

# Electromagnetic Transition Form Factors

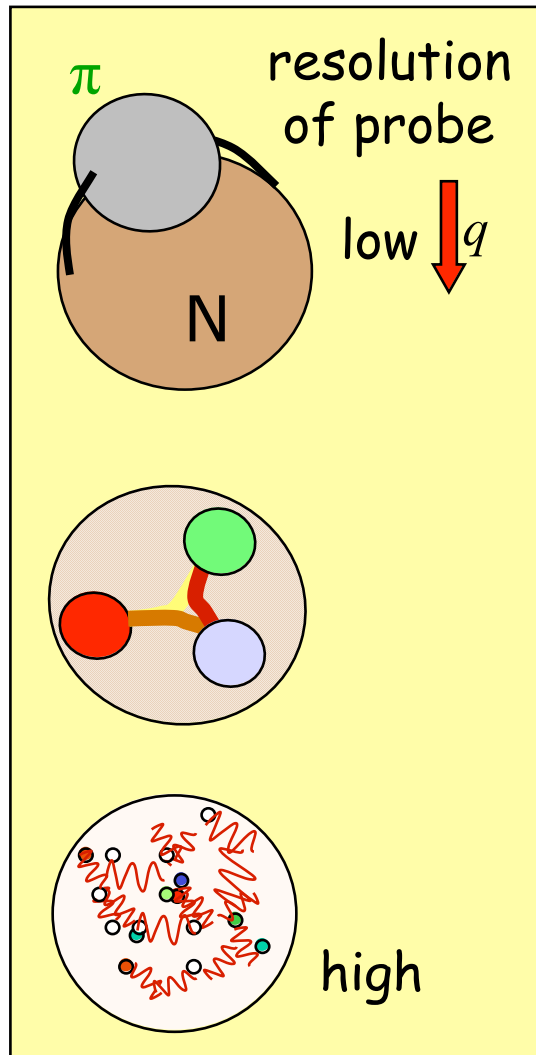
Aznauryan, V. D. Burkert, V. Mokeev

Jefferson Lab

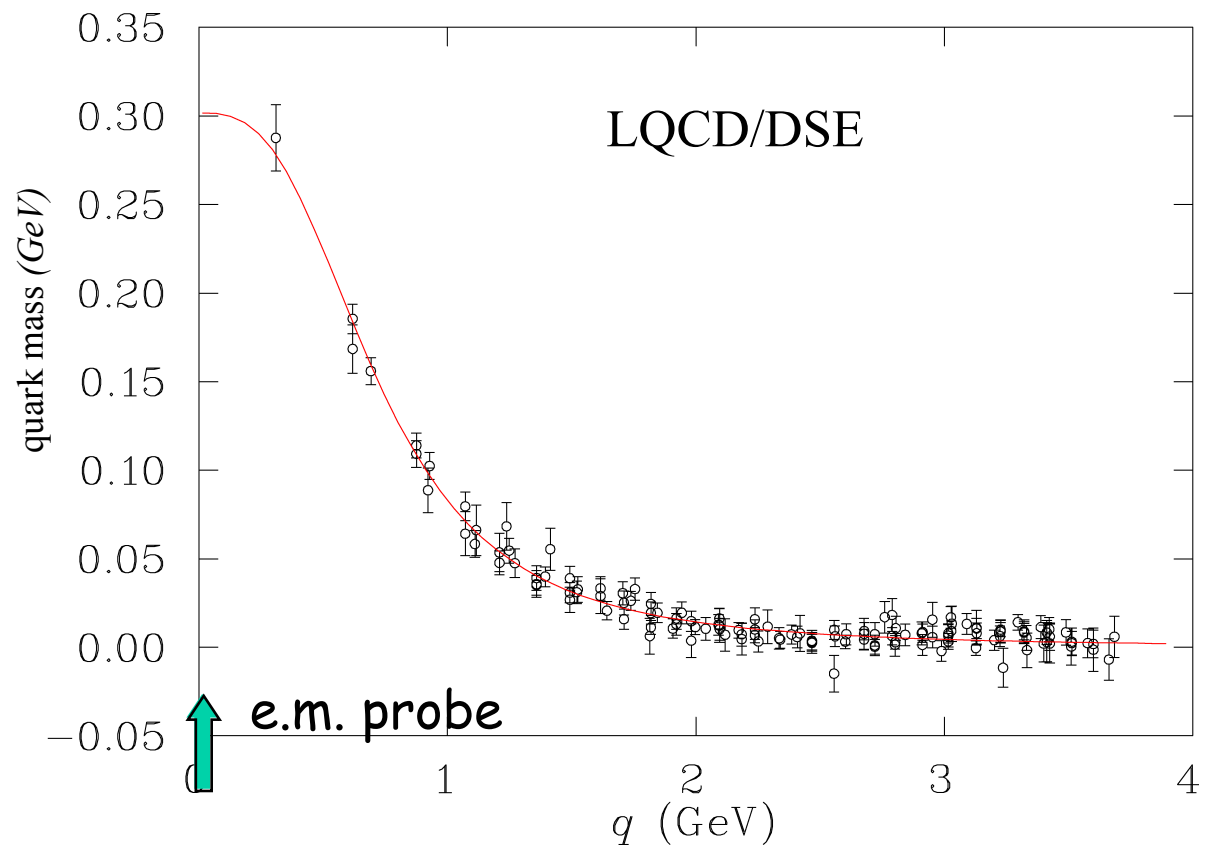
(CLAS Collaboration)

- Motivation
- Baryon resonance transitions in  $N\pi$ ,  $N\eta$ 
  - $N\Delta(1232)$  multipoles
  - Roper  $P_{11}(1440)$ ,  $S_{11}(1535)$
  - Helicity structure of  $D_{13}(1520)$
- Transition amplitudes in  $p\pi^+\pi^-$  channel
  - $P_{11}(1440)$ ,  $D_{13}(1520)$ ,  $D_{33}(1700)$ ,  $P_{13}(1720)$
- Summary & Outlook

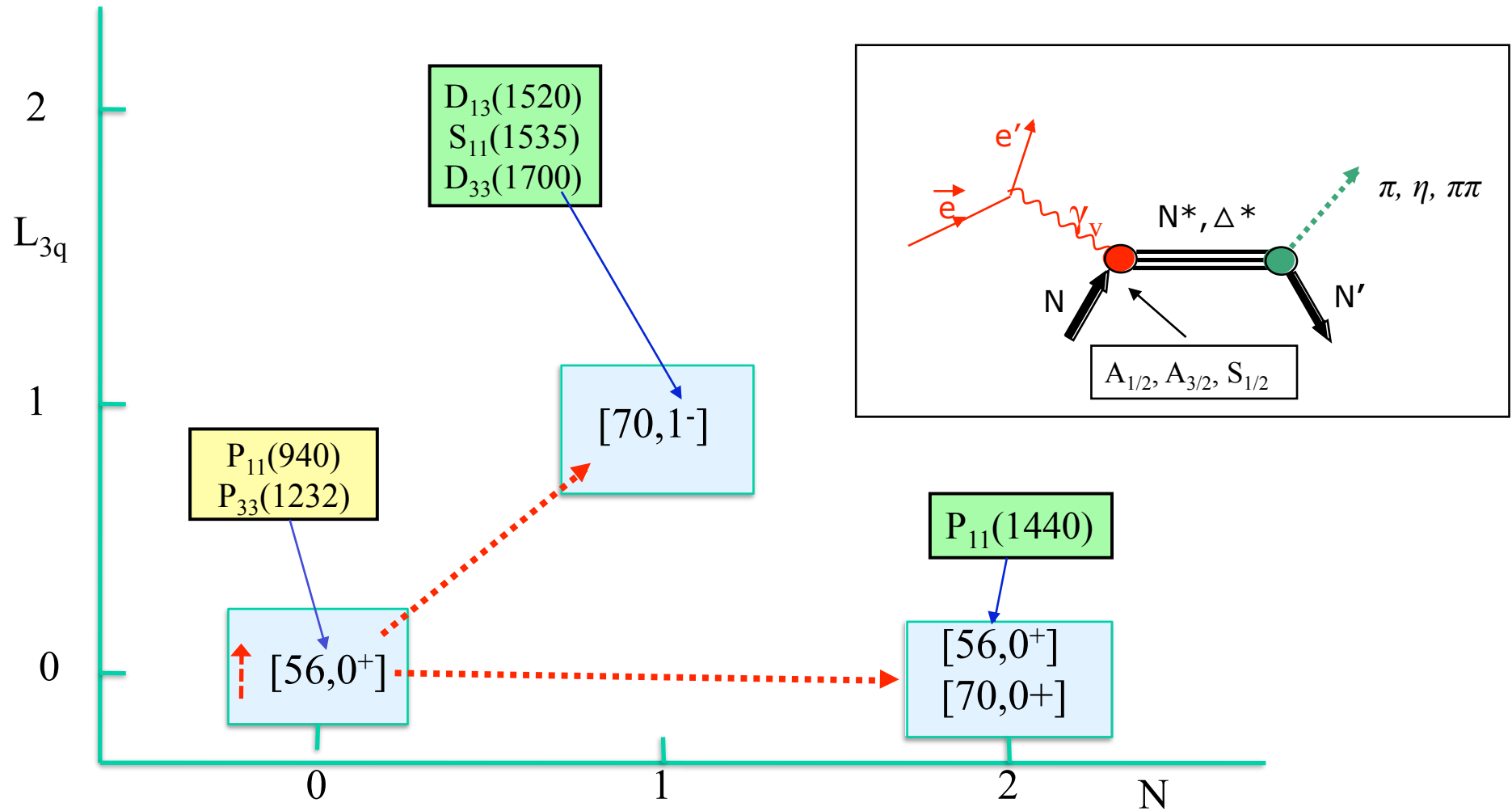
# Hadron Structure with e.m. Probes?



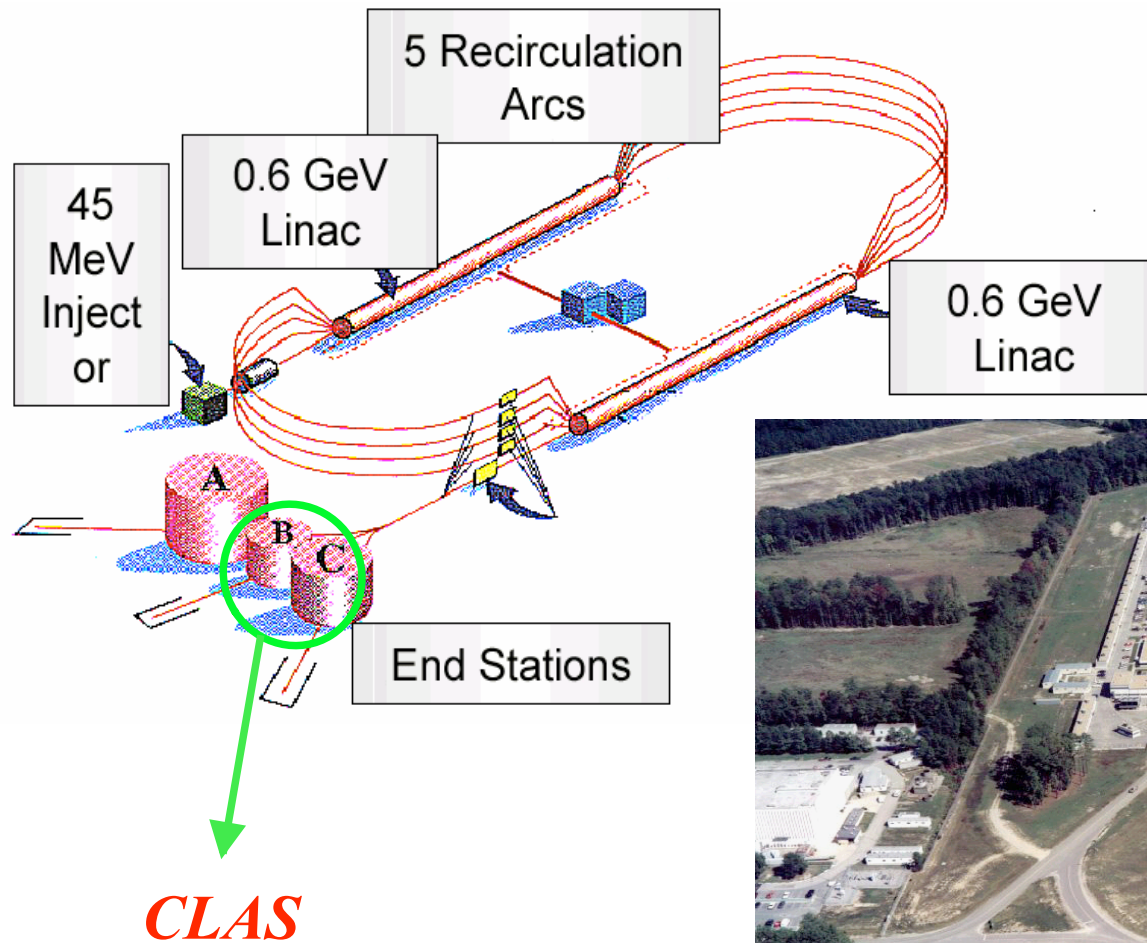
Allows to address central question:  
**What are the relevant degrees-of-freedom at varying distance scale?**



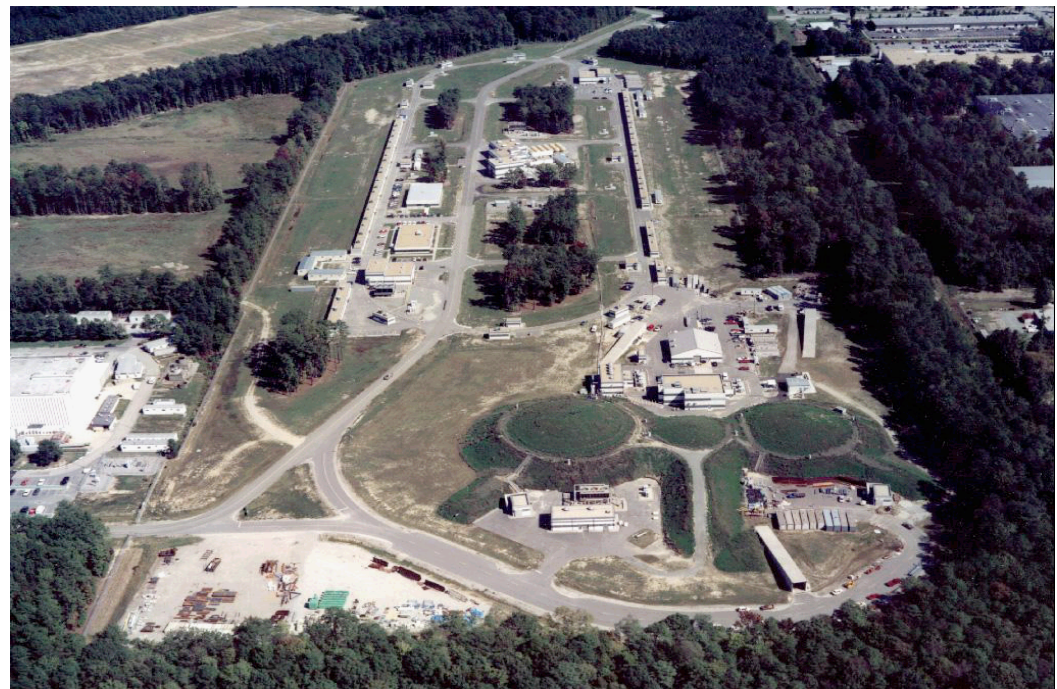
# SU(6)×O(3) Classification of lowest lying Baryons



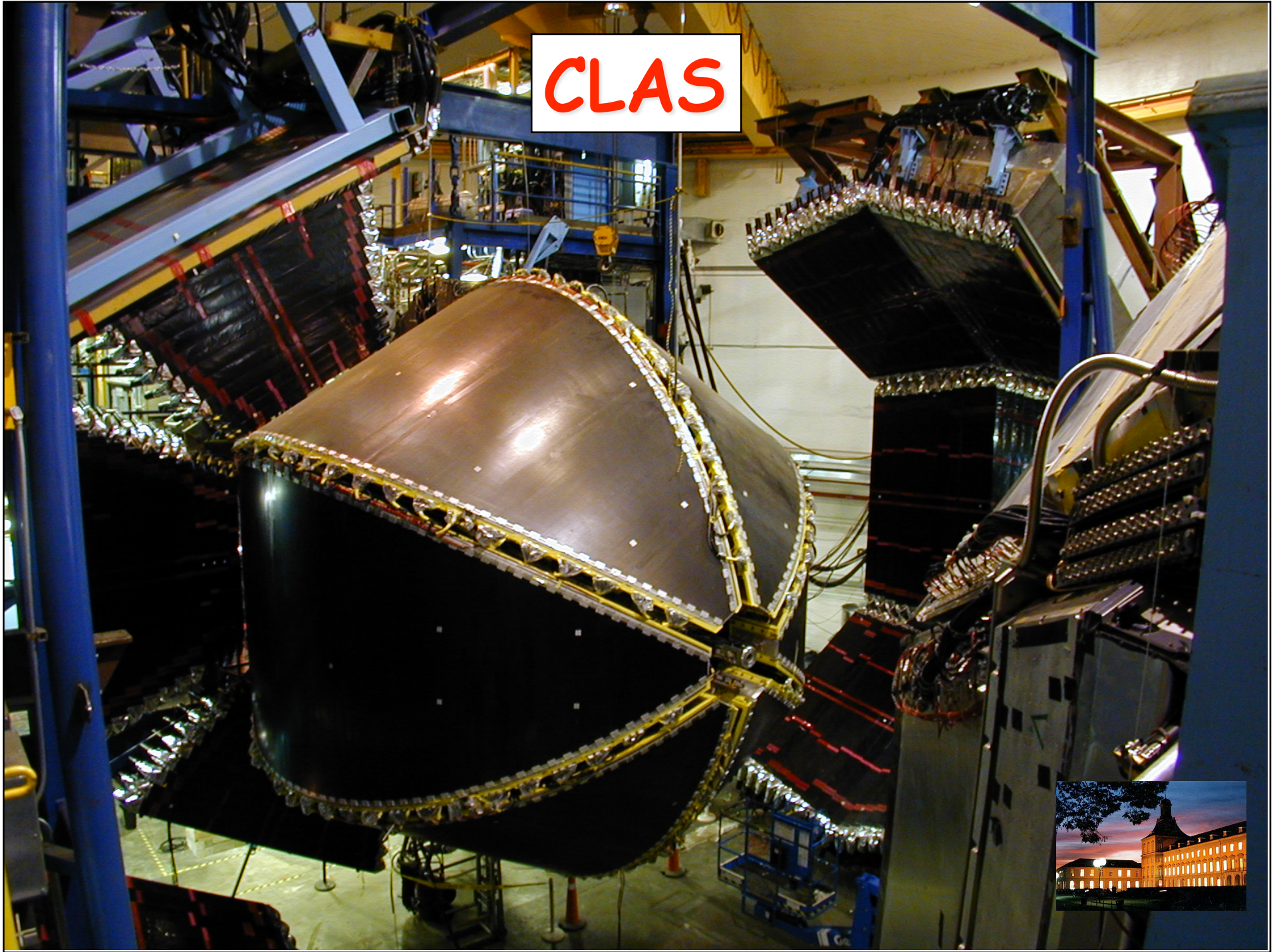
# JLab Site: The 6 GeV CW Electron Accelerator



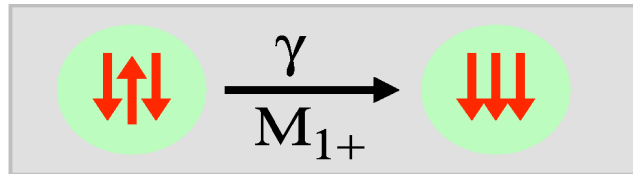
$E_{\max}$	~ 6 GeV
$I_{\max}$	~ 200 $\mu\text{A}$
Duty Factor	~ 100%
$\sigma_E/E$	~ $2.5 \cdot 10^{-5}$
Beam P	~ 85%
$E_g(\text{tagged})$	~ 0.8-5.5 GeV



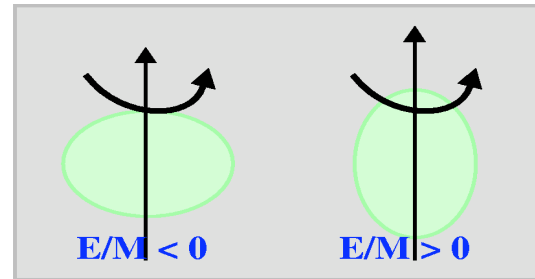
CLAS



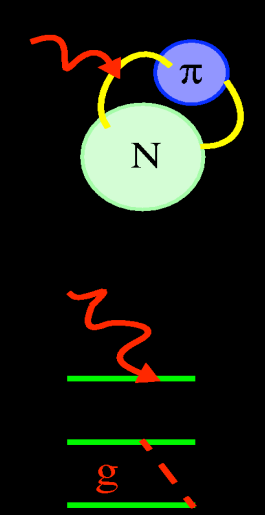
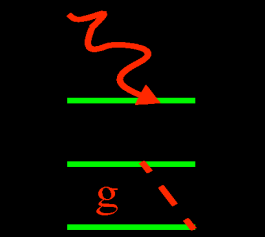
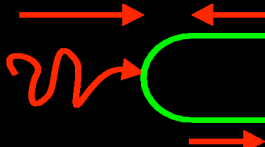
# N- $\Delta(1232)$ Quadrupole Transition

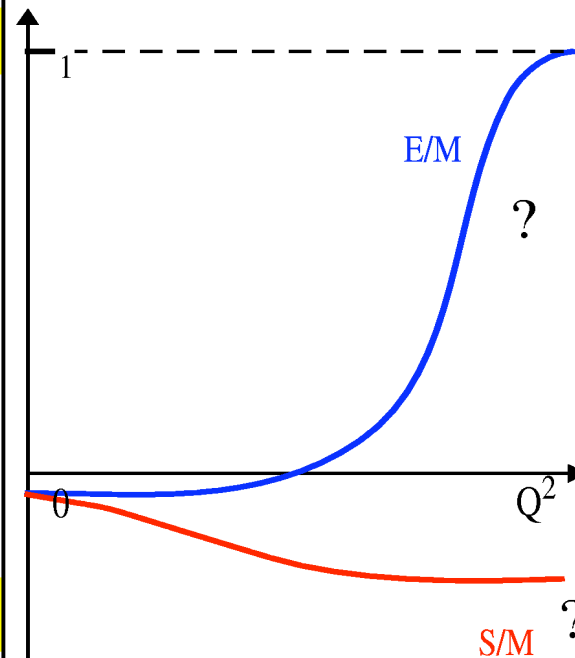


**SU(6):  $E_{1+}=S_{1+}=0$**

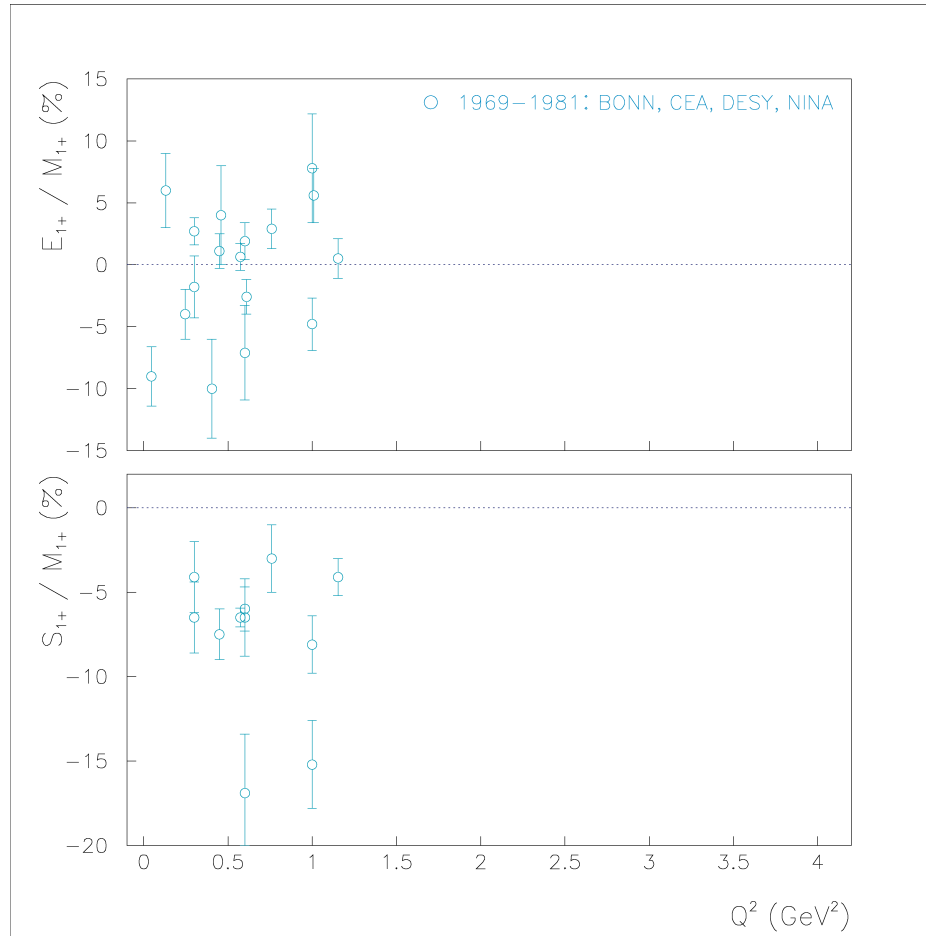


(A. Buchmann, E. Henley, 2000)

		E/M	S/M
	pion cloud	~0.03	~0.1
	one-gluon exch.	~ 0.01	
	pQCD	+1	const.



# Multipole Ratios $R_{EM}$ , $R_{SM}$ before 1999



← Sign?

←  $Q^2$  dependence?

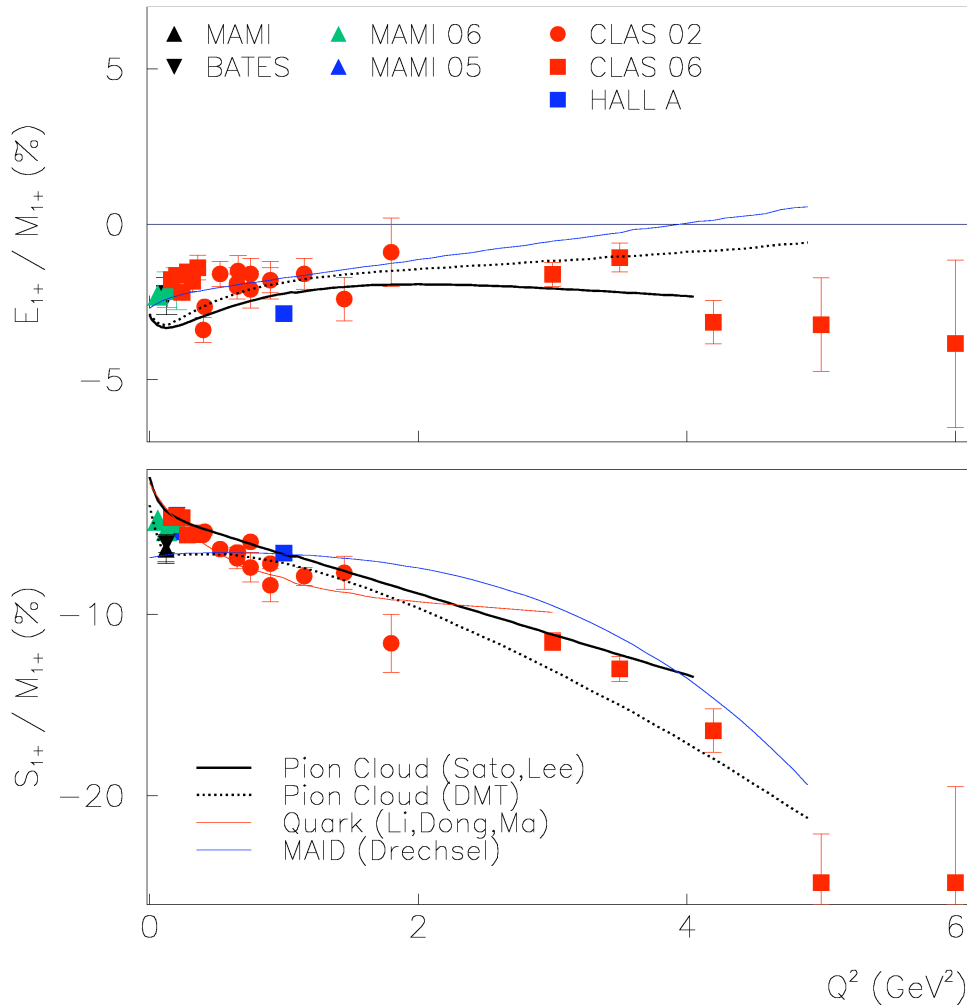
➤ Data could not determine sign or  $Q^2$  dependence

# N $\Delta$ electroproduction experiments after 1999

Reaction	Observable	W	Q <sup>2</sup>	Author, Conference, Publication	LAB
p(e,e'p) $\pi^0$	$\sigma_0$ $\sigma_{TT}$ $\sigma_{LT}$ $\sigma_{LTP}$	1.221	0.060	S. Stave, EPJA, 30, 471 (2006)	MAMI
p(e,e'p) $\pi^0$	$R'_{LT}$ , $R''_{LT}$ $R^i_{LT}$	1.232	0.121	H. Schmieden, EPJA, 28, 91 (2006)	MAMI
p(e,e'p) $\pi^0$	$R'_{LT}$ , $R''_{LT}$ $R^i_{LT}$	1.232	0.121	Th. Pospischil, PRL 86, 2959 (2001)	MAMI
p(e,e'p) $\pi^0$	$\sigma_0$ $\sigma_{TT}$ $\sigma_{LT}$ $\sigma_{LTP}$	1.232	0.127	C. Mertz, PRL 86, 2963 (2001) C. Kunz, PLB 564, 21 (2003) N. Sparveris, PRL 94, 22003 (2005)	BATES
p(e,e'p) $\pi^0$	$\sigma_0$ $\sigma_{TT}$ $\sigma_{LT}$ $\sigma_{LTP}$	1.232 1.221	0.127 0.200	N. Sparveris, SOH Workshop (2006) N. Sparveris, nucl-ex/611033	MAMI
p(e,e'p) $\pi^0$	$A_{LT}$ $A_{LTP}$	1.232	0.200	P. Bartsch, PRL 88, 142001 (2002) D. Elsner, EPJA, 27, 91 (2006)	MAMI
p(e,e'p) $\pi^0$ p(e,e'p $^+$ )n	$\sigma_0$ $\sigma_{TT}$ $\sigma_{LT}$ $\sigma_{LTP}$	1.10-1.40	0.16-0.35	C. Smith, SOH Workshop (2006)	JLAB / CLAS
p(e,e'p) $\pi^0$	$\sigma_0$ $\sigma_{TT}$ $\sigma_{LT}$	1.11-1.70	0.4-1.8	K. Joo, PRL 88, 122001 (2001)	JLAB / CLAS
p(e,e'p) $\pi^0$ p(e,e'p $^+$ )n	$\sigma_{LTP}$	1.11-1.70	0.40,0.65	K. Joo, PRC 68, 32201 (2003) K. Joo, PRC 70, 42201 (2004) K. Joo, PRC 72, 58202 (2005)	JLAB / CLAS
p(e,e'p $^+$ )n	$\sigma_0$ $\sigma_{TT}$ $\sigma_{LT}$	1.11-1.60	0.3-0.6	H. Egiyan, PRC 73, 25204 (2006)	JLAB / CLAS
p(e,e'p) $\pi^0$	16 response functions	1.17-1.35	1.0	J. Kelly, PRL 95, 102001 (2005)	JLAB / Hall A
p(e,e'p) $\pi^0$	$\sigma_0$ $\sigma_{TT}$ $\sigma_{LT}$	1.10-1.40	3.0-6.0	M. Ungaro, PRL 97, 112003 (2006)	JLAB / CLAS
p(e,e'p) $\pi^0$	$\sigma_0$ $\sigma_{TT}$ $\sigma_{LT}$	1.10-1.35	2.8, 4.0	V. Frolov, PRL 82, 45 (1999)	JLAB / Hall C



# $N\Delta$ Multipole Ratios $R_{EM}, R_{SM}$ in 2007

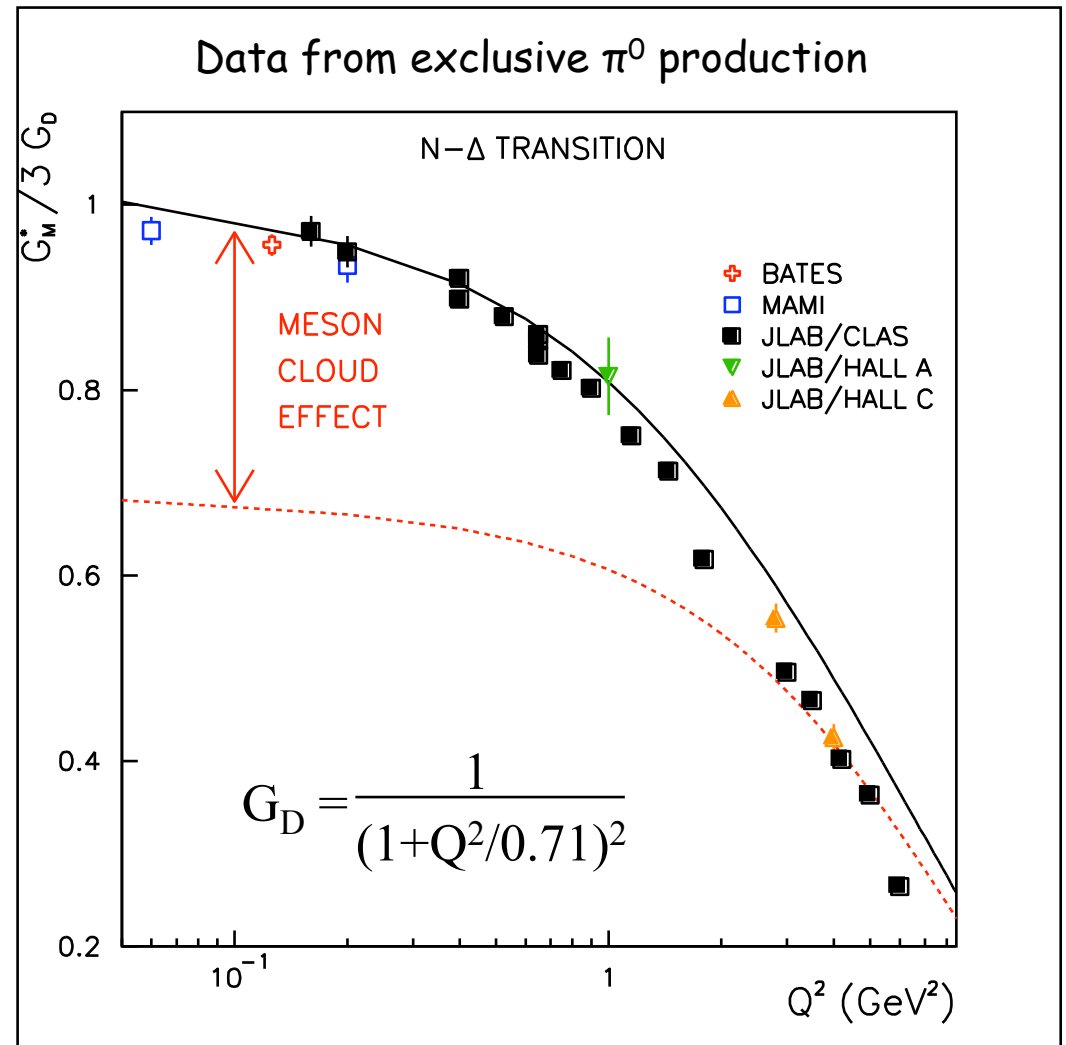


- There is no sign for asymptotic pQCD behavior in  $R_{EM}$  or  $R_{SM}$ .
- $R_{EM} < 0$  at low  $Q^2$  favors **oblate shape of  $\Delta(1232)$**  and prolate shape of the proton.
- Dynamical models attribute the deformation to contributions of the **pion cloud** at low  $Q^2$ .
- Data at  $Q^2 = 7 \text{ GeV}^2$  still to come from Jlab Hall C.

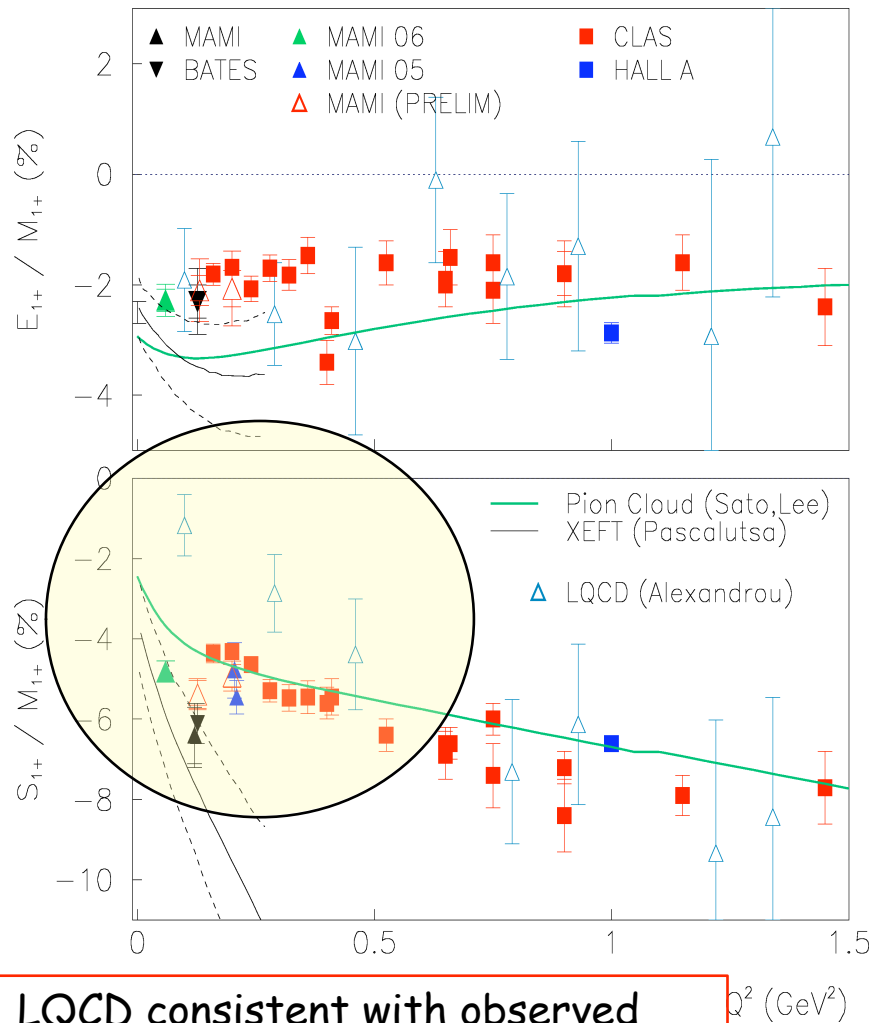
# $N\Delta$ Transition Form Factors - $G_M^*$

➤ 1/3 of  $G_M^*$  at low  $Q^2$  is due to vertex dressing and pion cloud contributions.

Meson contributions play a role even at relatively high  $Q^2$ .



# Comparison with Theory



LQCD consistent with observed rise in magnitude with  $Q^2$  of RSM

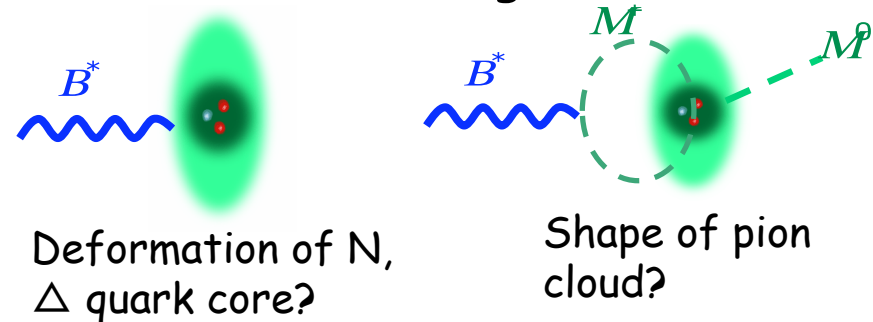
## Quenched Lattice QCD

- $E_{1+}/M_{1+}$ : Good agreement within large errors.
- $S_{1+}/M_{1+}$ : Undershoots data at low  $Q^2$ .
- Linear chiral extrapolations may be naïve and/or dynamical quarks required

## Dynamical Models

- Pion cloud model allows reasonable description of quadrupole ratios over large  $Q^2$  range.

What are we learning from E/M, S/M?



Need to isolate the first term (within model) or go to high  $Q^2$  to study quark core.

# 2nd and 3<sup>rd</sup> nucleon resonance regions

(PDG 2006)

State	$\eta_{N\pi}$	$\eta_{N\eta}$	$\eta_{N\pi\pi}$
$P_{11}(1440)$	0.55-0.75		0.3-0.4
$D_{13}(1520)$	0.55-0.65	0.0023	0.4-0.5
$S_{11}(1535)$	0.35-0.55	0.45-0.60	< 0.1
$D_{33}(1700)$	0.1-0.2		0.8-0.9
$P_{13}(1720)$	0.1-0.2	0.04	> 0.7

## Analysis tools:

- **Unitary isobar model** (UIM), starting from MAID.
- **Dispersion relations** (DR), for **1-pion** analysis.
- Isobar model (JM06) for **2-pion** analysis with leading contributions as observed in the data. Fit to 9 independent one-dimensional projections of 5-dim. cross sections.

# UIM & DR Fit at low & high $Q^2$

# data points > 50,000 ,  $E_e = 1.515, 1.645, 5.75 \text{ GeV}$

Observable	$Q^2$	Number of Data points
$d\sigma/d\Omega(\pi^0)$	0.40	3 530
	0.65	3 818
$d\sigma/d\Omega(\pi^+)$	0.40	2 308
	0.65	1 716
	1.7-4.3	33 000
$A_e(\pi^0)$	0.40	956
	0.65	805
$A_e(\pi^+)$	0.40	918
	0.65	812
	1.7 - 4.3	3 300
$d\sigma/d\Omega(\eta)$	0.375	172
	0.750	412

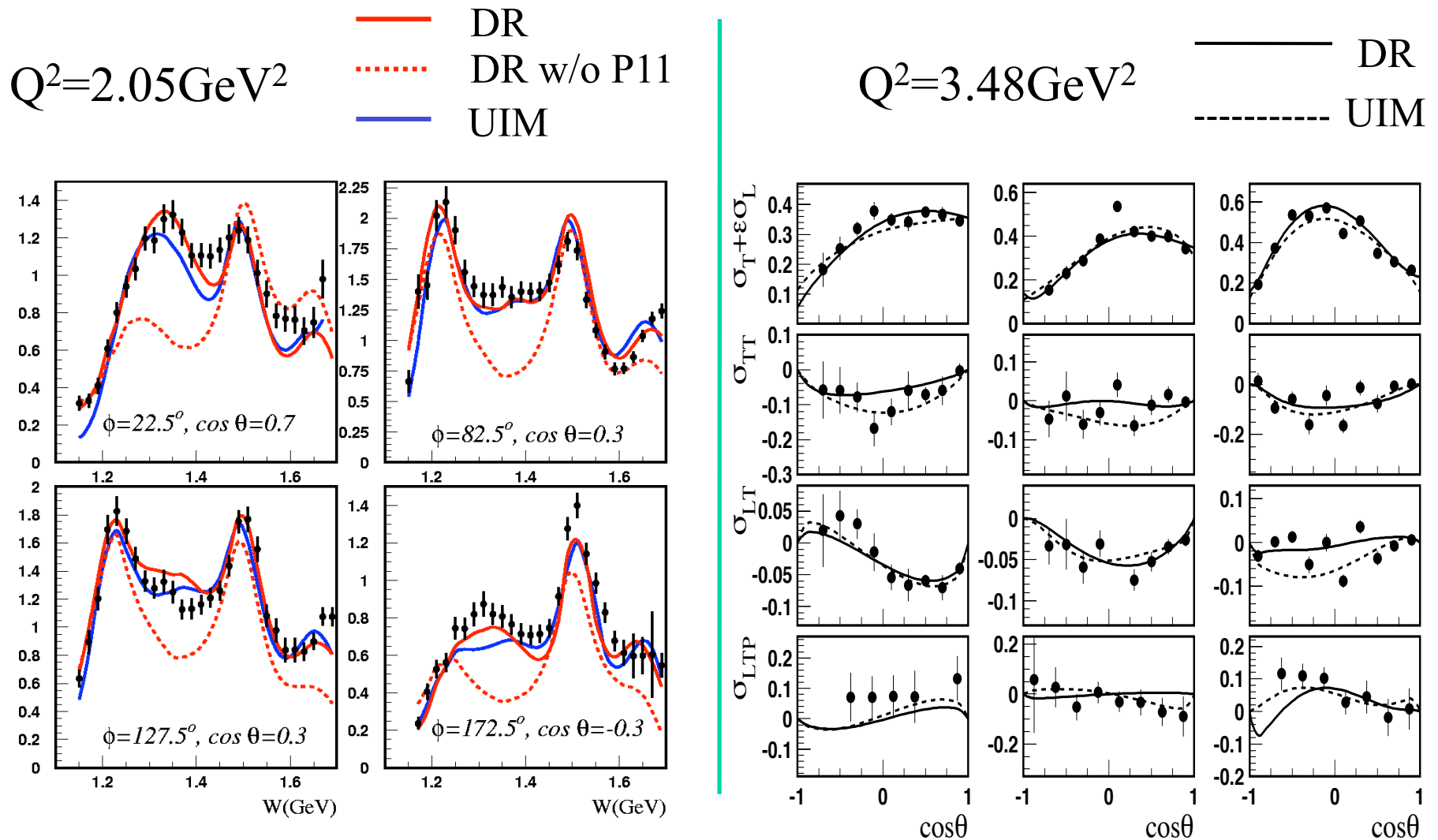
Low  $Q^2$  results:

I. Aznauryan et al.,  
PRC71, 015201, 2005;  
PRC 72, 045201, 2005;

High  $Q^2$  results on Roper:

I. Aznauryan et al.,  
arXiv:0804.0447 [nucl-  
ex].

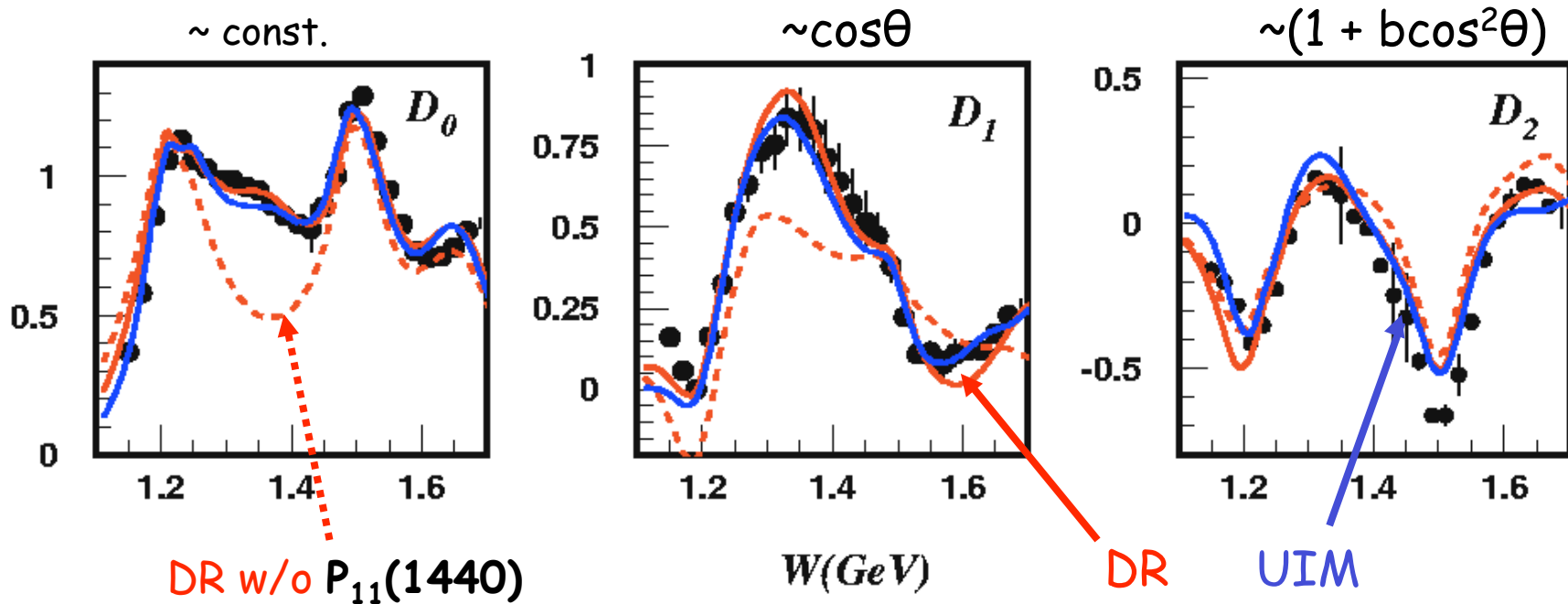
# Fits to diff. cross sections & structure functions



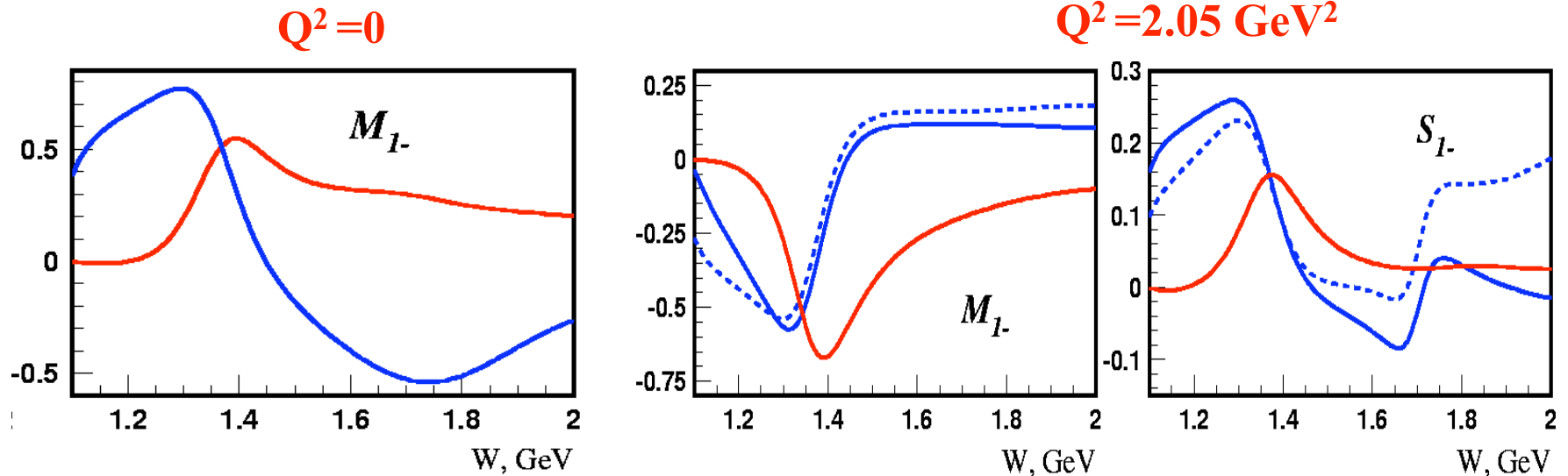
# Legendre moments for $\sigma_T + \epsilon\sigma_L$

$$\sigma_T + \epsilon\sigma_L = \sum_{l=0}^n D_l^{T+L} P_l(\cos\theta_\pi^*)$$

$$Q^2 = 2.05 \text{ GeV}^2$$



# Multipole amplitudes for $\gamma^* p \rightarrow \pi^+ n$



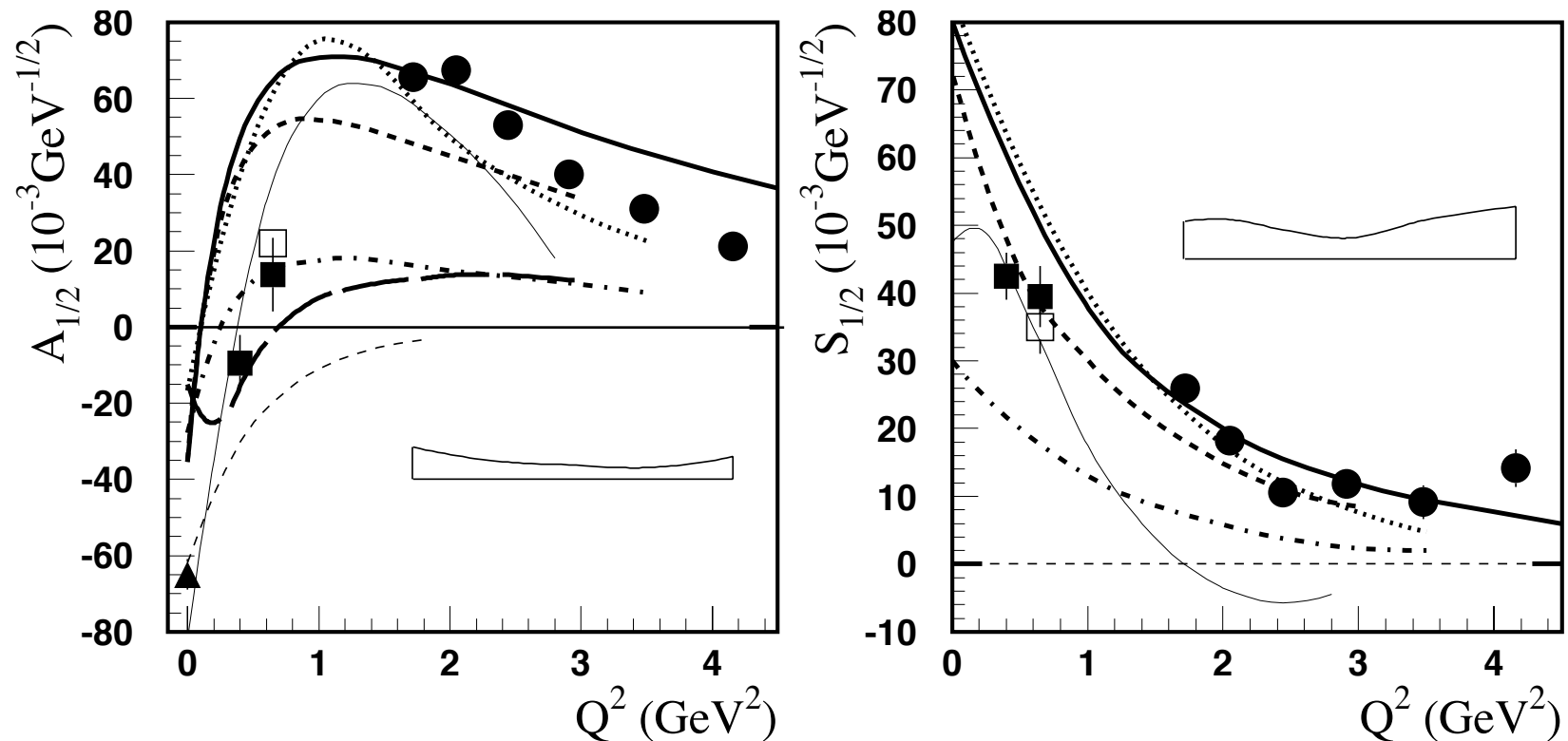
➤ At  $Q^2=1.7-4.2$ , resonance behavior is seen in these amplitudes more clearly than at  $Q^2 = 0$

➤ DR and UIM give close results for real parts of multipole amplitudes

Im ————  
 Re\_UIM ————  
 Re\_DR ······



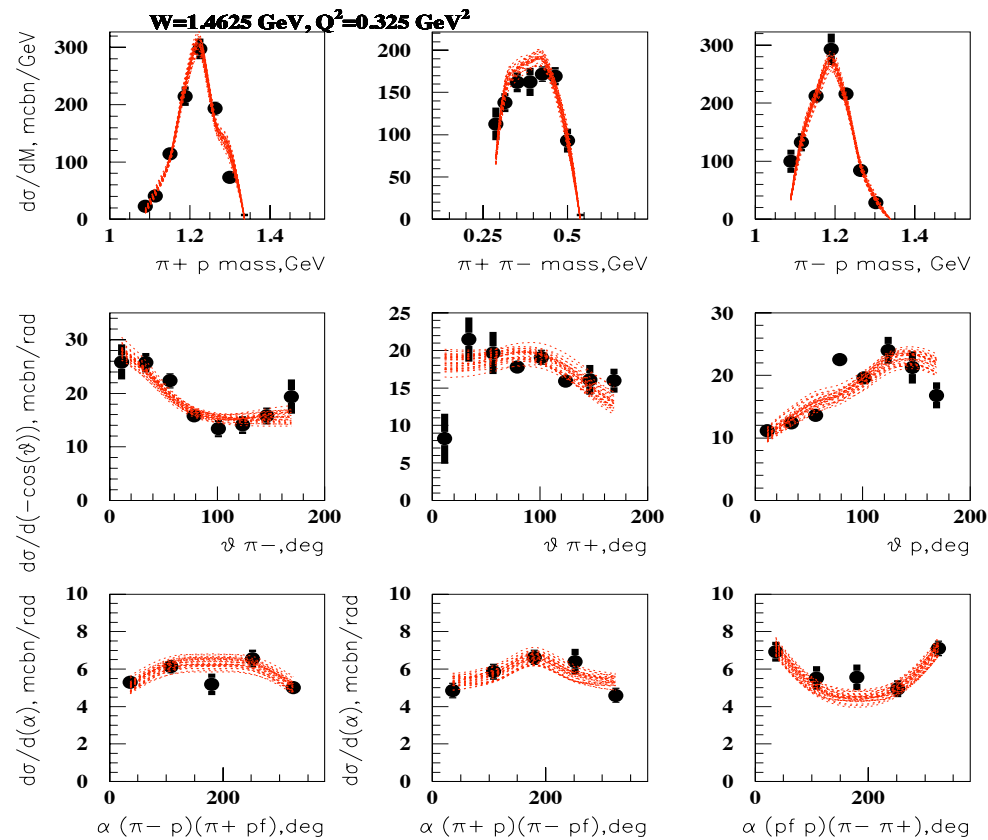
# Roper transition amplitudes from $N\pi$ data



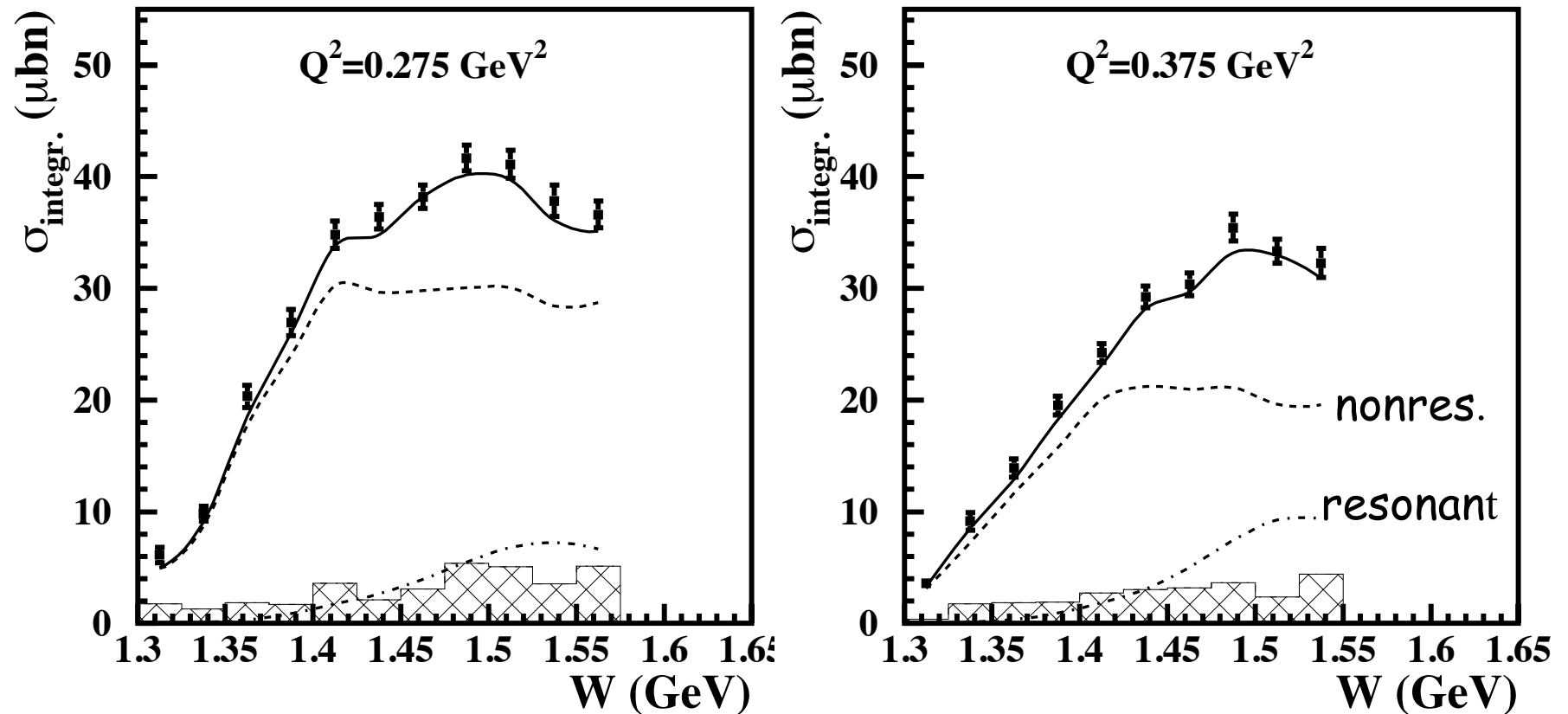
1. Weber, PR C41(1990)2783
2. Capstick..PRD51(1995)3598
3. Simula...PL B397 (1997)13
4. Riska..PRC69(2004)035212
5. Aznauryan, PRC76(2007)025212
6. Cano PL B431(1998)270

# JM06 Fit to $p(\gamma_\nu, p\pi^-\pi^+)$

Simultaneous fit to 9 one-dimensional integrated cross sections.

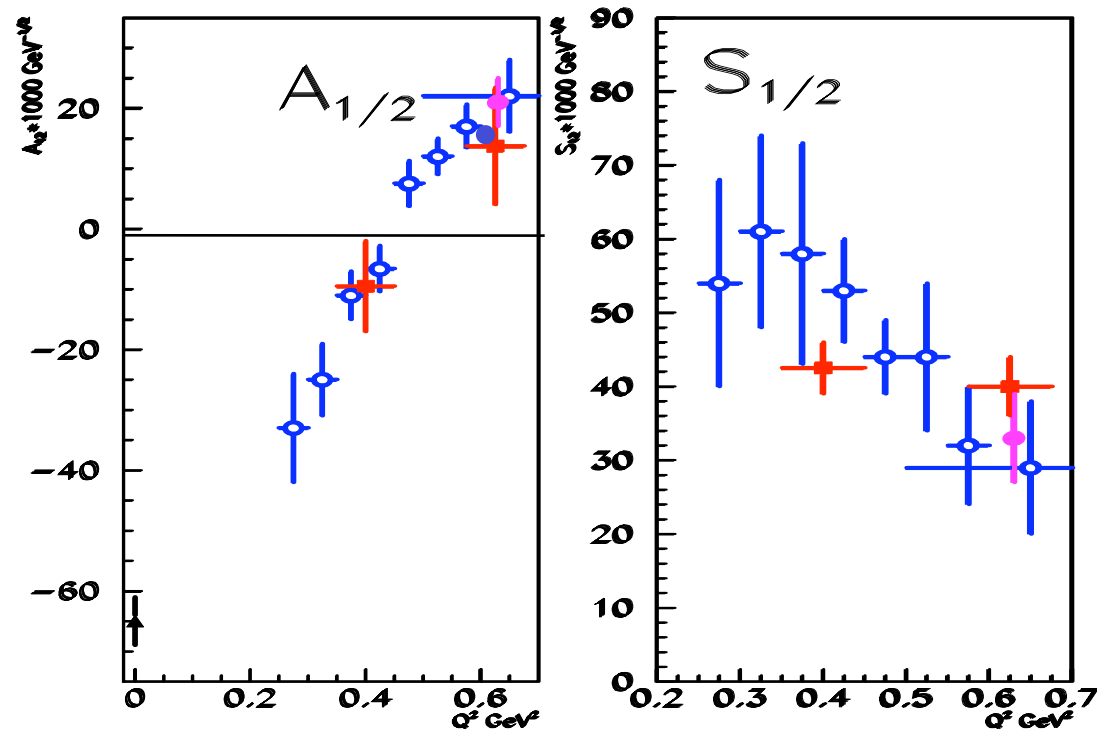


# Integrated cross sections for $p(\gamma_V, \rho\pi^+\pi^-)$



# $P_{11}(1440)$ amplitudes from $p\pi^+\pi^-$ data.

## $P_{11}(1440)$

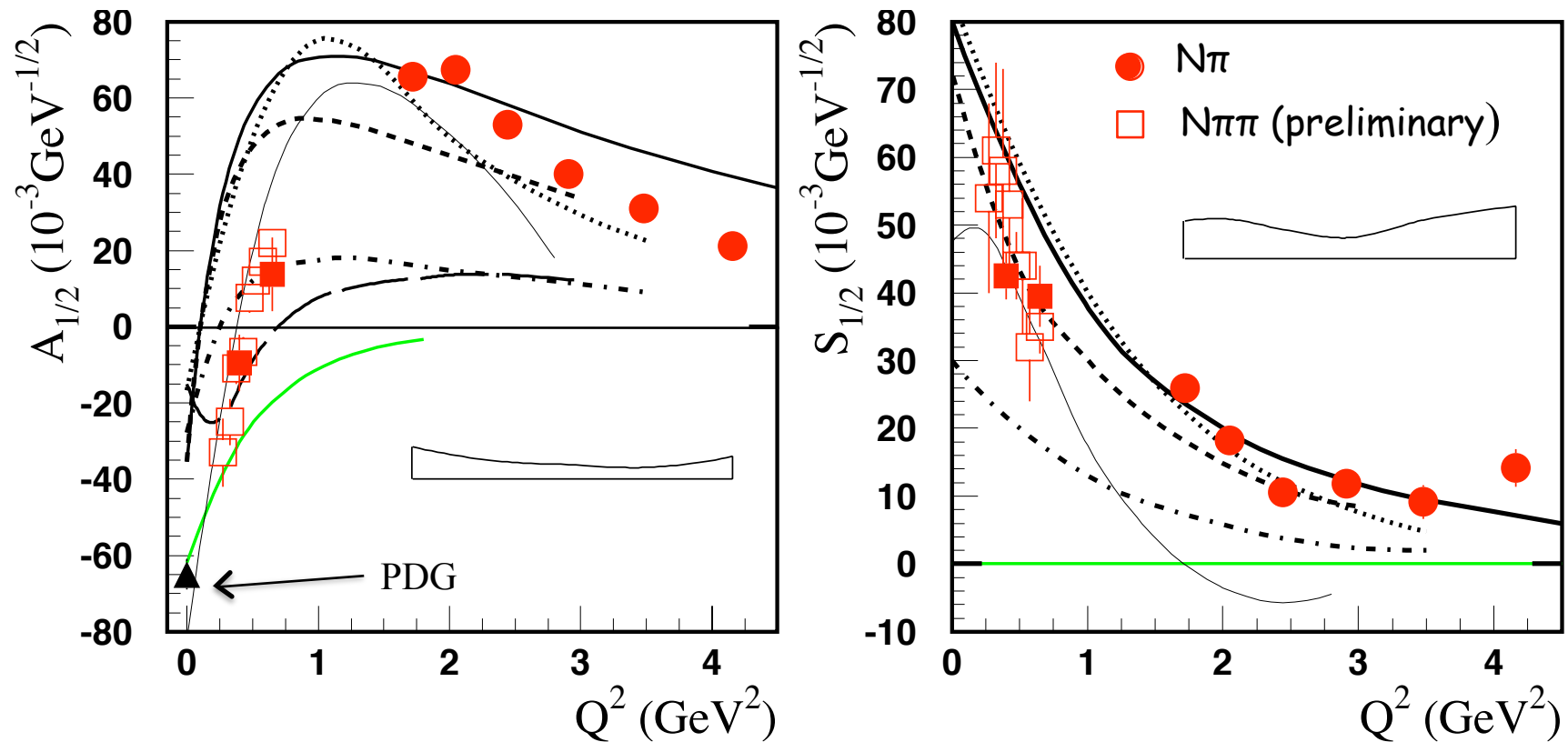


$\circ$  From  $N\pi\pi$  data (preliminary)

$\bullet$  From  $N\pi$  data

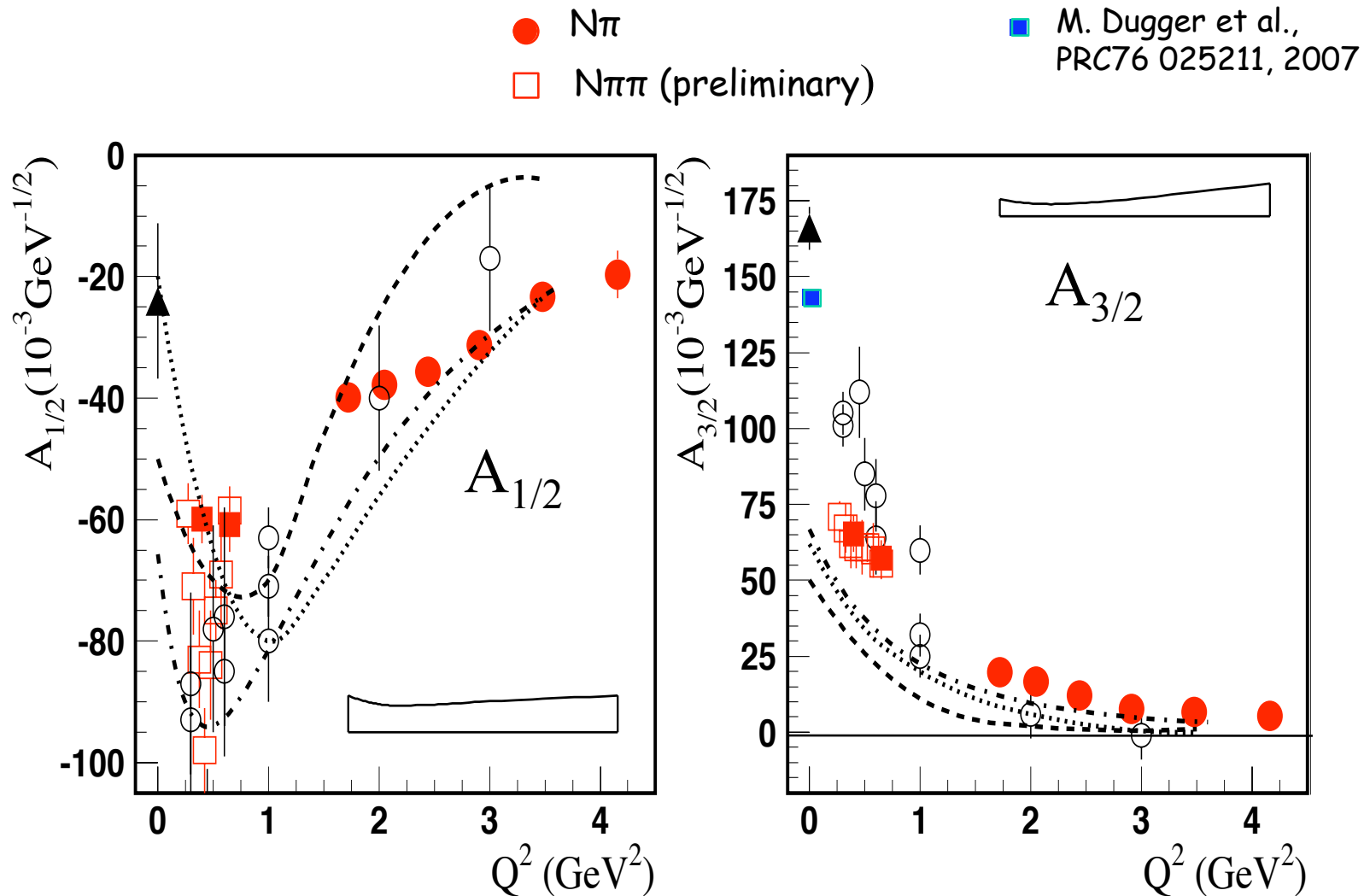
$\bullet$  Combined  $N\pi, N\pi\pi$  data

# $P_{11}(1440)$ amplitudes from $N\pi$ and $N\pi\pi$

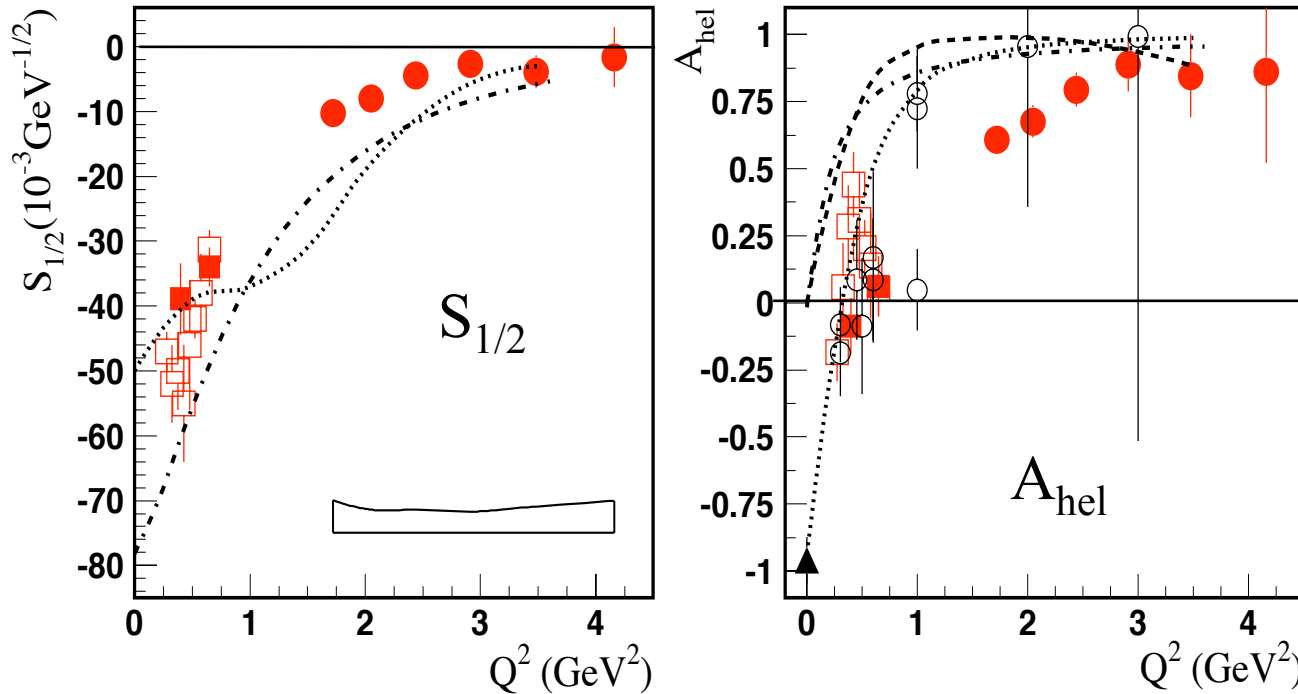


First observed zero crossing of a nucleon form factor!

# Transition amplitudes for $\gamma_v p D_{13}(1520)$

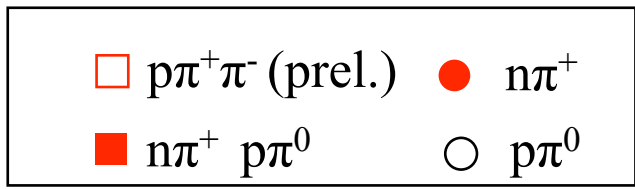


# Transition amplitudes for $\gamma_{\nu} p D_{13}(1520)$



$$A_{\text{hel}} = \frac{A_{1/2}^2 - A_{3/2}^2}{A_{1/2}^2 + A_{3/2}^2}$$

CQM predictions:  
 $A_{1/2}$  dominance with  
 increasing  $Q^2$ .



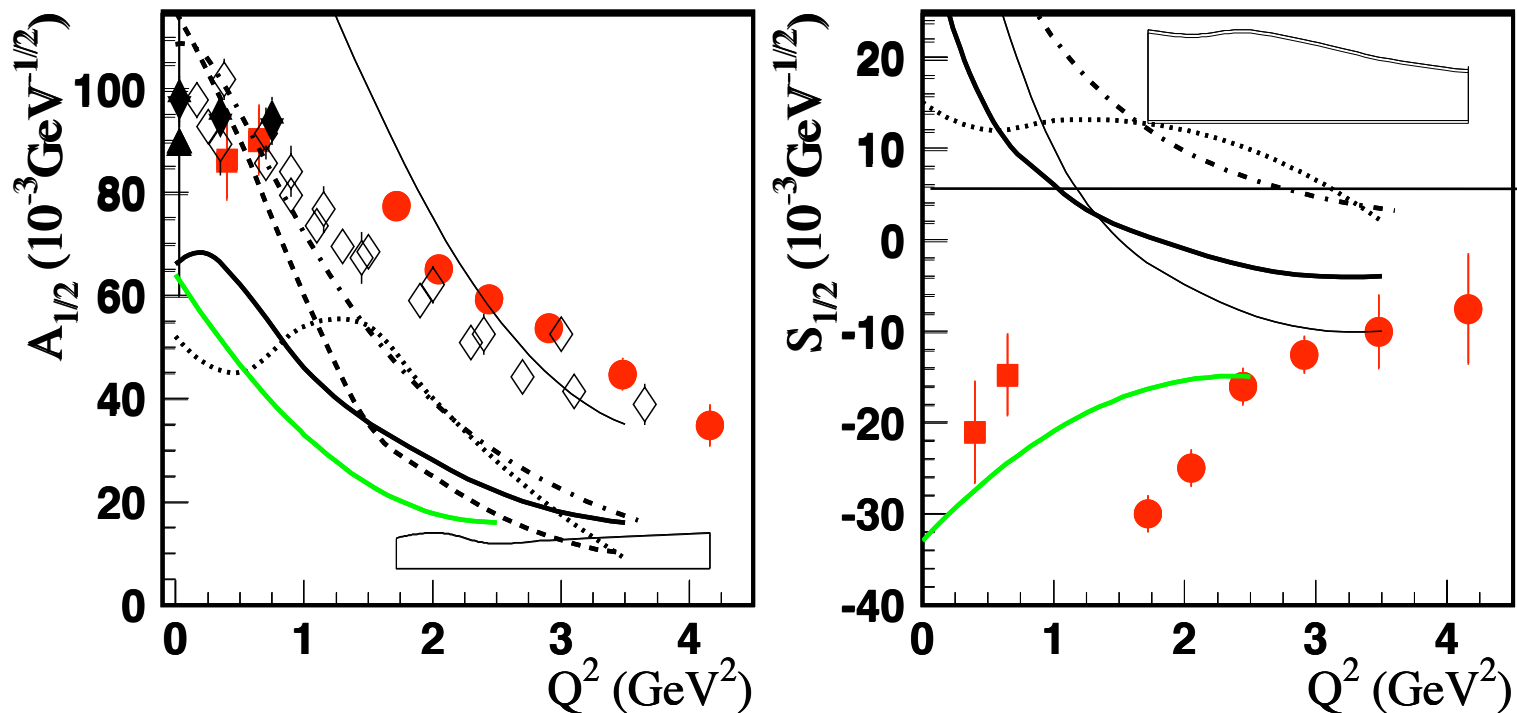
# The $S_{11}(1535)$

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- This state has traditionally been studied in the  $S_{11}(1535) \rightarrow p\eta$  channel, which a prominent decay.
  - $S_{11}(1535) \rightarrow p\eta$  ;  $p\eta$  selects isospin  $I=1/2$
  - $S_{11}(1535) \rightarrow N\pi$  ;  $N\pi$  sensitive to  $I=1/2, 3/2$
- For the study of  $S_{1/2}$   $N\pi$  channel is important.  $S_{1/2}$  difficult to extract in  $p\eta$  channel.



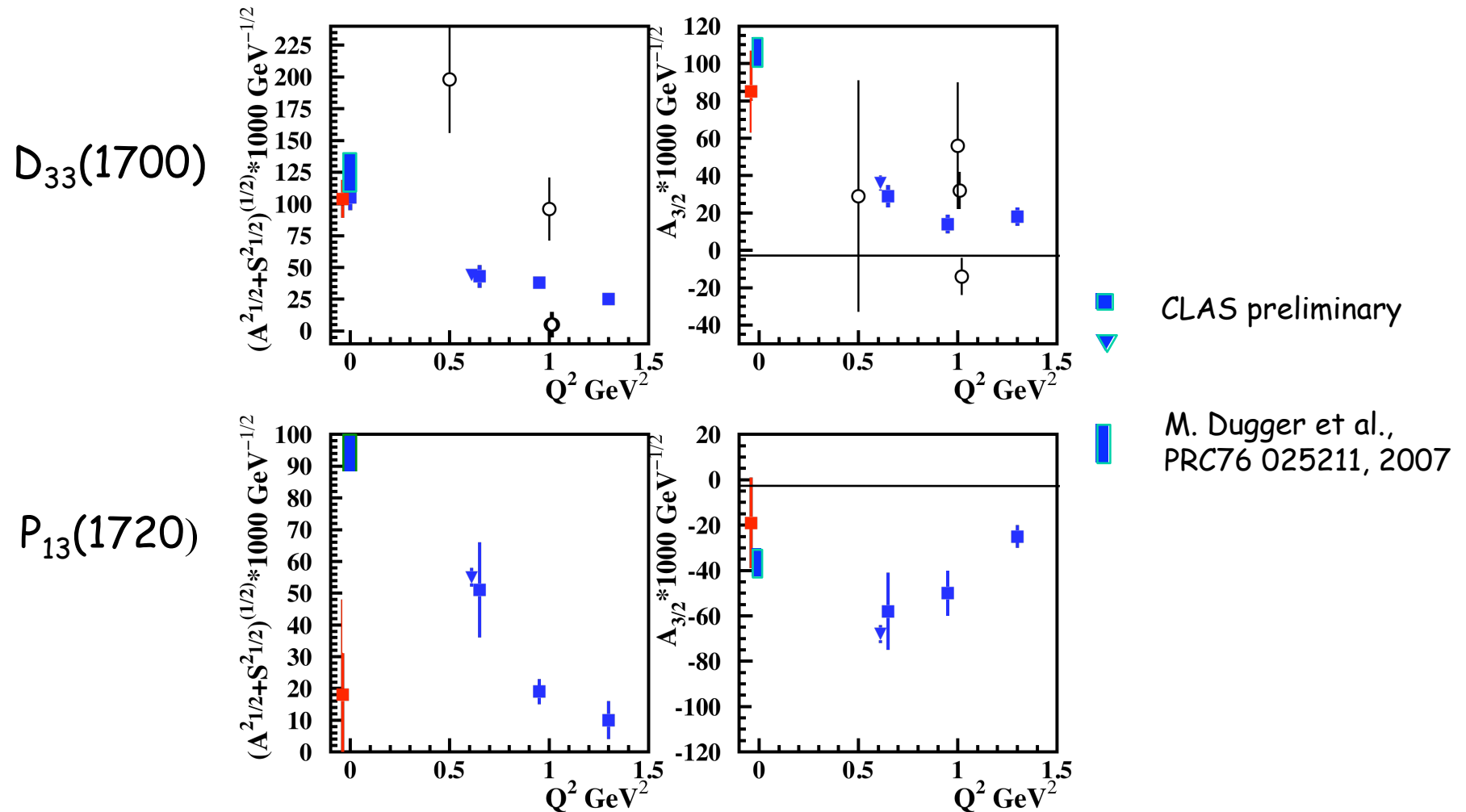
# Transition amplitudes for $S_{11}(1535)$



- $A_{1/2}$  from  $n\pi^+$  consistent with  $p\eta$  within uncertainties of b.r.
- In  $n\pi^+$  the  $S_{0+}$  amplitude interferes with the strong  $M_{1-}$  allowing access to the longitudinal coupling.  $D_0^{LT} \sim \text{Re}(E_{0+}S_{1-}^* + S_{0+}M_{1-}^*)$ .
- Sign not consistent with CQM, but agrees with dynamically generated resonance prediction.

This may indicate that CQM's must take into account meson cloud to reproduce sign of  $S_{1/2}$ , see: B. Julia-Diaz, et.al. (EBAC), Phys. Rev. C77:045205(2008).

# Transition amplitudes for $D_{33}(1700)$ , $P_{13}(1720)$



# Conclusions & Outlook

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- $N\Delta(1232)$  amplitudes are well determined at  $Q^2$  up to  $6 \text{ GeV}^2$ .
  - No sign of transition to asymptotic QCD behavior
- Roper  $P_{11}(1440)$  amplitudes determined up to  $4.5 \text{ GeV}^2$  using two different analysis approaches (DR, UIM), and two channels
  - Sign change of  $A_{1/2}$  seen in  $N\pi$  and  $N\pi\pi$
  - High  $Q^2$  behavior consistent with radial excitation of the nucleon as in CQM
- $S_{11}(1535)$  amplitudes measured in  $n\pi^+$  channel, for the first time
  - Hard  $A_{1/2}$  form factor confirmed
  - First measurement of  $S_{1/2}$ . Sign inconsistent with CQM, consistent with dynamically generated state
- $D_{13}(1520)$  in  $n\pi^+$  and  $p\pi^+\pi^-$ 
  - Helicity switch from  $A_{3/2}$  dominance to  $A_{1/2}$  dominance at  $Q^2 > 0.6 \text{ GeV}^2$
- $P_{13}(1720)$  and  $D_{33}(1700)$  in  $p\pi^+\pi^-$ 
  - the first consistent mapping of their  $Q^2$  dependence

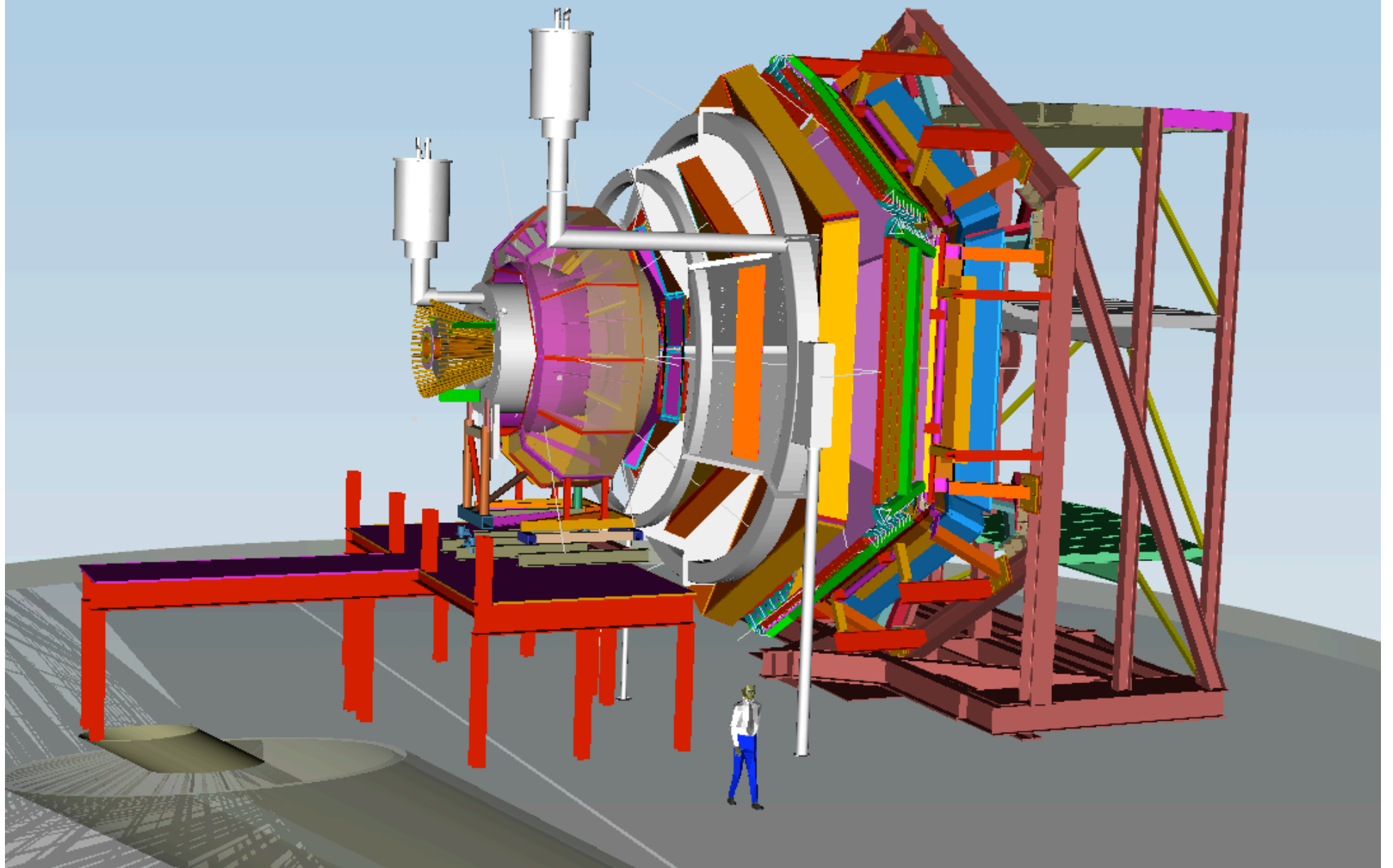
# Future prospects of $N^*$ Physics at the JLab

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- Hall C data on  $N\Delta$  at high  $Q^2$  expected soon
- New data on  $Q^2$  dependence of high mass states (CLAS)
- An experiment is planned in Hall A to study  $N\Delta$  at very low  $Q^2$
- An extensive program is underway with polarized photon beams and polarized targets to search for new baryon states (CLAS)
- Large effort underway at EBAC to develop the coupled channel analysis of these and other data
- Proposal for a transition form factor program at high  $Q^2$  for the JLab 12 GeV upgrade with CLAS12

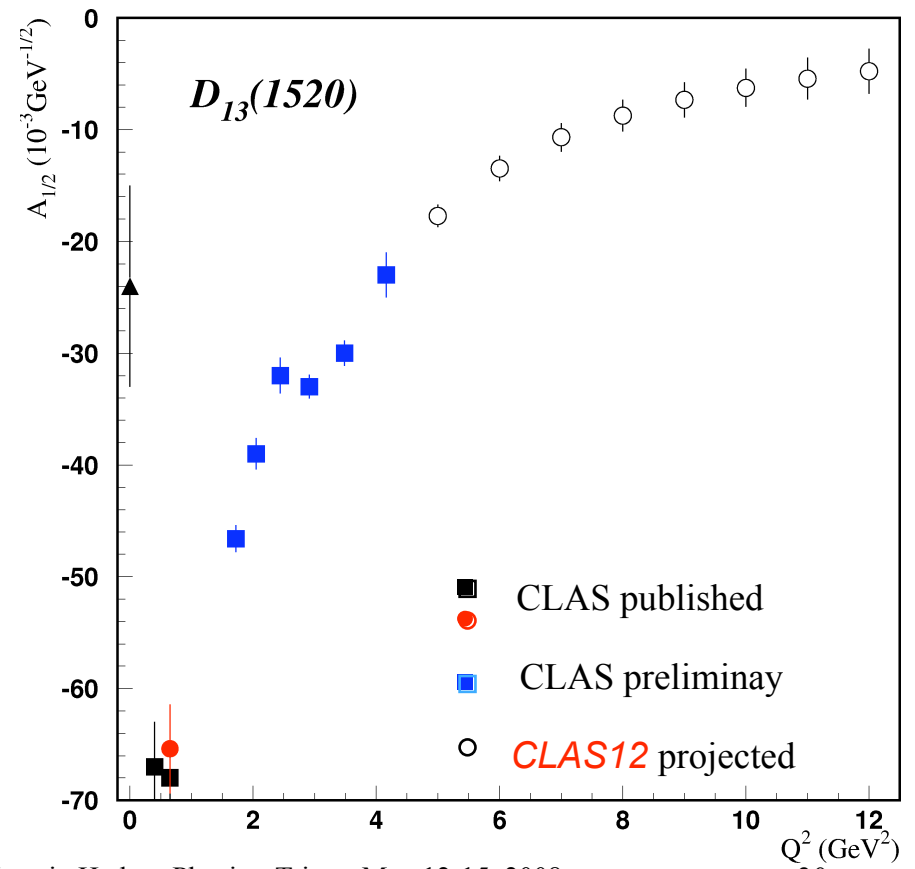
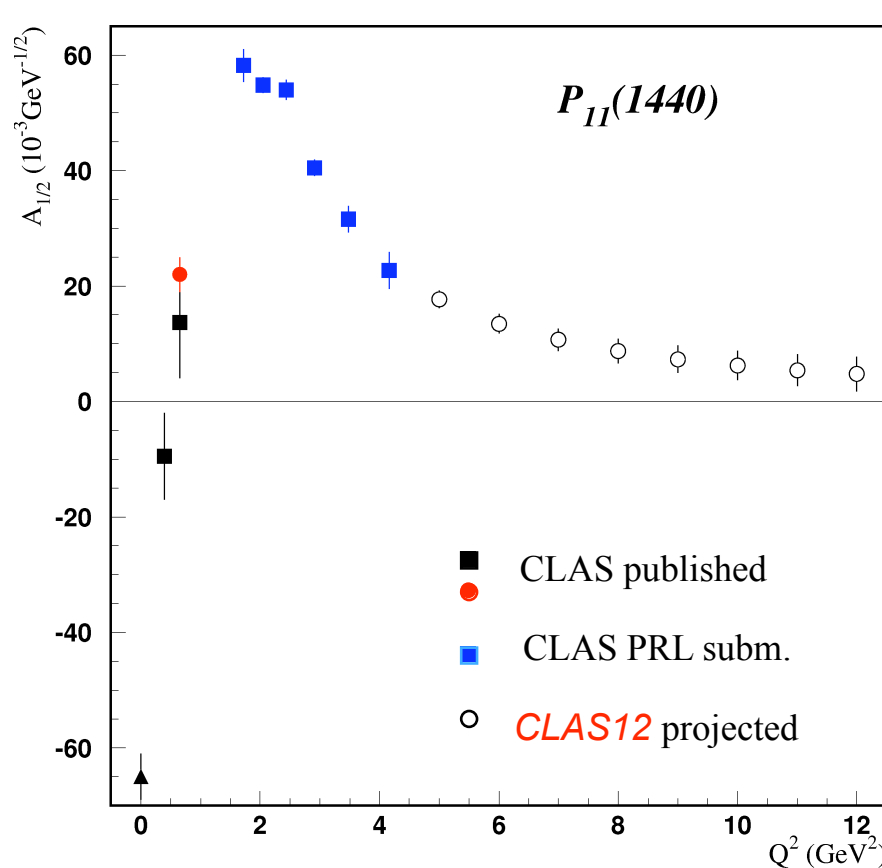
# CLAS12 - Detector

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# Projections for $N^*$ Transition Amplitudes @ 12 GeV

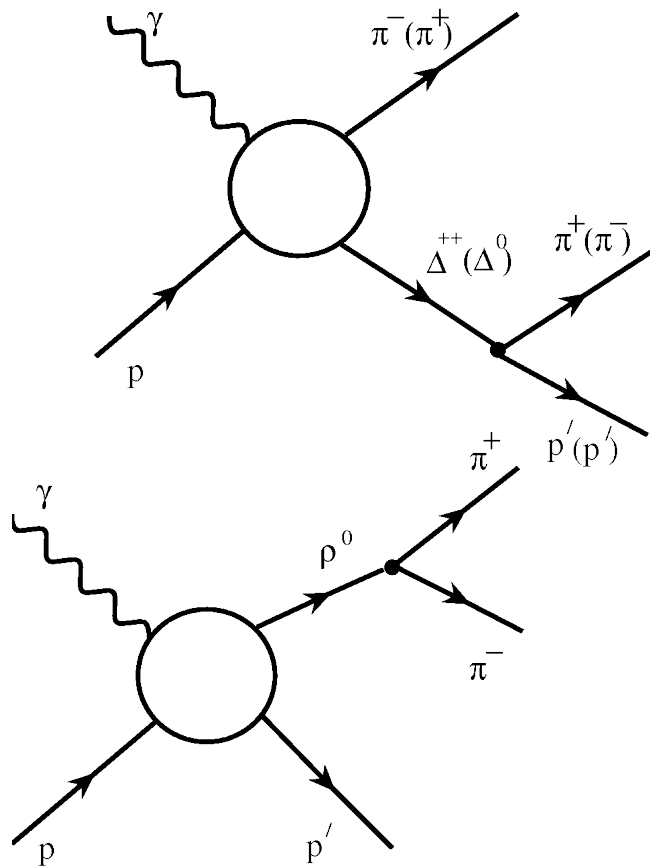
Probe the transition from effective degrees of freedom, e.g. constituent quarks, to elementary quarks, with characteristic  $Q^2$  dependence.



# Additional Slides

# JLAB-MSU model (JM06) for $2\pi$ electroproduction.

## 3-body processes:



## Isobar channels included:

$\pi\Delta^{++}$

- All well established  $N^*$  with  $\pi\Delta$  decays and  $3/2^+(1720)$  candidate, seen in CLAS  $2\pi$  data.

- Reggetized Born terms & effective FSI&ISI treatment .

- Extra  $\pi\Delta$  contact term.

$\rho\rho$

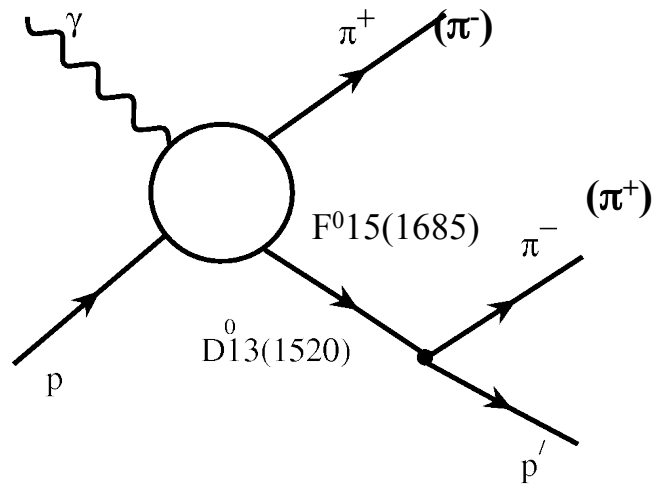
- All well established  $N^*$  with  $\rho\rho$  decays and  $3/2^+(1720)$  candidate.

- Diffractive ansatz for non-resonant part &  $\rho$ -line shrinkage in  $N^*$  region.



# JM06 Model, cont'd

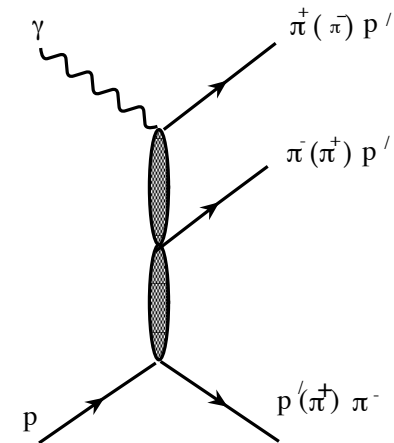
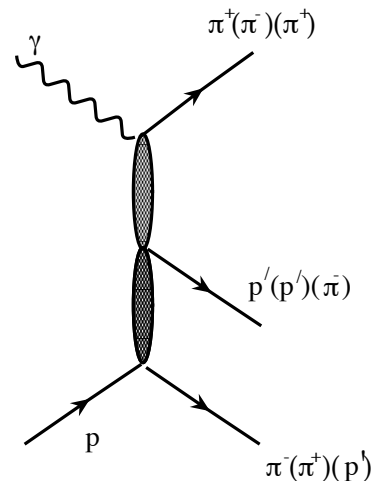
## 3-body processes:



## Direct 2π production

## Isobar channels included:

- $\pi^+ D_{13}^0(1520)$ ,  $\pi^+ F_{15}^0(1685)$  isobar channels.



V.Mokeev, et al., J. Phys. 69, 012019 (2007).