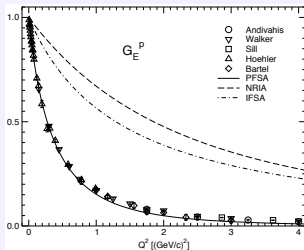
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**Point-Form** vs. **Instant-Form** Spectator Approximation:

$$r_E^2 \text{ [fm}^2\text{]}$$

### GBE CQM

	IFSM	PFSM	NRIA	Experiment
Proton	0.156	0.824	0.102	$0.7569 \pm 0.0139$
Neutron	-0.020	-0.135	-0.009	$-0.1161 \pm 0.0022$

$$\mu \text{ [n.m.]}$$

### GBE CQM

	IFSM	PFSM	NRIA	Experiment
Proton	1.24	2.70	2.74	2.792847351
Neutron	-0.79	-1.70	-1.82	-1.91304273

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## Summary

$\pi$ ,  $\eta$ , and  $K$  Decay Modes

of

$N^*$ ,  $\Delta^*$ ,  $\Lambda^*$ ,  $\Sigma^*$ ,  $\Xi^*$  Resonances

# $\pi$ Decay Widths of $N^*$ and $\Delta^*$

	$N^*, \Delta^*$ $\rightarrow N\pi$	Experiment [MeV]	Relativistic			Nonrel. EEM	
			GBE	OGE	II	GBE	OGE
RQM & CQMs	$N(1440)$	$(227 \pm 18)_{-59}^{+70}$	30	59	38	7	27
	$N(1520)$	$(66 \pm 6)_{-5}^{+9}$	21	23	38	38	37
Spectra	$N(1535)$	$(67 \pm 15)_{-17}^{+28}$	25	39	33	559	1183
Ew Structure	$N(1650)$	$(109 \pm 26)_{-3}^{+36}$	6.3	9.9	3	157	352
	$N(1675)$	$(68 \pm 8)_{-4}^{+14}$	8.4	10.4	4	13	16
Decays	$N(1700)$	$(10 \pm 5)_{-3}^{+3}$	1.0	1.3	0.1	2.2	2.7
	$N(1710)$	$(15 \pm 5)_{-5}^{+30}$	19	21		8	6
Multiplets	$\Delta(1232)$	$(119 \pm 1)_{-5}^{+5}$	35	31	62	89	85
	$\Delta(1600)$	$(61 \pm 26)_{-10}^{+26}$	0.5	5.1		93	86
Wave Functions	$\Delta(1620)$	$(38 \pm 8)_{-6}^{+8}$	1.2	2.8	4	76	177
	$\Delta(1700)$	$(45 \pm 15)_{-10}^{+20}$	3.8	4.1	2	10.4	9.1

With theoretical masses

T. Melde, W. Plessas, and R.F. Wagenbrunn: Phys. Rev. C **72**, 015207 (2005); ibid. **74**, 069901 (2006)

# $\pi$ Decay Widths of $N^*$ and $\Delta^*$

	$N^*, \Delta^*$ $\rightarrow N\pi$	Experiment [MeV]	Relativistic		Nonrel. EEM	
			GBE	OGE	GBE	OGE
RQM & CQMs  GBE CQM OGE CQM II CQM	$N(1440)$	$(227 \pm 18)_{-59}^{+70}$	28	<u>39</u>	6	14
	$N(1520)$	$(66 \pm 6)_{-5}^{+9}$	22	23	38	36
	$N(1535)$	$(67 \pm 15)_{-17}^{+28}$	24	<b>38</b>	579	1231
Spectra  Ew Structure PF ew FFs Diff. RQMs PF vs. IF	$N(1650)$	$(109 \pm 26)_{-3}^{+36}$	6.3	10.5	158	327
	$N(1675)$	$(68 \pm 8)_{-4}^{+14}$	9.1	9.9	15	15
Decays pi, eta, K	$N(1700)$	$(10 \pm 5)_{-3}^{+3}$	1.1	1.3	2.9	2.9
	$N(1710)$	$(15 \pm 5)_{-5}^{+30}$	<b>15</b>	<u>12</u>	6.0	3.2
Multiplets PDG Systematics QM Classif. Wave Functions Decays	$\Delta(1232)$	$(119 \pm 1)_{-5}^{+5}$	33	31	81	85
	$\Delta(1600)$	$(61 \pm 26)_{-10}^{+26}$	0.2	<u>2.4</u>	56	31
	$\Delta(1620)$	$(38 \pm 8)_{-6}^{+8}$	1.4	2.8	74	176
	$\Delta(1700)$	$(45 \pm 15)_{-10}^{+20}$	4.6	5.4	14	14

With experimental masses

T. Melde, W. Plessas, and R.F. Wagenbrunn: Phys. Rev. C **72**, 015207 (2005); *ibid.* **74**, 069901 (2006)

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$\Lambda^*$ $\rightarrow \Sigma\pi$	Experiment [MeV]	Relativistic		Nonrel. EEM	
		GBE	OGE	GBE	OGE
$\Lambda(1405)$	$(50 \pm 2)$	55	78	320	611
$\Lambda(1520)$	$(6.55 \pm 0.16)^{+0.04}_{-0.04}$	5	9	5	8
$\Lambda(1600)$	$(53 \pm 38)^{+60}_{-10}$	3	<b>33</b>	2	34
$\Lambda(1670)$	$(14.0 \pm 5.3)^{+8.3}_{-2.5}$	69	103	620	1272
$\Lambda(1690)$	$(18 \pm 6)^{+4}_{-2}$	<b>19</b>	<b>25</b>	24	28
$\Lambda(1800)$	<i>seen</i>	68	101	473	1175
$\Lambda(1810)$	$(38 \pm 23)^{+40}_{-10}$	3.8	2.1	55	150
$\Lambda(1830)$	$(52 \pm 19)^{+11}_{-12}$	14	19	16	24

With theoretical masses

T. Melde, W. Plessas, and B. Sengl: Phys. Rev. C 76, 025204 (2007)



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$N \rightarrow N\eta$	Experiment [MeV]	Relativistic		Nonrel. EEM	
		GBE	OGE	GBE	OGE
$N(1520)$	$(0.28 \pm 0.05)_{-0.01}^{+0.03}$	0.1	0.1	0.04	0.04
$N(1535)$	$(64 \pm 19)_{-28}^{+28}$	27	35	127	236
$N(1650)$	$(10 \pm 5)_{-1}^{+4}$	50	74	283	623
$N(1675)$	$(0 \pm 1.5)_{-0.1}^{+0.3}$	1.5	2.4	1.1	1.8
$N(1700)$	$(0 \pm 1)_{-0.5}^{+0.5}$	0.5	0.9	0.2	0.3
$N(1710)$	$(6 \pm 1)_{-4}^{+11}$	0.02	0.06	2.9	9.3

With theoretical masses

T. Melde, W. Plessas, and R.F. Wagenbrunn: Phys. Rev. C **72**, 015207 (2005); *ibid.* **74**, 069901 (2006)

# K Decay Widths of $\Lambda^*$ and $\Sigma^*$

	$\Lambda^*, \Sigma^*$ $\rightarrow NK$	Experiment [MeV]	Relativistic		Nonrel. EEM	
			GBE	OGE	GBE	OGE
RQM & CQM	$\Lambda(1520)$	$(7.02 \pm 0.16)_{-0.44}^{+0.46}$	12	24	23	63
GBE CQM OGE CQM	$\Lambda(1600)$	$(33.75 \pm 11.25)_{-15}^{+30}$	15	35	4.1	23
II CQM	$\Lambda(1670)$	$(8.75 \pm 1.75)_{-2}^{+4.5}$	0.3	$\approx 0$	45	86
Spectra	$\Lambda(1690)$	$(15 \pm 3)_{-2}^{+3}$	1.2	1.0	4.2	6.5
Ew Structure	$\Lambda(1800)$	$(97.5 \pm 22.5)_{-25}^{+40}$	4.2	6.4	3.1	8.6
PF ew FFs Diff. RQMs PF vs. IF	$\Lambda(1810)$	$(52.5 \pm 22.5)_{-20}^{+50}$	4.1	12	23	44
Decays pi, eta, K	$\Lambda(1830)$	$(6.18 \pm 3.33)_{-1.05}^{+1.05}$	0.1	0.9	0.1	0.1
Multiplets	$\Sigma(1660)$	$(20 \pm 10)_{-6}^{+30}$	0.9	0.9	0.4	$\approx 0$
PDG Systematics	$\Sigma(1670)$	$(6.0 \pm 1.8)_{-1.4}^{+2.6}$	1.1	1.0	1.9	2.0
QM Classif. Wave Functions	$\Sigma(1750)$	$(22.5 \pm 13.5)_{-3}^{+28}$	$\approx 0$	1.4	10	48
Decays	$\Sigma(1775)$	$(48.0 \pm 3.6)_{-5.6}^{+6.5}$	11	15	20	41
Summary	$\Sigma(1940)$	$(22 \pm 22)_{-16}^{+16}$	1.1	1.5	3.3	6.8

With theoretical masses

## Classification of baryon resonances by the PDG (2008)

multiplet	$(LS)J^P$					
octet	$(0 \frac{1}{2}) \frac{1}{2}^+$	$N(939)$	$\Lambda(1116)$	$\Sigma(1193)$	$\Xi(1318)$	
octet	$(0 \frac{1}{2}) \frac{1}{2}^+$	$N(1440)$	$\Lambda(1600)$	$\Sigma(1660)$	$\Xi(?)$	
octet	$(0 \frac{1}{2}) \frac{1}{2}^+$	$N(1710)$	$\Lambda(1810)$	$\Sigma(1880)$	$\Xi(?)$	
octet	$(1 \frac{1}{2}) \frac{1}{2}^-$	$N(1535)$	$\Lambda(1670)$	$\Sigma(1620)$	$\Xi(?)$	
octet	$(1 \frac{1}{2}) \frac{1}{2}^-$	$N(1650)$	$\Lambda(1800)$	$\Sigma(1750)$	$\Xi(?)$	
octet	$(1 \frac{1}{2}) \frac{1}{2}^-$	$N(1520)$	$\Lambda(1690)$	$\Sigma(1670)$	$\Xi(1820)$	
octet	$(1 \frac{1}{2}) \frac{1}{2}^-$	$N(1700)$	$\Lambda(?)$	$\Sigma(?)$	$\Xi(?)$	
octet	$(1 \frac{1}{2}) \frac{1}{2}^-$	$N(1675)$	$\Lambda(1830)$	$\Sigma(1775)$	$\Xi(?)$	
decuplet	$(0 \frac{3}{2}) \frac{3}{2}^+$	$\Delta(1232)$	-	$\Sigma(1385)$	$\Xi(1530)$	
decuplet	$(0 \frac{3}{2}) \frac{3}{2}^+$	$\Delta(1600)$	-	$\Sigma(?)$	$\Xi(?)$	
decuplet	$(1 \frac{1}{2}) \frac{1}{2}^-$	$\Delta(1620)$	-	$\Sigma(?)$	$\Xi(?)$	
decuplet	$(1 \frac{1}{2}) \frac{1}{2}^-$	$\Delta(1700)$	-	$\Sigma(?)$	$\Xi(?)$	
singlet	$(1 \frac{1}{2}) \frac{1}{2}^-$	-	$\Lambda(1405)$	-	-	
singlet	$(1 \frac{1}{2}) \frac{1}{2}^-$	-	$\Lambda(1520)$	-	-	

## RQM & CQMs

GBE CQM  
 OGE CQM  
 II CQM

## Spectra

## EW Structure

PF ew FFs  
 Diff. RQMs  
 PF vs. IF

## Decays

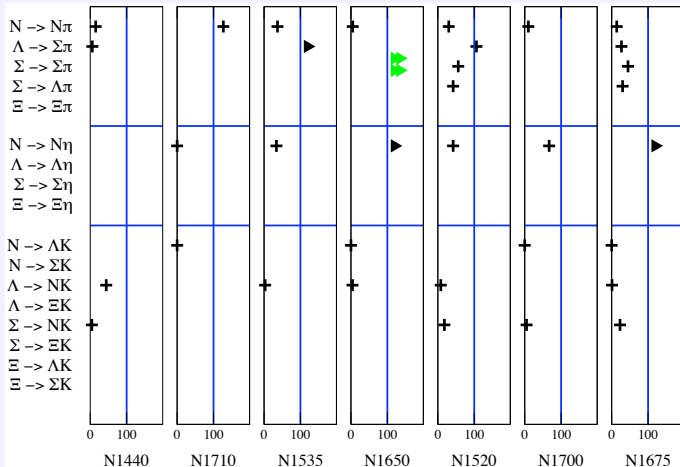
$\pi$ ,  $\eta$ , K

## Multiplets

PDG

Systematics  
 QM Classif.  
 Wave Functions  
 Decays

## Summary



## RQM & CQMs

GBE CQM  
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 PF vs. IF

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$\pi$ ,  $\eta$ , K

## Multiplets

PDG

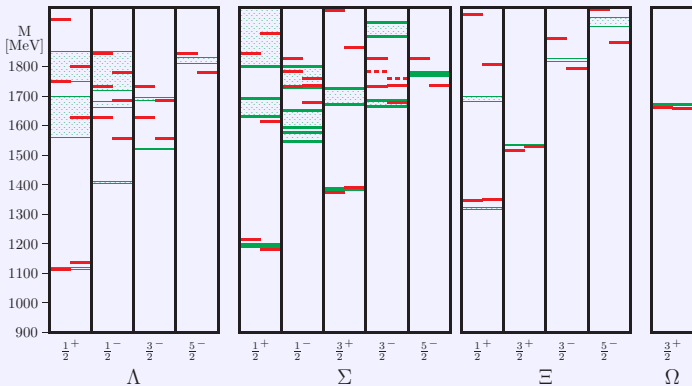
Systematics

QM Classif.

Wave Functions

Decays

## Summary



For  $\Sigma$  with  $J^P = \frac{1}{2}^-$  we have  $\Sigma[1560]$ ,  $\Sigma[1620]$ , and  $\Sigma(1750)$

For  $\Sigma$  with  $J^P = \frac{3}{2}^-$  we have  $\Sigma(1670)$ ,  $\Sigma[1940]$ , and a third  $\Sigma\{\approx 1770\}$  not yet seen (dashed)

- ▶ Consider **spectral** and **decay** data
- ▶ Sort results according to **flavor multiplets**
- ▶ Examine the **spin**, **flavor**, and **space** symmetries of the various states

For the latter consider:

**Spatial probability density distribution**

$$\rho(\xi, \eta) = \xi^2 \eta^2 \int d\Omega_\xi d\Omega_\eta$$

$$\Psi_{M_\Sigma M_\Sigma T M_T}^*(\xi, \Omega_\xi, \eta, \Omega_\eta) \Psi_{M_\Sigma M_\Sigma T M_T}(\xi, \Omega_\xi, \eta, \Omega_\eta)$$

where  $\vec{\xi}$  and  $\vec{\eta}$  are the usual Jacobi coordinates

## RQM & CQMs

- GBE CQM
- OGE CQM
- II CQM

## Spectra

## EW Structure

- PF ew FFs
- Diff. RQMs
- PF vs. IF

## Decays

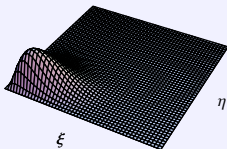
- $\pi$ ,  $\eta$ ,  $K$

## Multiplets

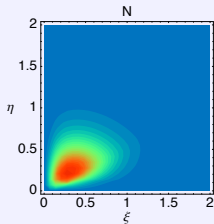
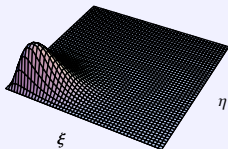
- PDG
- Systematics
- QM Classif.
- Wave Functions
- Decays

## Summary

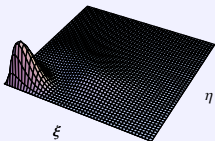
N GBE CQM



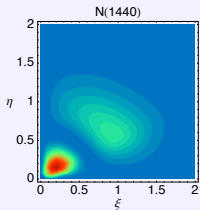
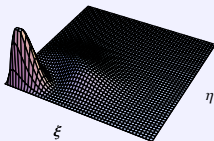
N OGE CQM



N(1440) GBE CQM



N(1440) OGE CQM



RQM & CQMs

GBE CQM

OGE CQM

II CQM

Spectra

EW Structure

PF ew FFs

Diff. RQMs

PF vs. IF

Decays

$\pi$ ,  $\eta$ ,  $K$

Multiplets

PDG

Systematics

QM Classif.

Wave Functions

Decays

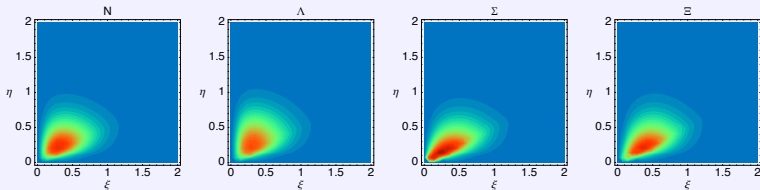
Summary

multiplet	$(LS)J^P$					
octet	$(0\frac{1}{2})\frac{1}{2}^+$	$N(939)^{100}$	$\Lambda(1116)^{100}$	$\Sigma(1193)^{100}$	$\Xi(1318)^{100}$	
octet	$(0\frac{1}{2})\frac{3}{2}^+$	$N(1440)^{100}$	$\Lambda(1600)^{96}$	$\Sigma(1660)^{100}$	$\Xi(1690)^{100}$	
octet	$(0\frac{1}{2})\frac{3}{2}^+$	$N(1710)^{100}$		$\Sigma(1880)^{99}$		
octet	$(1\frac{1}{2})\frac{1}{2}^-$	$N(1535)^{100}$	$\Lambda(1670)^{72}$	$\Sigma(1560)^{94}$		
octet	$(1\frac{1}{2})\frac{3}{2}^-$	$N(1650)^{100}$	$\Lambda(1800)^{100}$	$\Sigma(1620)^{100}$		
octet	$(1\frac{1}{2})\frac{3}{2}^-$	$N(1520)^{100}$	$\Lambda(1690)^{72}$	$\Sigma(1670)^{94}$	$\Xi(1820)^{97}$	
octet	$(1\frac{1}{2})\frac{3}{2}^-$	$N(1700)^{100}$		$\Sigma(1940)^{100}$		
octet	$(1\frac{1}{2})\frac{3}{2}^-$	$N(1675)^{100}$	$\Lambda(1830)^{100}$	$\Sigma(1775)^{100}$	$\Xi(1950)^{100}$	
decuplet	$(0\frac{3}{2})\frac{3}{2}^+$	$\Delta(1232)^{100}$	$\Sigma(1385)^{100}$	$\Xi(1530)^{100}$	$\Omega(1672)^{100}$	
decuplet	$(0\frac{3}{2})\frac{3}{2}^+$	$\Delta(1600)^{100}$	$\Sigma(1690)^{99}$			
decuplet	$(1\frac{1}{2})\frac{1}{2}^-$	$\Delta(1620)^{100}$	$\Sigma(1750)^{94}$			
decuplet	$(1\frac{1}{2})\frac{3}{2}^-$	$\Delta(1700)^{100}$				
singlet	$(1\frac{1}{2})\frac{1}{2}^-$	$\Lambda(1405)^{71}$				
singlet	$(1\frac{1}{2})\frac{3}{2}^-$	$\Lambda(1520)^{71}$				
singlet	$(0\frac{1}{2})\frac{1}{2}^+$	$\Lambda(1810)^{92}$				

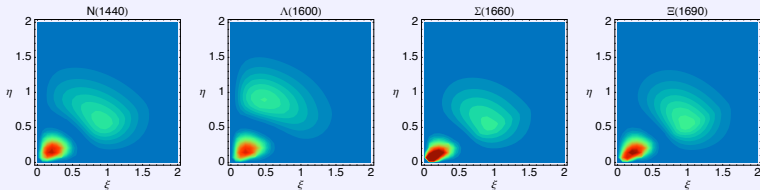
T. Melde, W. Plessas, and B. Sengl: Phys. Rev. D, to appear



$\rho(\xi, \eta)$  for the  $\frac{1}{2}^+$  octet baryon ground states  $N(939)$ ,  $\Lambda(1116)$ ,  $\Sigma(1193)$ ,  $\Xi(1318)$ :



$\rho(\xi, \eta)$  for the  $\frac{1}{2}^+$  octet baryon states  $N(1440)$ ,  $\Lambda(1600)$ ,  $\Sigma(1660)$ ,  $\Xi(1690)$ :



RQM & CQMs

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 OGE CQM  
 II CQM

Spectra

EW Structure

PF w/ FFs  
 Diff. RQMs  
 PF vs. IF

Decays

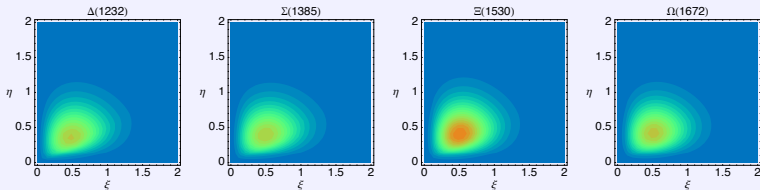
$\pi$ ,  $\eta$ ,  $K$

Multiplets

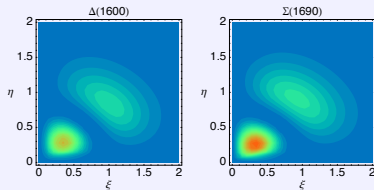
PDG  
 Systematics  
 QM Classif.  
 Wave Functions  
 Decays

Summary

$\rho(\xi, \eta)$  for the  $\frac{3}{2}^+$  decuplet baryon states  $\Delta(1232)$ ,  $\Sigma(1385)$ ,  $\Xi(1530)$ ,  $\Omega(1672)$ :



$\rho(\xi, \eta)$  for the  $\frac{3}{2}^+$  decuplet baryon states  $\Delta(1600)$ ,  $\Sigma(1690)$ :



RQM & CQMs

GBE CQM  
 OGE CQM  
 II CQM

Spectra

EW Structure

PF ew FFs  
 Diff. RQMs  
 PF vs. IF

Decays

$\pi$ ,  $\eta$ ,  $K$

Multiplets

PDG  
 Systematics  
 QM Classif.

Wave Functions  
 Decays

Summary

## RQM & CQMs

GBE CQM  
 OGE CQM  
 II CQM

## Spectra

## EW Structure

PF ew FFs  
 Diff. RQMs  
 PF vs. IF

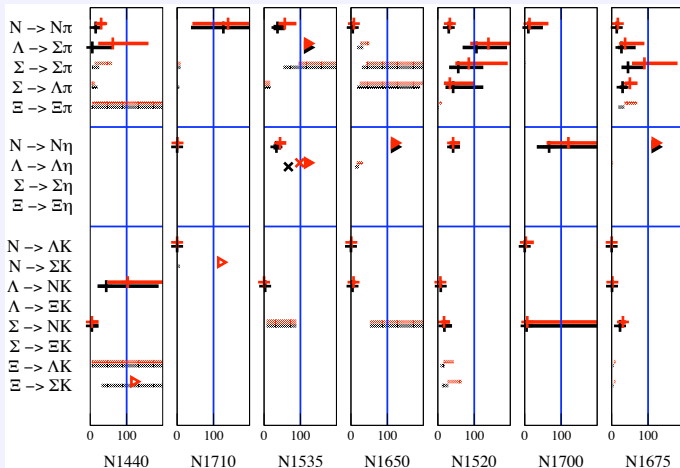
## Decays

$\pi$ ,  $\eta$ , K

## Multiplets

PDG  
 Systematics  
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 Decays

## Summary



## RQM & CQMs

GBE CQM  
 OGE CQM  
 II CQM

## Spectra

## Ew Structure

PF ew FFs  
 Diff. RCQMs  
 PF vs. IF

## Decays

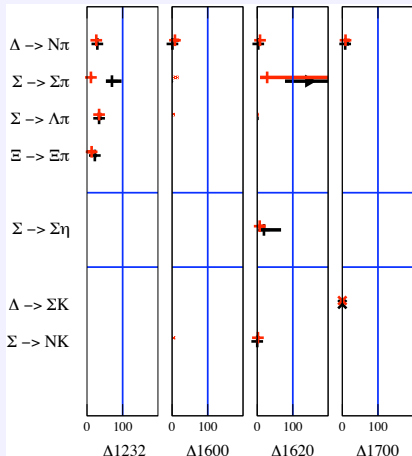
$\pi$ ,  $\eta$ , K

## Multiplets

PDG  
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## Decays

## Summary



T. Melde, W. Plessas, and B. Sengl: Phys. Rev. D, to appear

## RQM & CQMs

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 II CQM

## Spectra

## Ew Structure

PF ew FFs  
 Diff. RQMs  
 PF vs. IF

## Decays

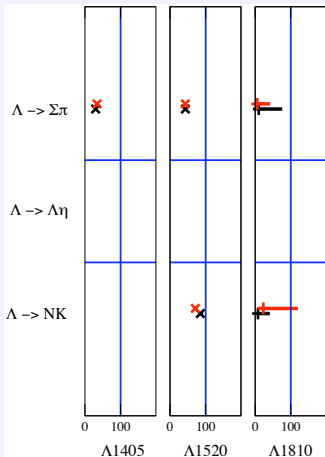
$\pi$ ,  $\eta$ , K

## Multiplets

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## Summary



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- ▶ **Relativistic CQMs** allow for a unified description of light and strange baryon spectra for  $E \lesssim 2$  GeV, especially in the case of the **GBE CQM**
  - ▶ mass-operator eigenvalues in relatively good order
- ▶ **Covariant point-form** predictions for the elastic electroweak nucleon structure in surprisingly good agreement with available data for  $q^2 \lesssim 4$  GeV<sup>2</sup> (in contrast to the **instant-form spectator-model** results)
  - ▶ ground-state wave functions appear reasonable
- ▶ **Strong decays** cannot yet be described in agreement with phenomenology
  - ▶ refinements necessary, both with respect to **resonance wave functions** and **decay mechanism**.

- ▶ **Spectra, decay widths, and spin-flavor-space** symmetries of states allow for a new (extended) **classification of baryon resonances** into flavor multiplets
  - ▶ to be confirmed by more experiments

Thank you very much

for

your attention!

RQM & CQMs

GBE CQM  
OGE CQM  
II CQM

Spectra

Ew Structure

PF ew FFs  
Diff. RQMs  
PF vs. IF

Decays

$\pi$ ,  $\eta$ ,  $K$

Multiplets

PDG  
Systematics  
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Decays

Summary

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RQM & CQMs

GBE CQM  
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