

# Nucleon form factors experiments with 12 GeV CEBAF

Nucleon FFs in 12 GeV era and  
Large Acceptance Large Luminosity  
Spectrometer for Hall A TJNAF

Bogdan Wojtsekhowski, Jefferson Lab

# Outline of the talk

- ❖ status of FFs, connection FFs and GPDs, and calculation of the transverse densities
- ❖ 12 GeV program: GMP-18, GEP-15, GMN-17, and GEN-7.5 GeV<sup>2</sup>
- ❖ New spectrometer concept and applications
- ❖ Road map of construction

# Highlights of electromagnetic FFs

- Direct observation of the nucleon structure: Hofstadter 1950th
- Rosenbluth: L/T separation in 1950, Akhiezer:  $A_{LT}$  in 1957
- SLAC measurement of  $G_M^p$  up to  $30 \text{ GeV}^2$
- pQCD dimensional scaling:  $F_1 \sim 1/t^2$  and  $F_2/F_1 \sim 1/t$
- Polarized electron beam era: Sinclair's electron source in 1977
- CEBAF with polarimeter and polarized targets in 1990th
- Unification of DIS/FF/DVCS in GPDs by Muller, Ji, Radyushkin
- $G_E^p/G_M^p$  vs  $Q^2$  dependence, discovery by Perdrisat et al
- $G_M^n/G_M^p$  precision measurement by Brooks et al
- $G_E^n/G_M^n$  measurements at NIKHEF, Mainz, JLab, BATES
- Transverse densities by Burkardt, Diehl@C, Miller, Boffi&Pasquini ..

## Perspectives of the field in 12 GeV era

# Electro-Magnetic Form Factors

One-photon approximation,  $\alpha_{em} = 1/137$ , hadron current

$$\mathcal{J}_{hadronic}^\mu = ie\bar{N}(p') \left[ \gamma^\mu F_1(Q^2) + \frac{i\sigma^{\mu\nu}q_\nu}{2M} F_2(Q^2) \right] N(p) \quad \text{Rosenbluth (1950)}$$

Full expression for  $\mathcal{M}$  has three complex functions,  $F_1, F_2, F_3$  Guichon & Vanderhaeghen

$$\mathcal{M} = \frac{4\pi\alpha}{Q^2} \bar{u}' \gamma_\mu u \cdot \bar{N}' \left( \tilde{F}_1 \gamma^\mu - \tilde{F}_2 [\gamma^\mu, \gamma^\nu] \frac{q_\nu}{4M} + \tilde{F}_3 K_\nu \gamma^\nu \frac{P^\mu}{M^2} \right) N \quad \text{Afanasev et al.}$$

$$\tilde{G}_M = \tilde{F}_1 + \tilde{F}_2 \quad \tilde{G}_E = \tilde{F}_1 - \tau \tilde{F}_2$$

$\tilde{F}_i$  are functions of  $(s - u)$  and  $t$

Blunden et al.

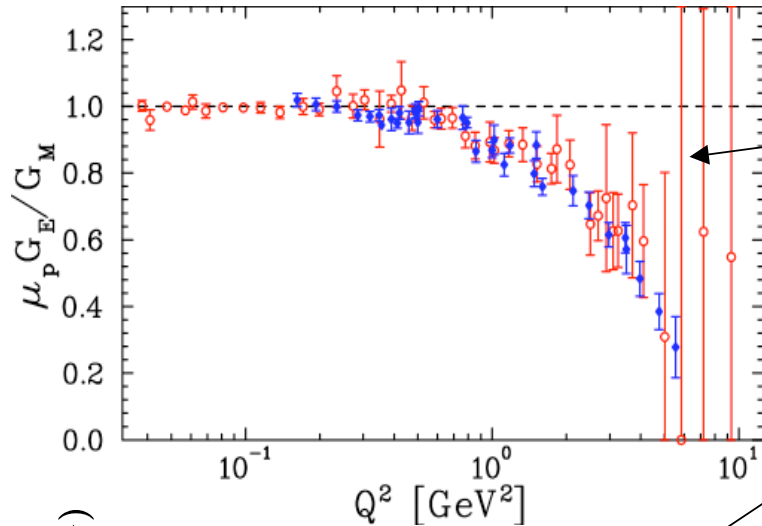
$$d\sigma = d\sigma_{NS} \left\{ \varepsilon (\tilde{G}_E + \frac{s-u}{4M^2} \tilde{F}_3)^2 + \tau (\tilde{G}_M + \varepsilon \frac{s-u}{4M^2} \tilde{F}_3)^2 \right\}$$

old  $G_{E,M}$  are real functions of  $t=-Q^2$

$$\sigma_R = \varepsilon G_E^2 + \tau G_M^2 + 2\tau G_M \operatorname{Re} \left( \delta \tilde{G}_M + \varepsilon \frac{s-u}{M^2} \tilde{F}_3 \right) + 2\varepsilon G_E \operatorname{Re} \left( \delta \tilde{G}_E + \frac{s-u}{M^2} \tilde{F}_3 \right)$$

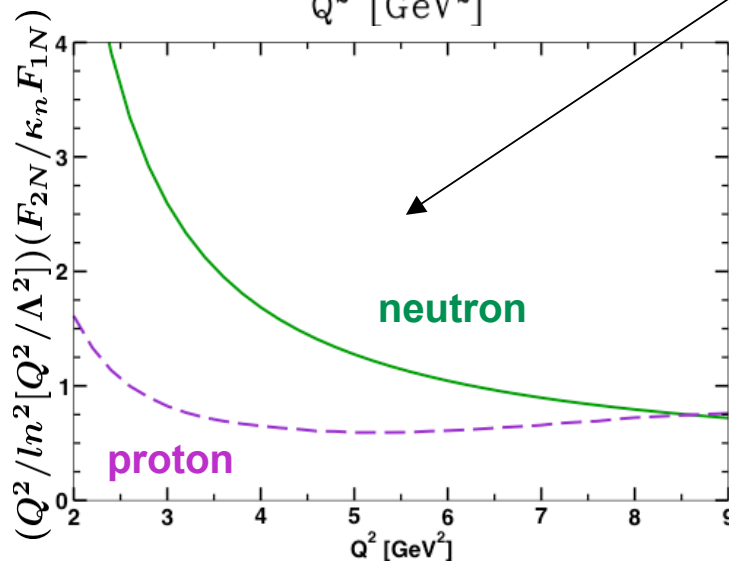
Extra terms contribute less than few % to  $\sigma_R$

# Recent development



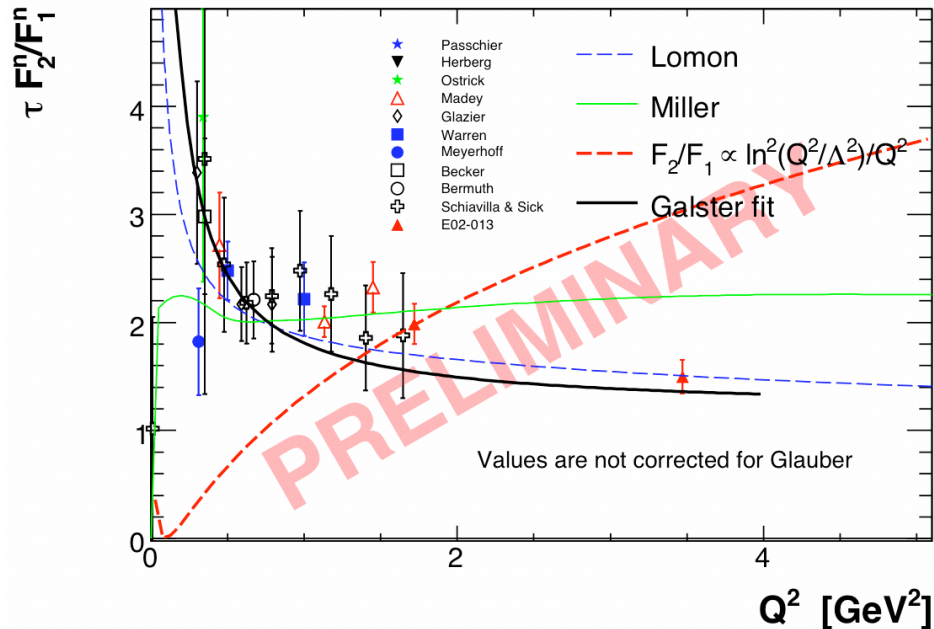
- Rosenbluth analysis with  $2-\gamma$  terms  
Arrington etal, nucl-ex:0707.1861  
E.Tomasi-Gustafsson etal,  
PRC 75 (2007)

- FFs from DSE approach in QCD  
C.Roberts, arXiv:0712.0633



- Confirmation of GEP at  $Q^2 \sim 4 \text{ GeV}^2$   
with Focal Plane Polarimeter in HMS  
**Perdrisat etal, [ GEP-III ]**
- Constrain on  $2-\gamma$  terms with  $\varepsilon$  scan  
at fixed  $Q^2 = 2.5 \text{ GeV}^2$  with FPP in HMS  
It was reported today by **L.Pentchev**

# Last month news

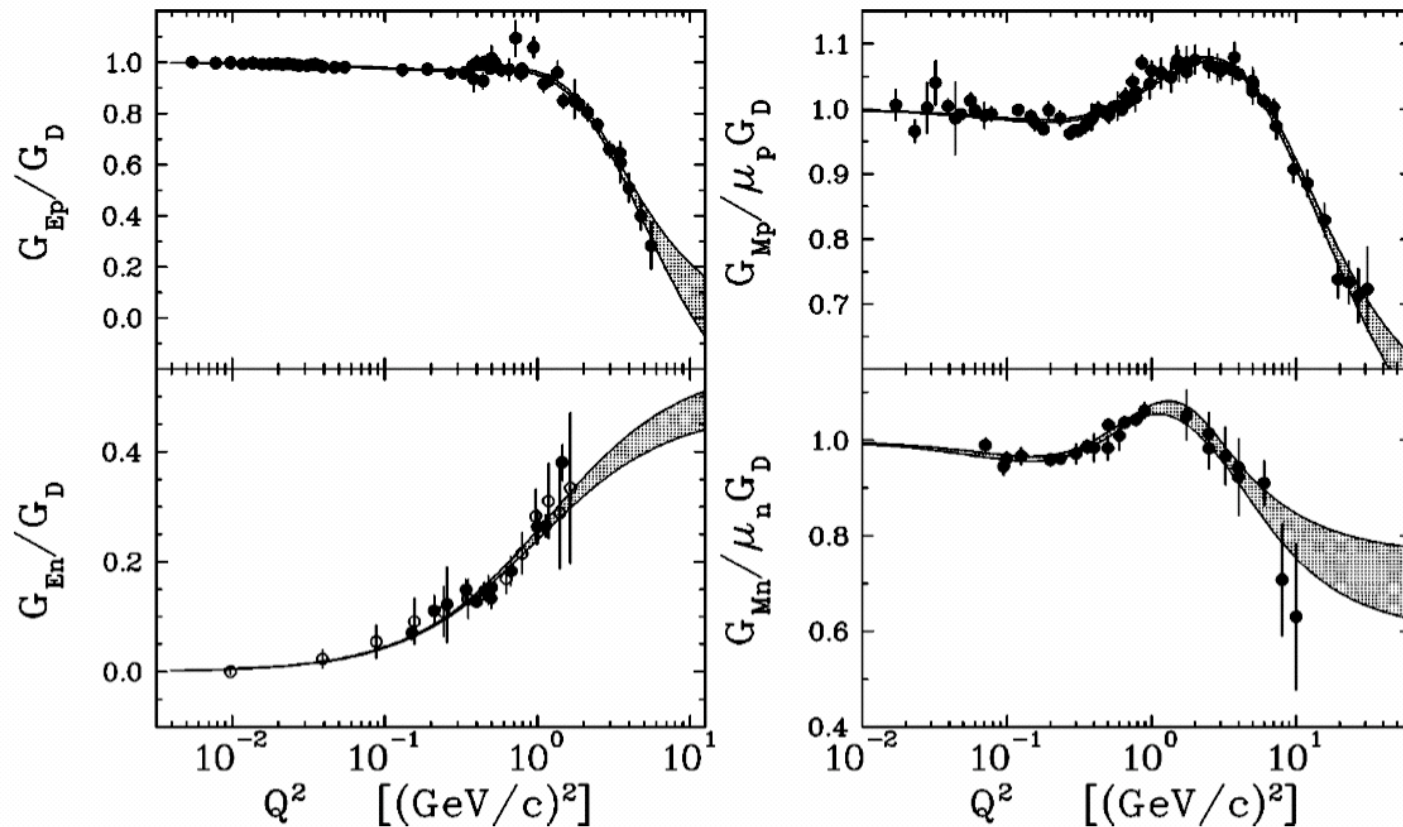


- Preliminary result from JLab He-3(e,e'n) experiment for GEN/GMN at 1.7 and 3.5 GeV<sup>2</sup>.  
more will be in June  
“Neutron FFs”, Elba-X

- GEP-III is taking data for GEP/GMP at 8.5 GeV<sup>2</sup>.  
E.Brash report in Trento

# Kelly's parameterization

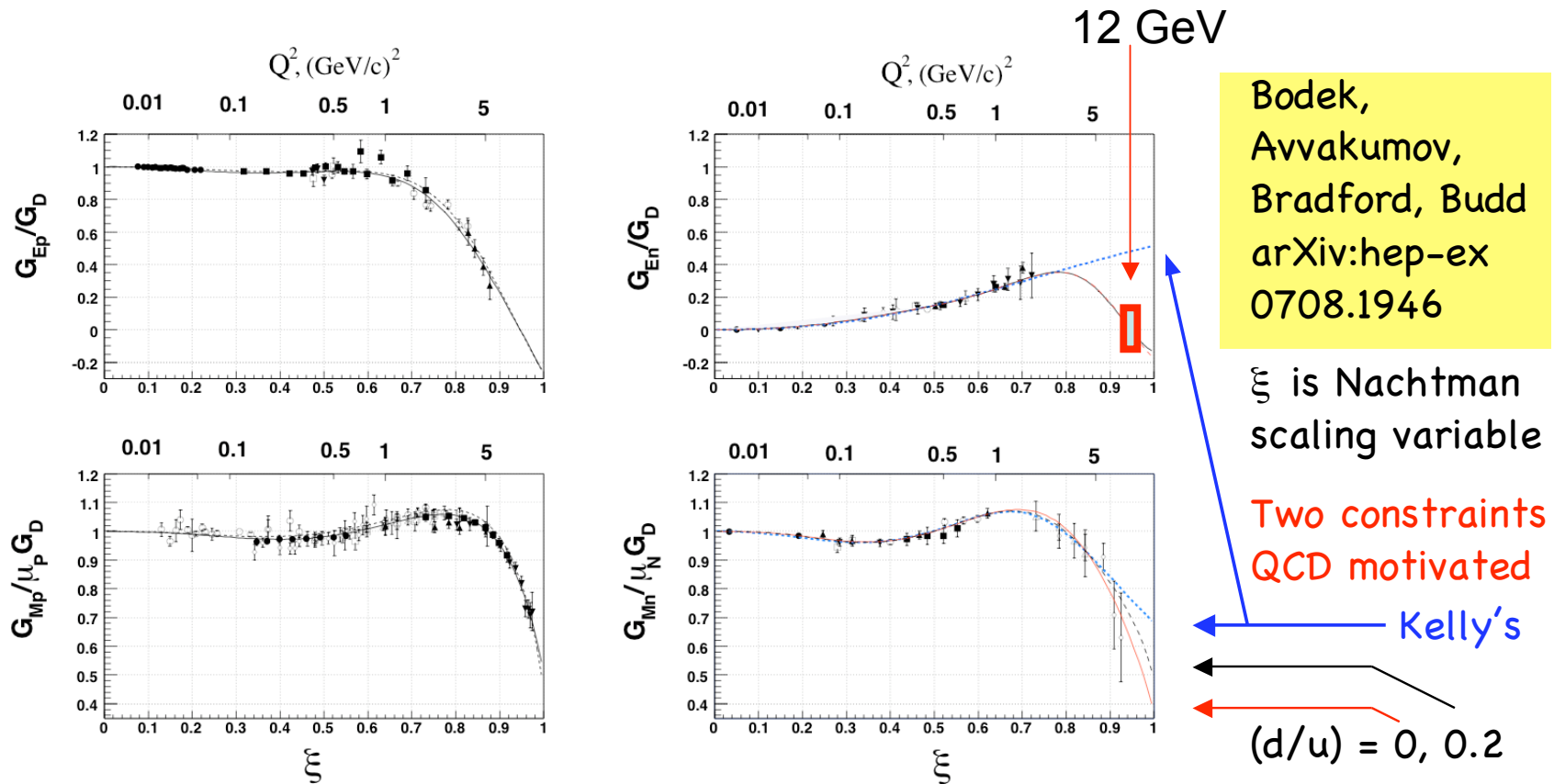
J. Kelly,  
PRC 70,  
068202  
(2004)



$$G(Q^2) = \sum_{k=0}^{n=1} a_k \tau^k / (1 + \sum_{k=1}^{n+2=3} b_k \tau^k)$$

scaling constraint:  $Q \rightarrow \infty, G \sim Q^{-4}$

# New parameterization



$$\xi^{p,n} = 2/(1 + \sqrt{1 + \tau_{p,n}^{-1}})$$

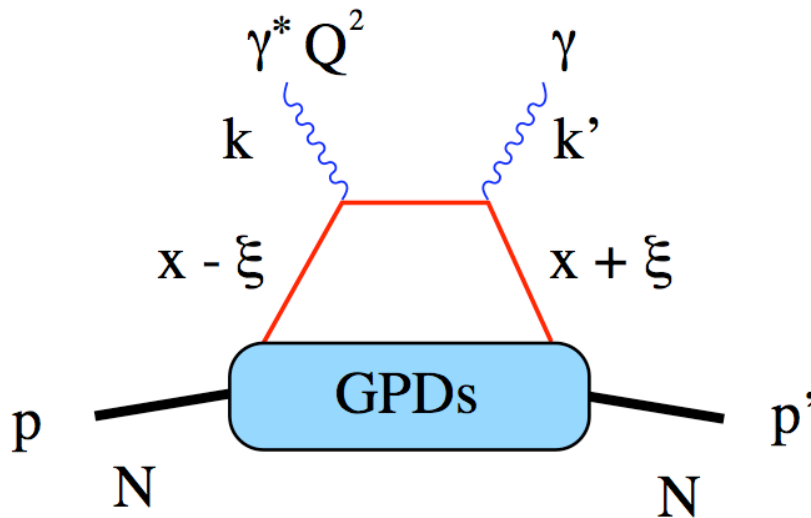
$$G_{BABB} = A(\xi) \times G_{Kelly}(Q^2)$$

constrains: at  $\xi \rightarrow 1$

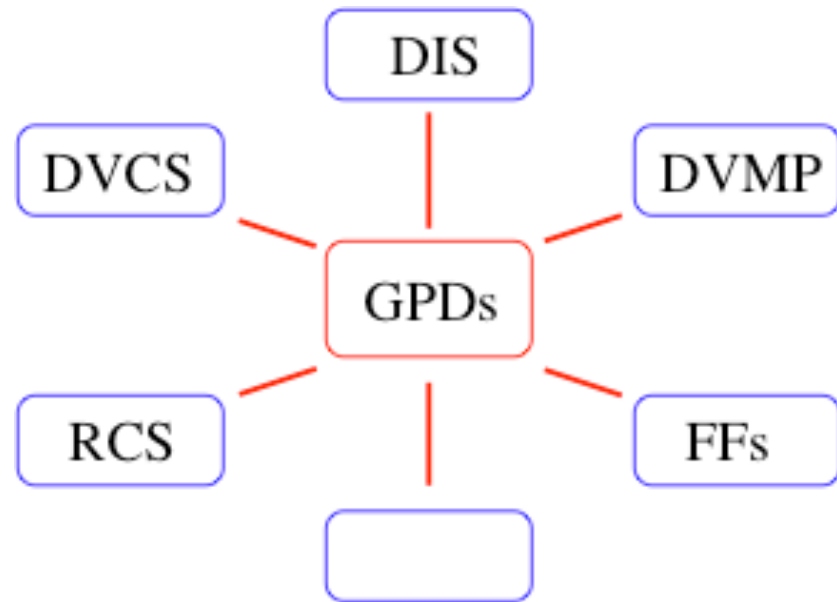
$$1) \frac{G_{Mn}^2}{G_{Mp}^2} = \frac{1+4(d/u)}{4+(d/u)} \quad 2) \frac{G_{En}^2}{G_{Mn}^2} = \frac{G_{Ep}^2}{G_{Mp}^2}$$

# GPDs of nucleon

Müller (94), Ji (97), Radyushkin (97)



where  $\xi = (p_q^+ - p_q'^+)/ (p_q^+ + p_q'^+)$



Quark dynamics of nucleon encoded in GPD functions

$H(x, \xi, t)$ ,  $\tilde{H}(x, \xi, t)$  hadron helicity-conserving; vector and axial-vector

$E(x, \xi, t)$ , and  $\tilde{E}(x, \xi, t)$  helicity-flipping; tensor and pseudo-scalar

# GPDs information

Reduction formulas at  $\xi = t = 0$   
for DIS and  $\xi = 0$  for FFs

$$H^q(x, \xi = 0, t = 0) = q(x)$$

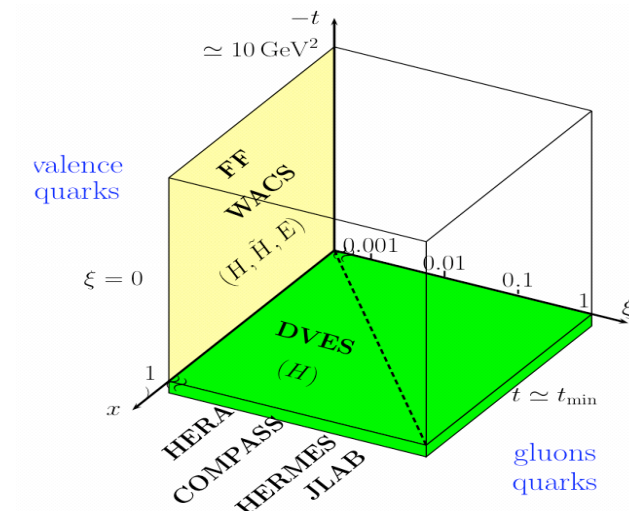
$$\tilde{H}^q(x, \xi = 0, t = 0) = \Delta q(x)$$

$$\int_{-1}^{+1} dx H^q(x, 0, Q^2) = F_1^q(Q^2)$$

$$\int_{-1}^{+1} dx E^q(x, 0, Q^2) = F_2^q(Q^2)$$

P.Kroll, Excl.-07

a lot to  
measure



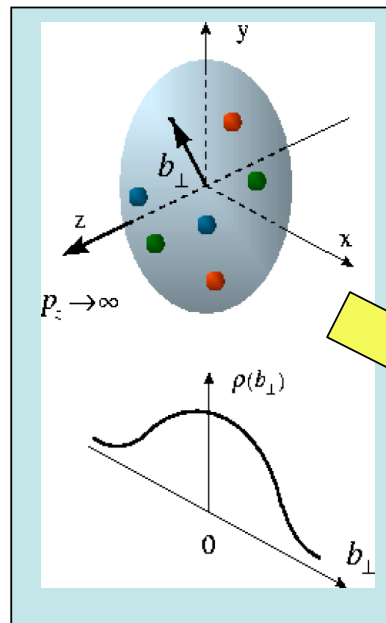
Ji's sum rule for quark orbital momentum

$$\langle L_v^q \rangle = \frac{1}{2} \int_0^1 dx [x E_v^q(x, \xi = 0, t = 0) + x q_v(x) - \Delta q_v(x)]$$

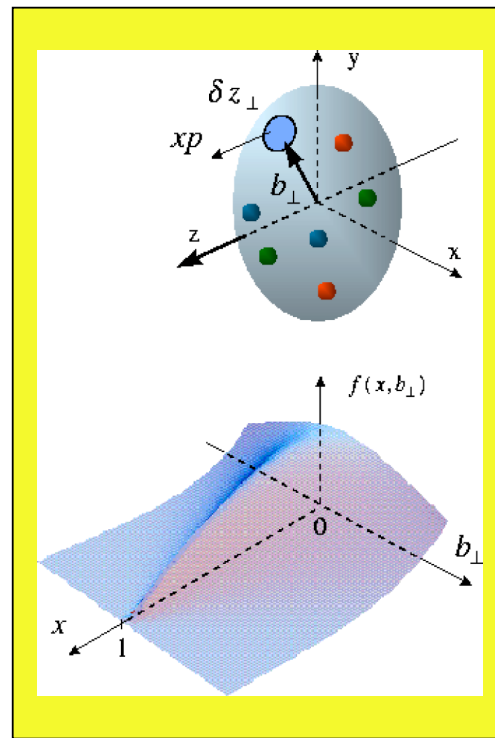
DVCS will access low  $t$ , large  $Q^2$  kinematics

FFs presently are the main source for  $E_v^q$

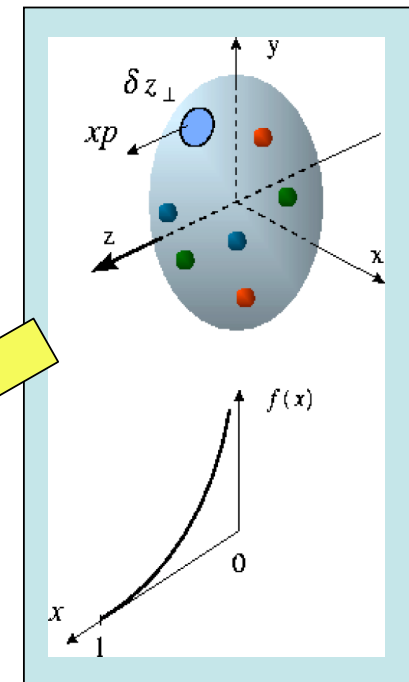
# 3-d picture of the nucleon



Proton form factors,  
transverse charge &  
current densities



Correlated quark momentum  
and helicity distributions in  
transverse space - GPDs



Structure functions,  
quark longitudinal  
momentum & helicity  
distributions

# Impact parameter and densities

$$F_1(t) = \sum_q e_q \int dx H_q(x, t)$$

Muller, Ji, Radyushkin

$$q(x, \mathbf{b}) = \int \frac{d^2 q}{(2\pi)^2} e^{i \mathbf{q} \cdot \mathbf{b}} H_q(x, t = -q^2)$$

M.Burkardt

$$\rho(b) \equiv \sum_q e_q \int dx q(x, \mathbf{b}) = \int d^2 q F_1(q^2) e^{i \mathbf{q} \cdot \mathbf{b}}$$

P.Kroll: u/d segregation

$$\rho(b) = \int_0^\infty \frac{Q \cdot dQ}{2\pi} J_0(Qb) \frac{G_E(Q^2) + \tau G_M(Q^2)}{1 + \tau}$$

G.Miller

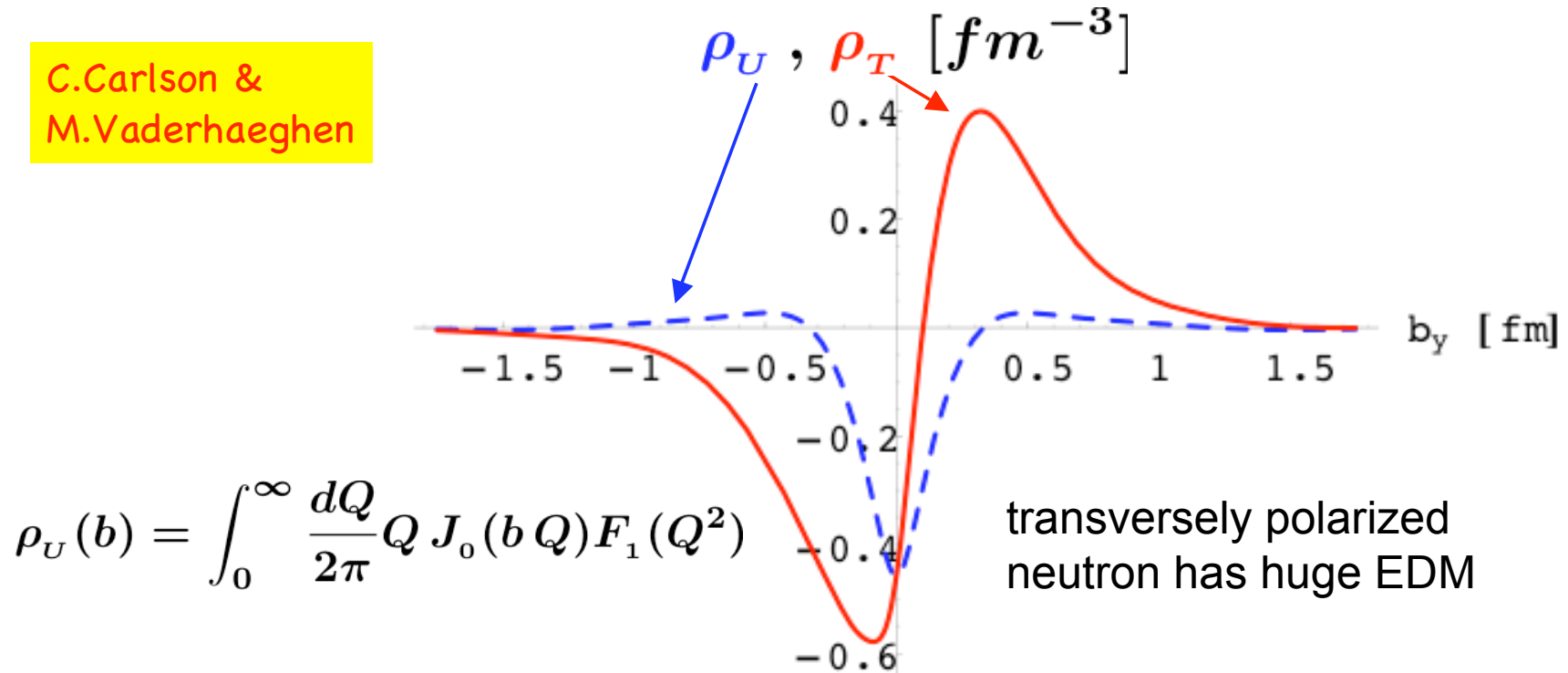
center of momentum  $\mathbf{R}_\perp = \sum_i \mathbf{x}_i \cdot \mathbf{r}_{\perp, i}$

$\mathbf{b}$  is defined relative to  $\mathbf{R}_\perp$

# Transverse densities

$$\rho_T(\vec{b}) = \rho_U(b) - \sin(\phi_b - \phi_S) \int_0^\infty \frac{dQ}{2\pi} \frac{Q^2}{2M} J_1(bQ) F_2(Q^2)$$

C. Carlson &  
M. Vanderhaeghen

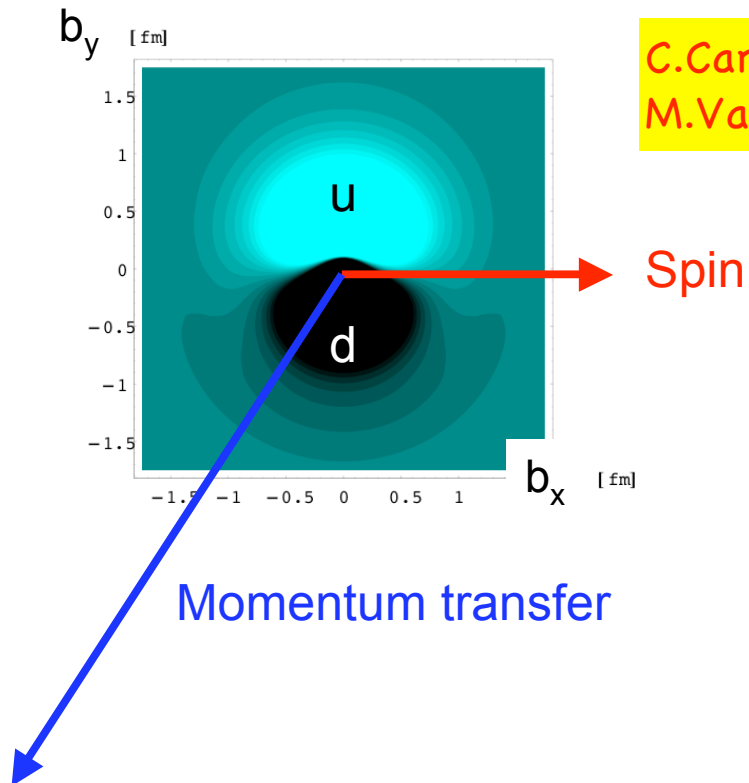


# Density in polarized neutron

Transversity effects in

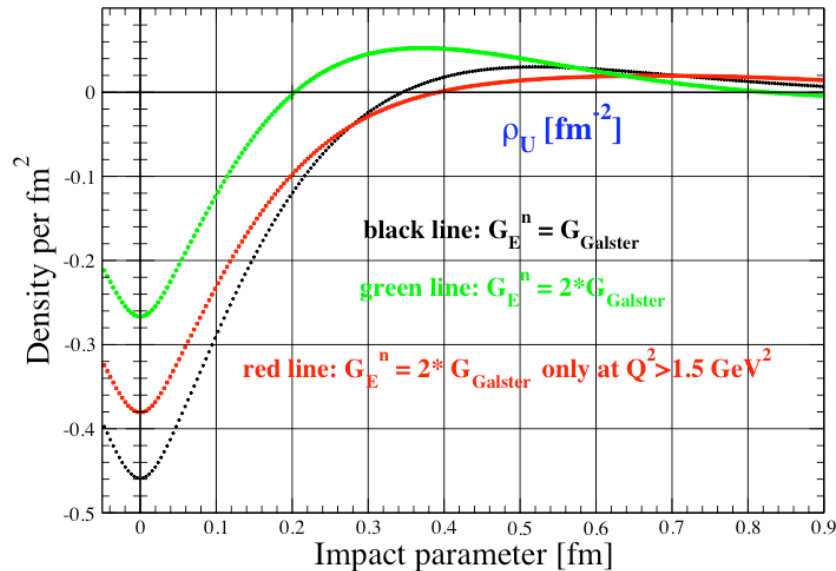
$$\vec{n}(e, e' \pi^-) X$$

$$\vec{n}(e, e' \pi^+) X$$

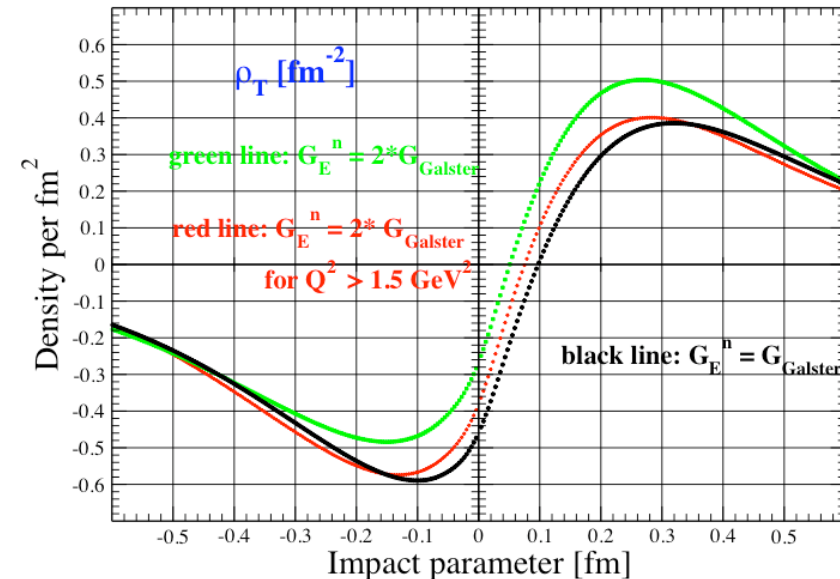


# Effect of GEN

Neutron transverse charge density



Neutron transverse charge density



- Negative density at low  $b$  in a neutron => d quarks dominate
- High  $Q^2$  elastic process in Feynman mechanism requires a large  $x$  quark, so d quarks dominate at large  $x$ , in agreement with DIS

# CEBAF electron beam in 2013(4)

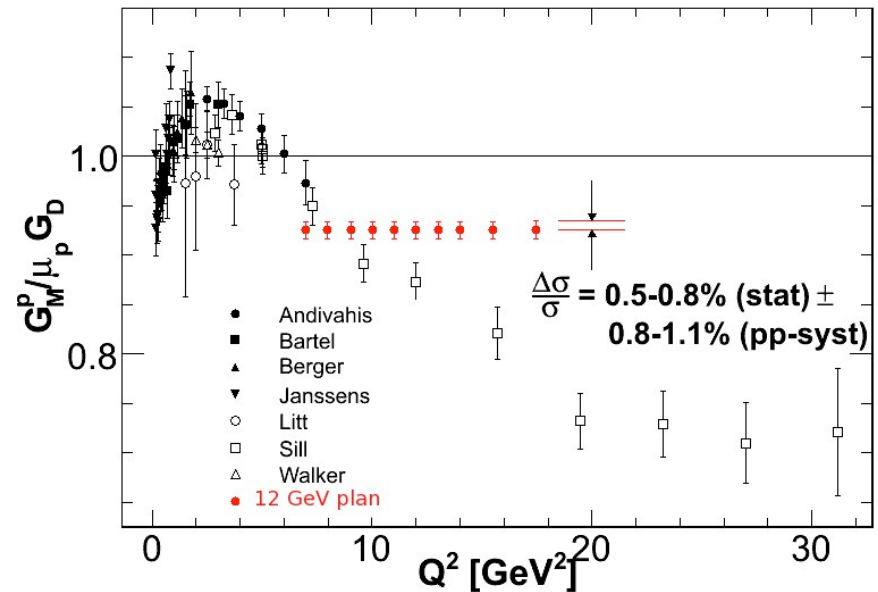
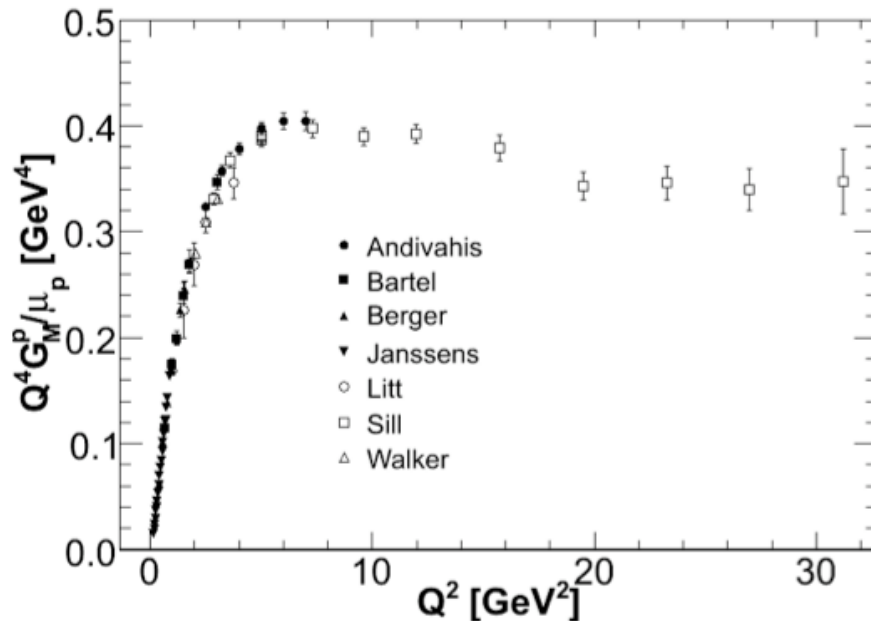
- Beam energy 11/12 GeV
- Beam power 1 MW
- Beam current (Hall A/D) 85/5  $\mu\text{A}$
- Beam polarization 85%
- Emittance @ 12 GeV 10 nm-rad
- Energy spread @ 12 GeV 0.02%
- Beam spot  $\sim 0.1\text{mm}$
- Simultaneous beam delivery Up to 3 halls

Hall A will be the first hall which will get the beam

# GMP at high $Q^2$

precision data for GMP with HRS at 11 GeV

B.Moffit, S.Gilad, J.Arrington & BW



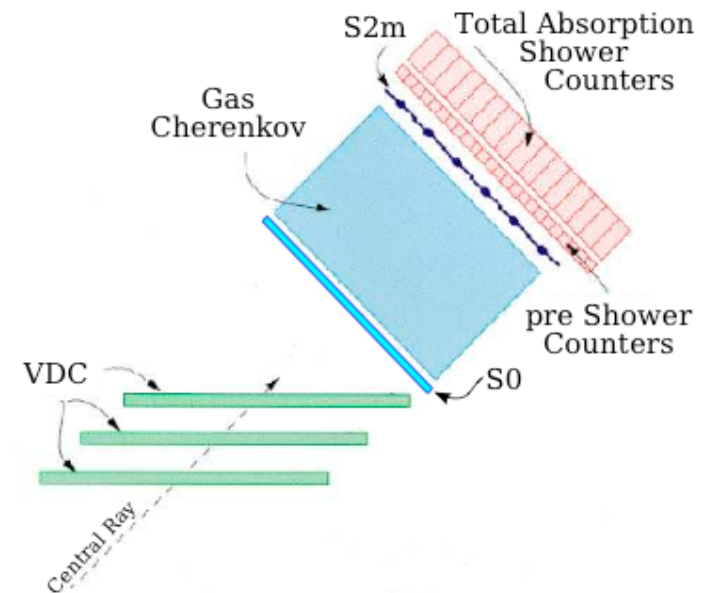
GMP is the base for all other form factor measurements

Approved single arm measurement will use existing HRSs of Hall A, high luminosity, well understood optics, enhanced detector packages

# GMP with HRS

| $E_{beam}$ ,<br>GeV | $Q^2$ ,<br>GeV <sup>2</sup> | $\theta_e$<br>degree | $E_{e'}$ ,<br>GeV | Time,<br>days | Events |
|---------------------|-----------------------------|----------------------|-------------------|---------------|--------|
| 6.6                 | 7.0                         | 35                   | 2.87              | 0.1           | 40k    |
|                     | 8.0                         | 42                   | 2.35              | 0.2           | 40k    |
|                     | 9.0                         | 52                   | 1.78              | 0.5           | 40k    |
|                     | 10.0                        | 67                   | 1.25              | 1.5           | 40k    |
| 8.8                 | 9.0                         | 29                   | 4.00              | 0.2           | 40k    |
|                     | 10.0                        | 33                   | 3.47              | 0.5           | 40k    |
|                     | 11.0                        | 38                   | 2.95              | 0.5           | 40k    |
|                     | 12.0                        | 44                   | 2.42              | 1.5           | 40k    |
|                     | 13.0                        | 53                   | 1.86              | 3.0           | 28k    |
| 11                  | 13.0                        | 31                   | 4.07              | 1             | 28k    |
|                     | 14.0                        | 35                   | 3.53              | 2             | 24k    |
|                     | 15.5                        | 42                   | 2.74              | 2.5           | 20k    |
|                     | 17.5                        | 58                   | 1.69              | 12            | 16k    |

Table of kinematics  
Systematical uncertainties  
Advanced optics analysis

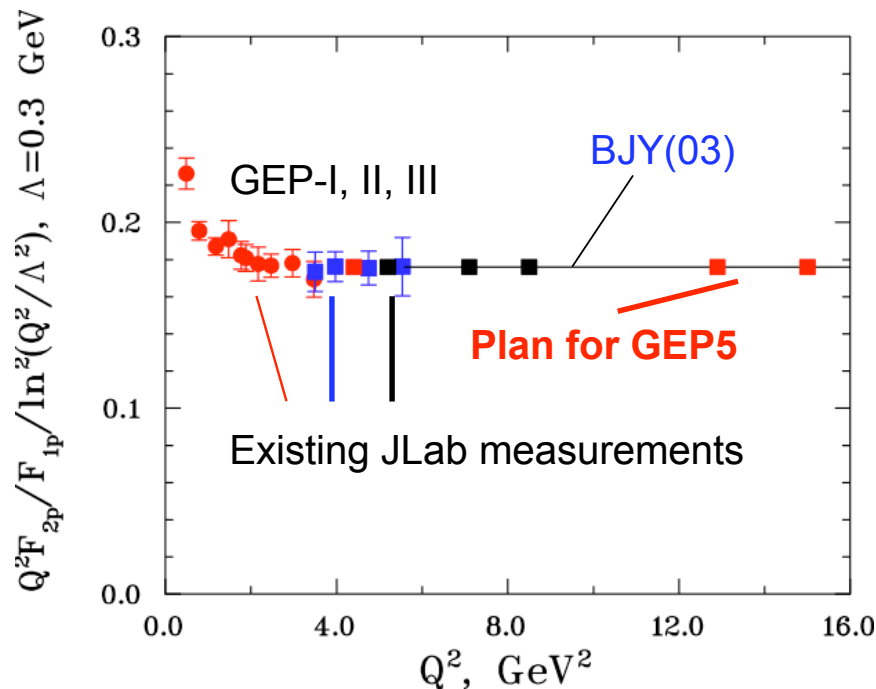


Improved track reconstruction

# GEP/GMP for max $Q^2$

Pentchev, Perdrisat, Punjabi, Cisbani & BW

$$\mathcal{J}_{hadronic}^{\mu} = ie\bar{N}(p') \left[ \gamma^{\mu} F_1(Q^2) + \frac{i\sigma^{\mu\nu} q_{\nu}}{2M} F_2(Q^2) \right] N(p)$$



- Up to max  $Q^2 = 15 \text{ GeV}^2$
- Study the spin flip part of the hadron current
- Constrain GPDs at high  $t$
- Provide critical test of the FF models and reaction dynamics

$\Delta(F_2/F_1)/(F_2/F_1)$  accuracy will be **3%**

compare to  $\frac{\ln^2(Q^2=10/\Lambda^2)}{\ln^2(Q^2=15/\Lambda^2)} = 0.85$

# Challenges at high $Q^2$

$$\text{Form factor} \propto Q^{-4}$$

$$\text{Cross section} \propto E^2/Q^4 \times Q^{-8}$$

$$\begin{aligned} \text{Figure-of-Merit} &\propto A_Y^2 \times \sigma \times \Omega \\ &\propto E^2/Q^{16} \end{aligned}$$

Need large statistics  $\rightarrow$  max luminosity and solid angle

Max luminosity  $\rightarrow$  large background

Large solid angle  $\rightarrow$  small bend  $\rightarrow$  huge background

Solution is a modern tracking detector based on  
Gas Electron Multiplier (F.Sauli, 1997)

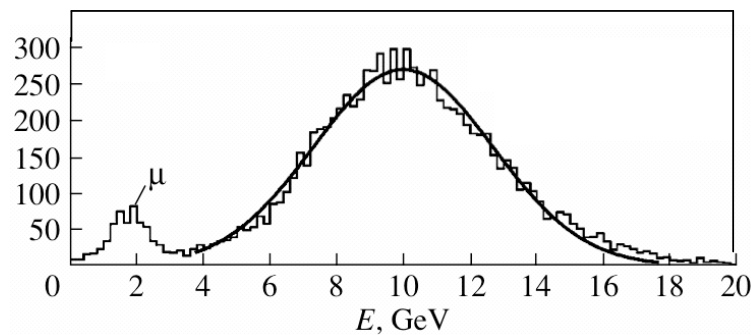
$$H(\vec{e}, e' \vec{p})$$


# New in GEP5 experiment

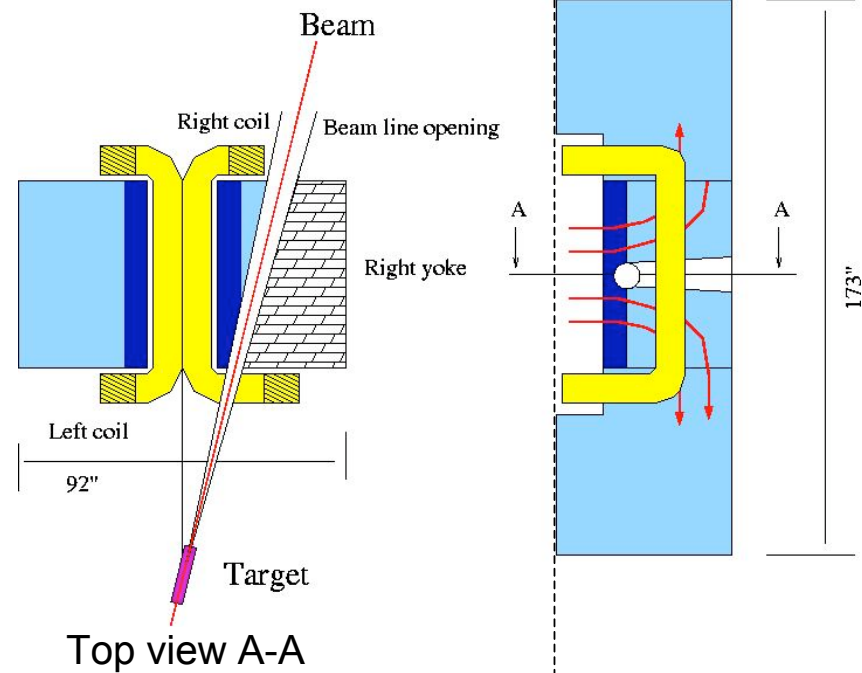
1. Large solid angle in the proton arm at a small scattering angle achieved with single dipole magnet. Beam line will go through a hole in magnet pole.
2. Gas Electron Multiplier chambers to handle high rate of the background. Similar counting rates handled in COMPASS; rate will be much higher in LHCb.
3. High threshold trigger with hadron calorimeter.

# Proton Arm

- Magnet: 48D48 - 46 cm gap, 3 Tm field integral, 100 ton
- solid angle is 35 msr for GEP, could be  $\sim 70$  msr
- GEM chambers for tracking with  $70\text{ }\mu\text{m}$  resolution
- momentum resolution is 0.5% for 8.5 GeV/c proton
- angular resolution is 0.2-0.3 mrad
- trigger threshold is 4 GeV from hadron calorimeter



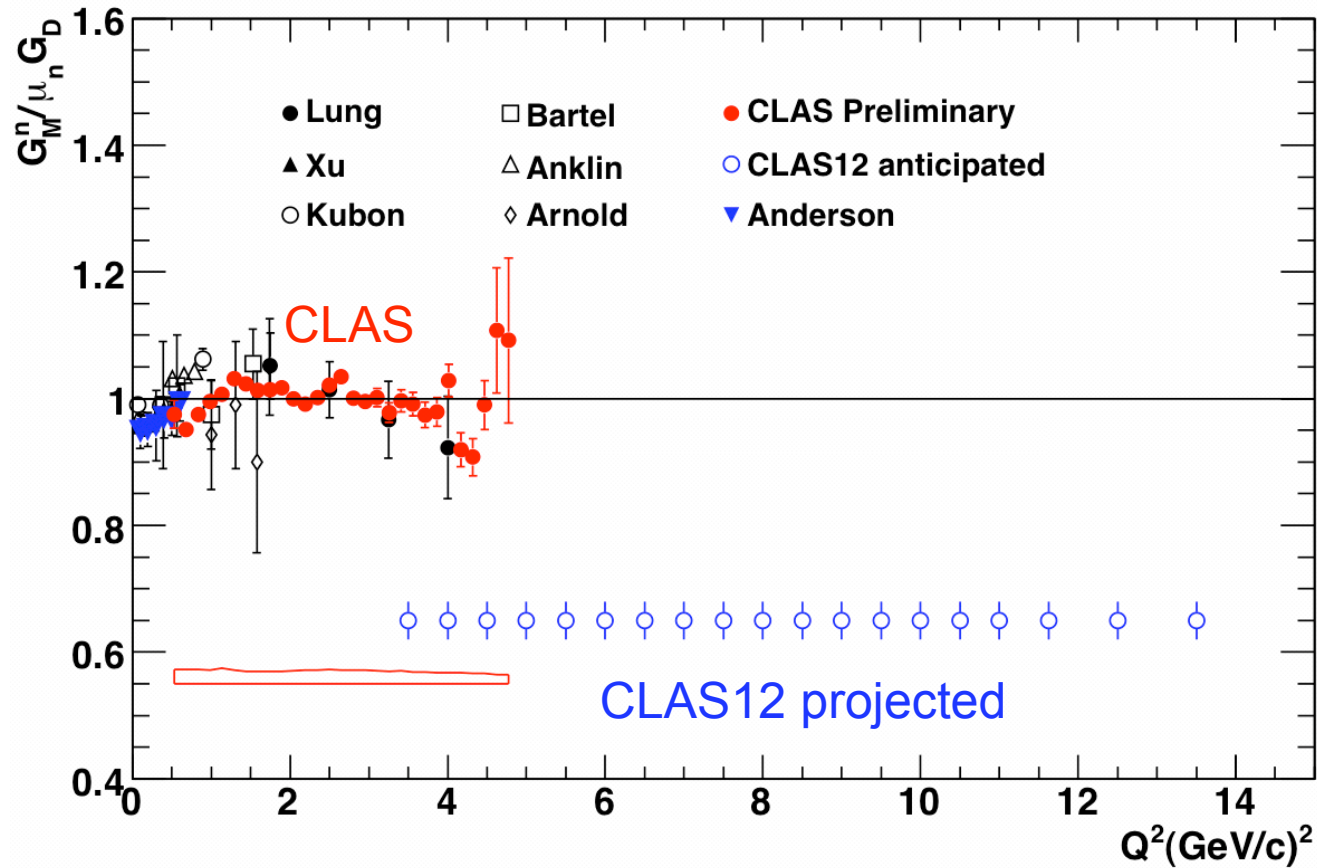
Calorimeter response for 10 GeV protons from test for Compass experiment



Top view A-A

# GMN/GMP at high $Q^2$

Brooks, Gilfoyle, Fafidi, Lachniet, Vineyard

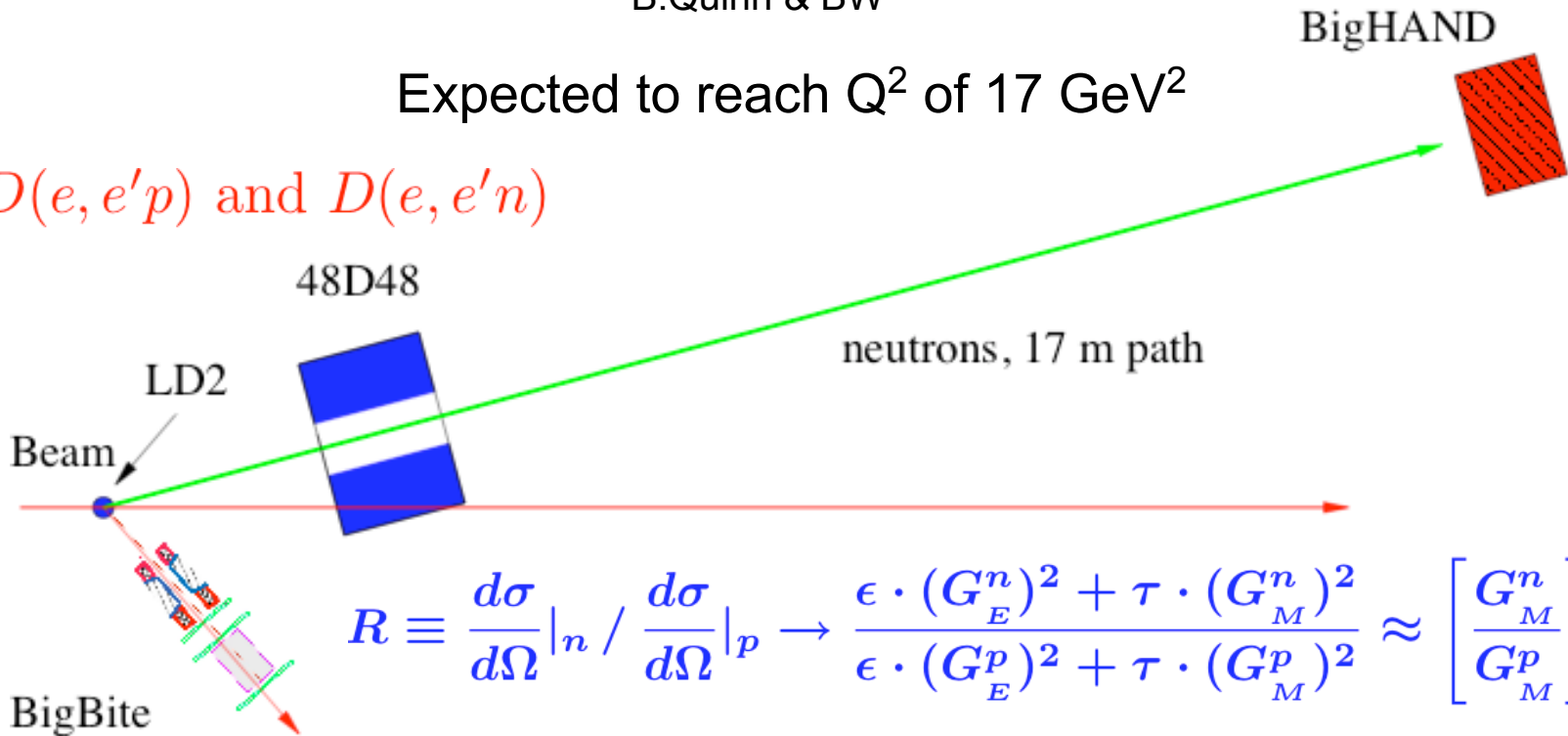


# GMN concept for max $Q^2$

B.Quinn & BW

Expected to reach  $Q^2$  of 17  $\text{GeV}^2$

$D(e, e'p)$  and  $D(e, e'n)$

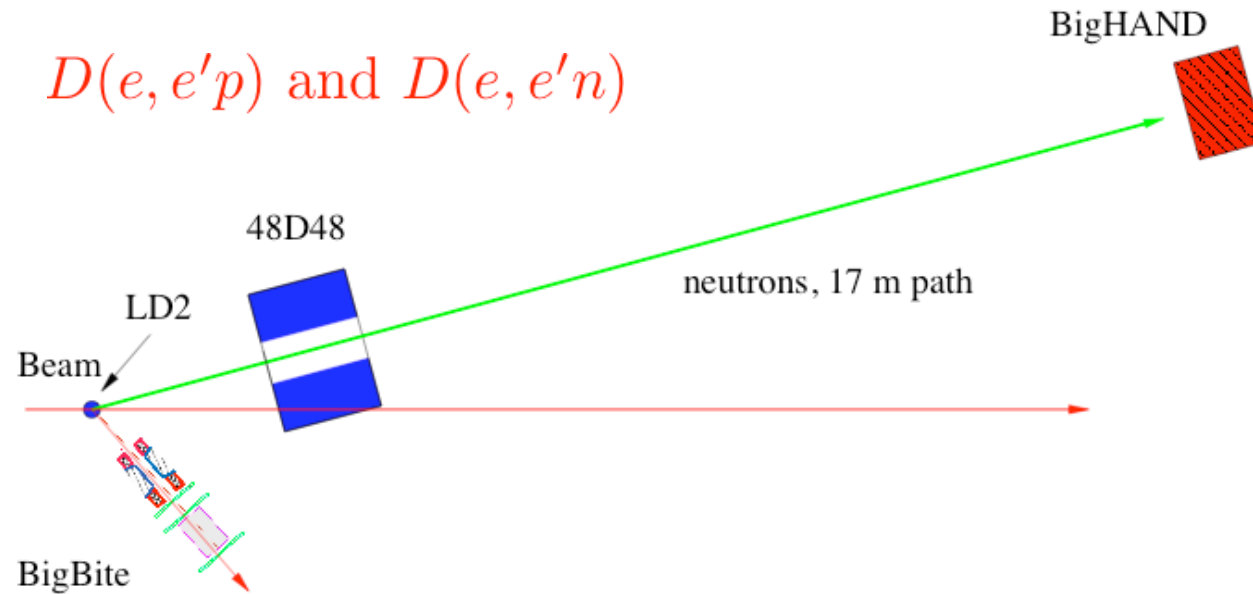


$$R \equiv \frac{d\sigma}{d\Omega}|_n / \frac{d\sigma}{d\Omega}|_p \rightarrow \frac{\epsilon \cdot (G_E^n)^2 + \tau \cdot (G_M^n)^2}{\epsilon \cdot (G_E^p)^2 + \tau \cdot (G_M^p)^2} \approx \left[ \frac{G_M^n}{G_M^p} \right]^2$$

$$\text{luminosity } \mathcal{L}_{eN} = 1 \cdot 10^{38} \text{ cm}^{-2}/s$$

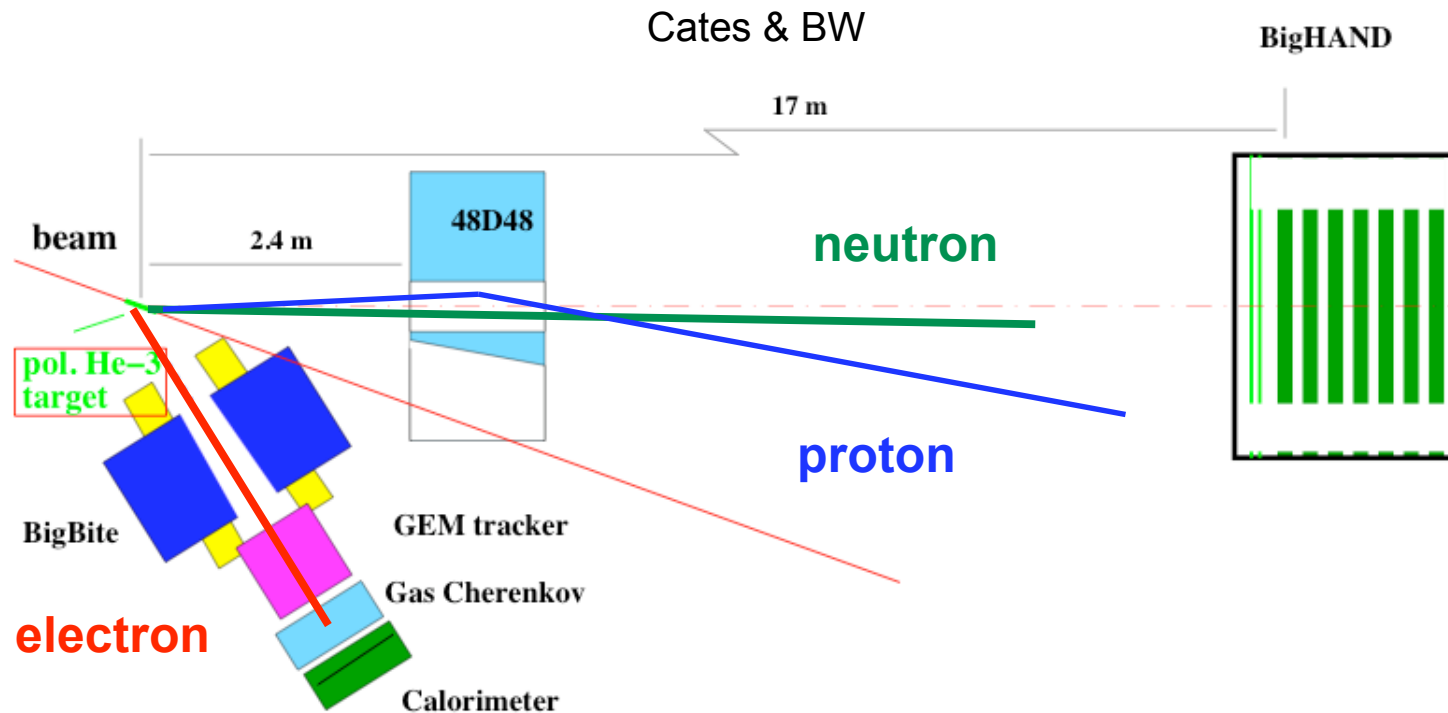
$$\text{accuracy for } G_M^n/G_M^p \sim 1 - 2\% \text{ in 50 days run}$$

# Scheme for GMN/GMP in details



- Long neutron path: angular resolution  $\sim 2$  mr, ToF  $\sim 0.3$  ns
- BigBite with GEM tracker: easy handle  $10^{38}$  cm<sup>-2</sup>/s luminosity, resolution of 0.1% at 1 GeV electron momentum
- 48D48 OFF/ON for protons: measurement of  $N(n+p)/N(n)$  in the same detector

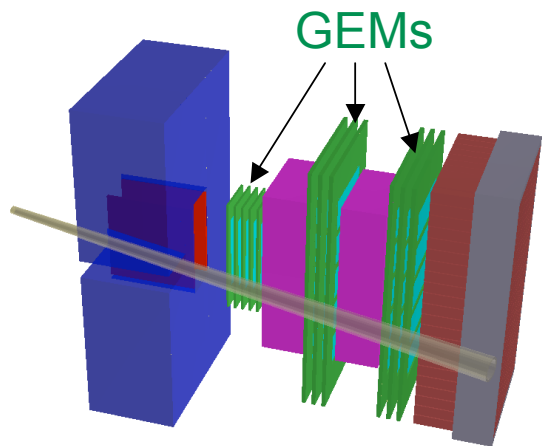
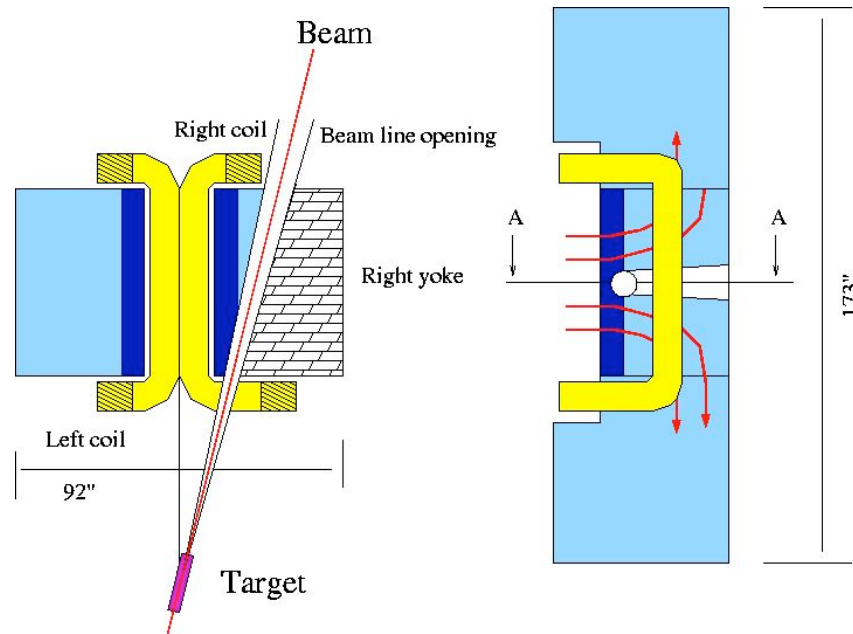
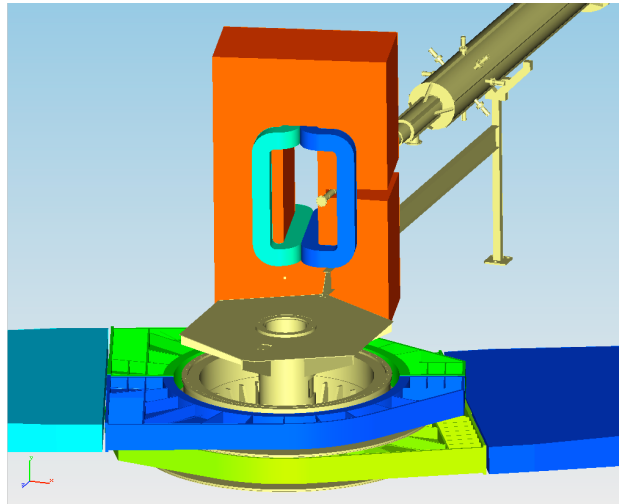
# GEN/GMN at $7.5 \text{ GeV}^2$



Beam energy of 6.6 GeV, 30 mA. Target: He-3, polarization 70%, 30 days

$G_E^n$  at  $7.5 \text{ GeV}^2$  with uncertainty of 20% \*  $G_{\text{Galster}}$  (or 0.06  $G_{\text{Dipole}}$ ).

# Multi Purpose Spectrometer



- Magnet: 48D48 - 46 cm gap, 2-3 Tesla\*m
- Solid angle is 70 msr at angle 15 deg.
- GEM chambers with 70  $\mu\text{m}$  resolution
- momentum resolution is 0.5% for 5 GeV/c
- angular resolution is 0.3 mr

# Parameters of MPS

Solid angle

| $\theta_{central},$<br>degree | $\Omega,$<br>msr | D,<br>meter | Hor. range,<br>degree | Vert. range,<br>degree |
|-------------------------------|------------------|-------------|-----------------------|------------------------|
| 3.5                           | 5                | 9.5         | $\pm 1.3$             | $\pm 3.3$              |
| 5.0                           | 12               | 5.8         | $\pm 1.9$             | $\pm 4.9$              |
| 7.5                           | 30               | 3.2         | $\pm 3$               | $\pm 8$                |
| 15                            | 72               | 1.6         | $\pm 4.8$             | $\pm 12.2$             |
| 30                            | 76               | 1.5         | $\pm 4.9$             | $\pm 12.5$             |

Resolution:

Momentum  $\Rightarrow$  
$$\frac{\sigma_p}{P} = 0.001 \cdot P[GeV]$$

Angular  $\Rightarrow$  
$$\sigma_\theta = 0.2 - 0.3 \text{ mr}$$

Momentum acceptance  $\Rightarrow$  
$$P \text{ range } 2 - 10 \text{ GeV}/c$$

# Physics experiments with MPS

## Exclusive processes

Nucleon FFs (GEP,GMP,GMN)

DVCS, WACS

Single pion production

Phi meson production

J/Psi photo-production

$e,e'\pi$  and  $e,e'\eta$  at large  $Q^2$  & low  $W$

## Polarized and exotic targets

GEN with He-3

Pol. DIS

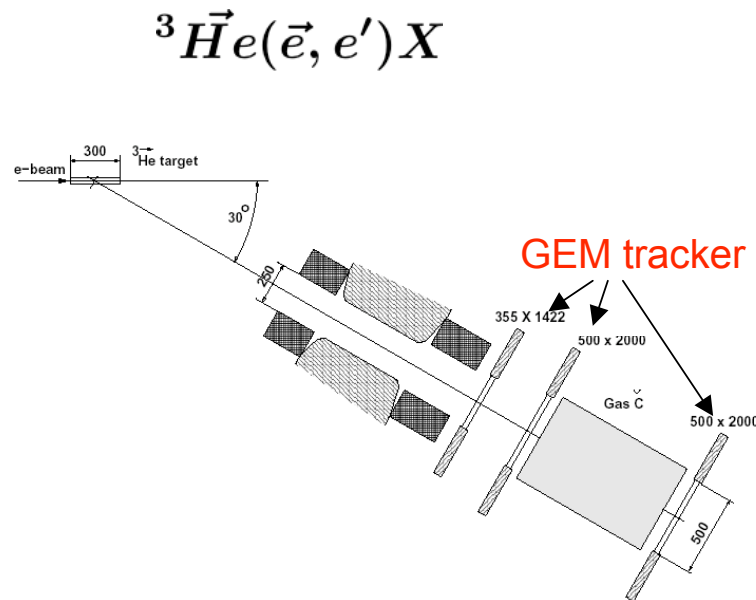
Pol. SIDIS

T/He-3 for u/d

ALL-WACS

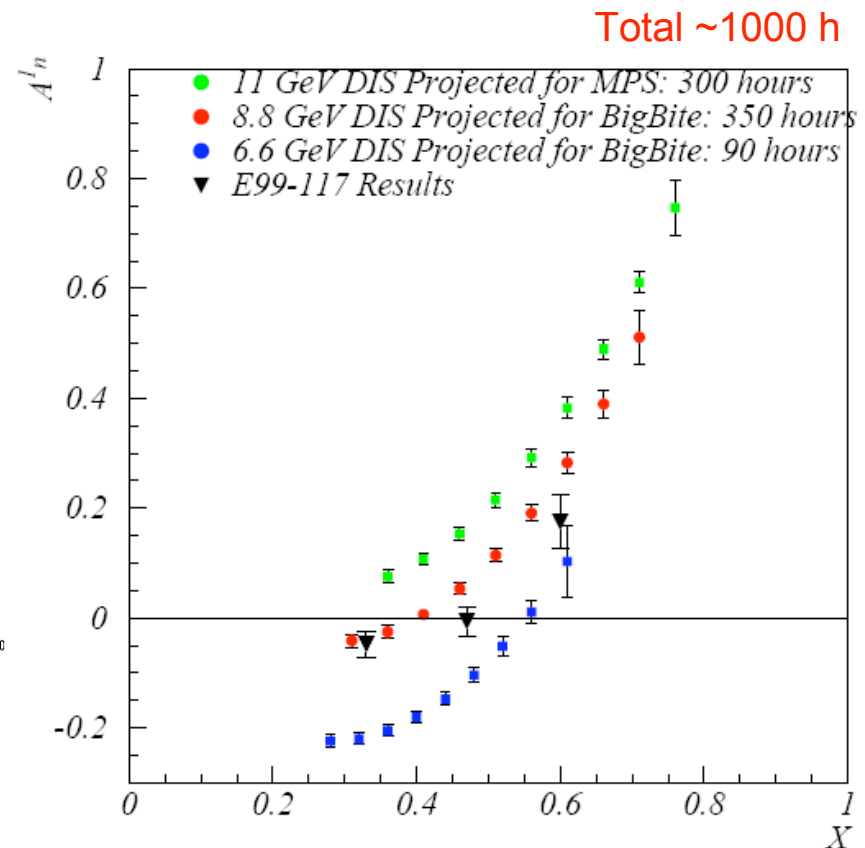
# Polarized DIS with MPS

Cates, Liyanage, Meiziani,  
Rosner, Zheng, and BW



MPS advantage over HMS+SHMS ~ 12

MPS advantage over BigBite ~ 6



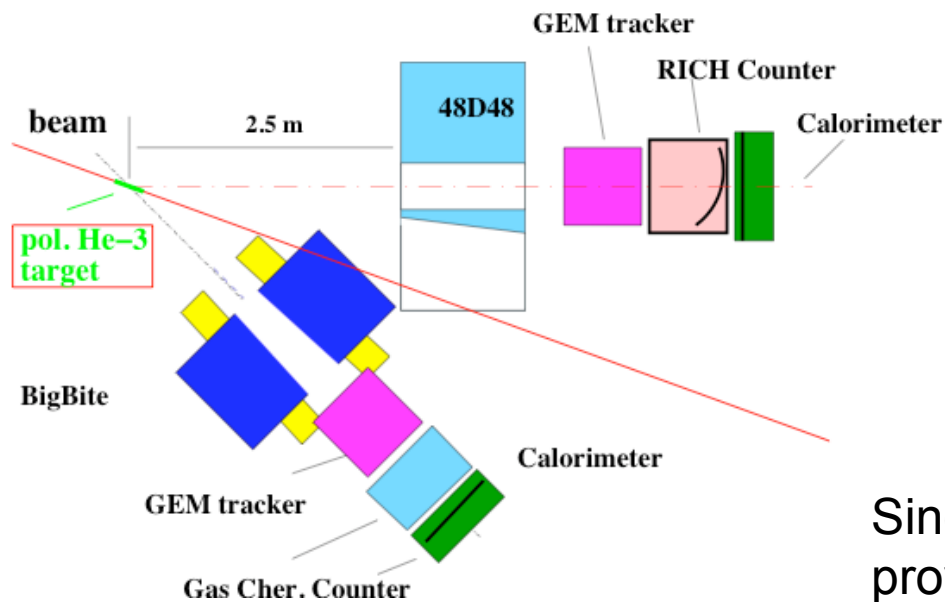
very good accuracy, x up to 0.75  
first test of  $Q^2$  dependence

# Neutron Transversity with MPS

MPS at 20 deg, BigBite at 25 deg

Cisbani & BW

40 msr x 50 msr



In one month **30,000 times more events** than in all transv. data collected by HERMES

Single run of MPS will provide full coverage for **all  $P_{\perp} > 1/6$  of  $P_{\parallel}$**

# Road map and time line

GEP5 experiment was approved in August 2007

- INFN **approved** ( September 2007) a startup GEM funding
- INFN funding is needed: 5 years grant for the front tracker of the MPS spectrometer, expected in September 2008
- NSF funding is needed: \$1.8M MRI grant for the FPP trackers including electronics, expected in summer 2009
- UK funding is needed for GEM DAQ and trigger construction

Time line for the construction project:

- ☐ First telescope GEM tracker in 2008: test in Hall A
- ☐ Project technical review in 2008
- ☐ BNL magnet in 2010
- ☐ First full size tracking device by 2011
- ☐ Front tracker by 2012
- ☐ FPP trackers by 2013
- ☐ Hadron calorimeter/electronics in 2013

# Summary

❖ 12 GeV CEBAF will provide precision nucleon Form Factors values:

- ✓  $G_E^p$  @ 15 GeV<sup>2</sup>
- ✓  $G_M^p$  @ 17.5 GeV<sup>2</sup>
- ✓  $G_E^n$  @ 7.5+ GeV<sup>2</sup>
- ✓  $G_M^n$  @ 14+ GeV<sup>2</sup>

❖ MPS spectrometer will be a universal tool for experiments in hadron physics at large  $Q^2$