

# Wide-angle exclusive scattering

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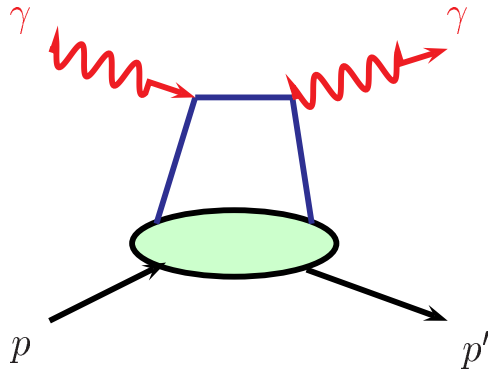
Outline:

- Factorization schemes
- The handbag contribution to WACS
- Extracting the GPDs from nucleon form factors
- Results on Compton scattering
- Summary

based on work done in collaboration with: [M. Diehl](#), [T. Feldmann](#), [R. Jakob](#)

# Handbag factorization in excl. reactions

D. Müller et al (94), Ji(97), Radyushkin (97)



only one active parton (others are spectators)

occur in

DVES (  $\gamma^* p \rightarrow \gamma p, Mp$  )  $Q^2$  large,  $t$  small

WAES (  $\gamma p \rightarrow \gamma p, Mp$  )  $Q^2$  small,  $t$  large

hard process:  $\gamma^{(*)} q \rightarrow \gamma q$

soft physics: GPDs  $H^q(x, \xi, t)$ ,  $\tilde{H}^q$ ,  $E^q$ ,  $\tilde{E}^q$  (skewness:  $\xi = \frac{p^+ - p'^+}{p^+ + p'^+}$ )

• reduction formulas:  $H^q(x, 0; 0) = q(x)$ ;  $\tilde{H}^q(x, 0; 0) = \Delta q(x)$

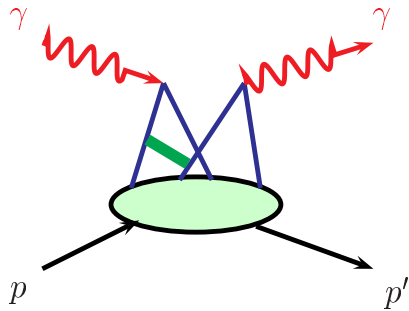
• sum rules:  $h_{10}^q(t) = \int_{-1}^1 dx H^q(x, \xi, t)$ ;  $F_1(t) = \sum_q e_q h_{10}^q(t)$ ;  
 $E^q \rightarrow F_2^q$ ;  $\tilde{H}^q \rightarrow F_A^q$ ;  $\tilde{E}^q \rightarrow F_P^q$

• polynomiality: e.g.  $\int_{-1}^1 dx x^{n-1} H^q(x, \xi, t) = \sum_{i=0}^{[n/2]} h_{n,i}^q(t) \xi^i$

universality, evolution, positivity constraints, Ji's sum rule

# Other topologies

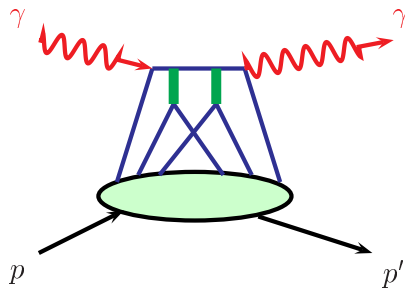
Two active partons



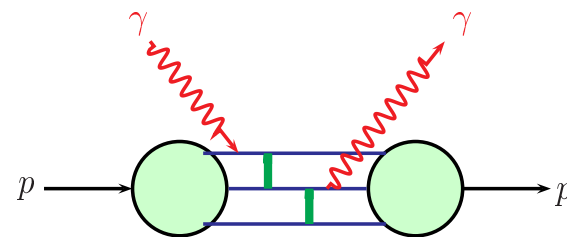
cat's ears

large virtualities or large intrinsic transverse momenta occur in diagram  
at least **one hard gluon** is required  
**expected to be suppressed**

Three active partons



valence quark apprx. (blob decays into two)



at least

two hard gluons required

**Brodsky-Lepage factorization** (leading twist)

hard process:  $\gamma qq \rightarrow \gamma qq$ , soft physics: DA  $\Phi_p = \Phi_p(x_1, x_2, x_3)$

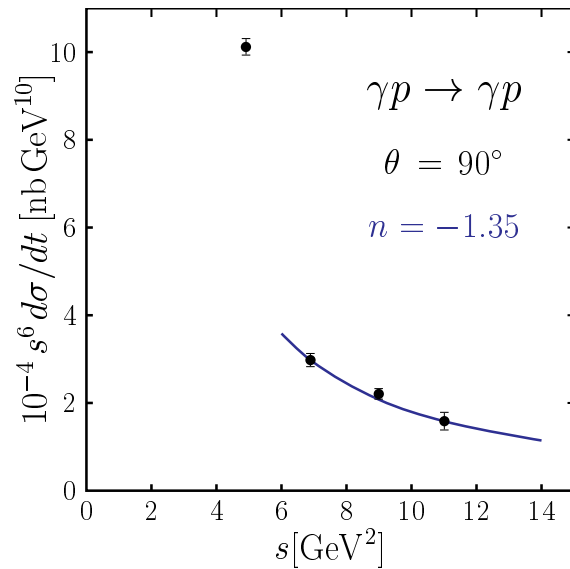
asymptotically dominant, handbag formally a power correction

**strongly suppressed** for  $t$  of order of  $10 \text{ GeV}^2$  ( $10^{-2} - 10^{-3}$ )

onset of leading-twist region probably above  $-t(-u) > 100 \text{ GeV}^2$

# Dimensional counting

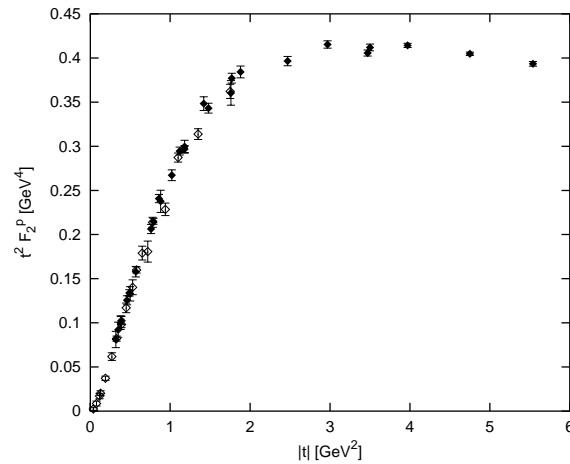
Matveev et al; Brodsky-Farrar  $\mathcal{O} \propto \frac{\Psi_1 \cdots \Psi_m}{Q^{n(m)}} \quad (+\text{pert. logs}) \quad \text{for } Q^2 \rightarrow \infty$



$$d\sigma/dt(\gamma p \rightarrow \gamma p, \theta \text{ fixed}) \sim s^{-(7 \dots 8)} \quad s^{-6}$$

$$F_2^p(t) \sim t^{-2} \quad t^{-3}$$

$$F_1^d(t) \sim t^{-3} \quad t^{-2}$$

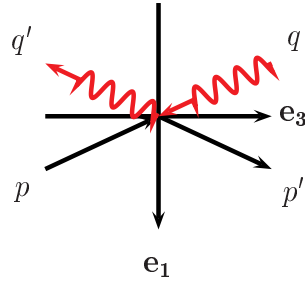
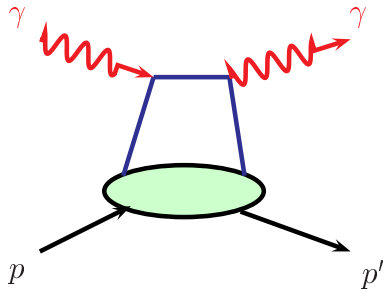


$$\sigma(\gamma\gamma \rightarrow p\bar{p}) \sim s^{-7.2} \quad s^{-5}$$

$$\sigma(\gamma\gamma \rightarrow \pi^+\pi^-) \sim s^{-3.95} \quad s^{-3}$$

$$\sigma(\gamma\gamma \rightarrow K^+K^-) \sim s^{-3.65} \quad s^{-3}$$

# The handbag contribution to WACS



$$s, -t, -u \gg \Lambda^2$$

$$\Lambda \sim \mathcal{O}(1\text{GeV})$$

typical hadronic scale

- work in a symmetric frame:

$$p^{(\prime)} = [p^+, \frac{m^2 - t/4}{2p^+}, \pm \Delta_{\perp}] \quad \xi = \frac{(p-p')^+}{(p+p')^+} = 0 \quad t = -\Delta_{\perp}^2$$

- assumption of soft contribution:

parton virtualities  $k_i^2 < \Lambda^2$  , intrinsic transverse momenta  $k_{\perp i}^2/x_i < \Lambda^2$

- consequences

$$\begin{aligned} \hat{s} &= (k_j + q)^2 \simeq (p + q)^2 = s && \text{propagators poles avoided} \\ \hat{u} &= (k_j - q')^2 \simeq (p - q')^2 = u && \text{active partons approximately on-shell} \\ &&& \text{collinear with parent hadrons} \\ &&& \text{and } x_j, x'_j \simeq 1 \end{aligned}$$

- physical situation: hard photon-parton scattering and soft emission and reabsorption of partons by hadrons

# The Compton amplitudes

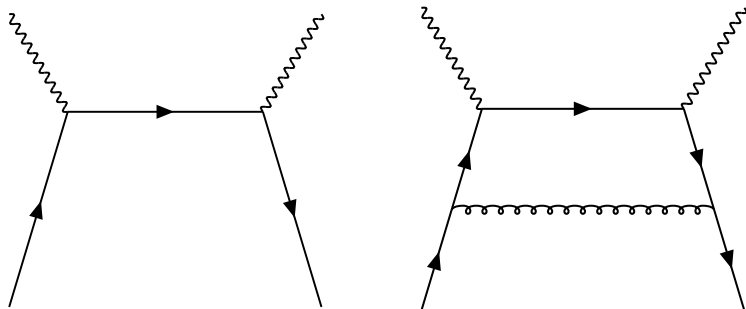
$$\mathcal{M}_{\mu'+,\mu+} = 2\pi\alpha_{elm} \left\{ \mathcal{H}_{\mu'+,\mu+} [R_V + R_A] + \mathcal{H}_{\mu'-,\mu-} [R_V - R_A] \right\}$$

$$\mathcal{M}_{\mu'-,\mu+} = -\pi\alpha_{elm} \frac{\sqrt{-t}}{m} \left\{ \mathcal{H}_{\mu'+,\mu+} + \mathcal{H}_{\mu'-,\mu-} \right\} R_T$$

$$R_V(t) = \sum_q e_q^2 \int_0^1 \frac{dx}{x} H_v^q(x, t), \quad \tilde{H}_v^q \Rightarrow R_A, \quad E_v^q \Rightarrow R_T^q$$

$$\tilde{E} \text{ decouples at } \xi = 0, \quad H_v = H^q - H^{\bar{q}} \quad (\text{sea quarks neglected})$$

$\mathcal{H}(s, t)$ : NLO  $\gamma q \rightarrow \gamma q$  amplitudes (+  $\gamma g \rightarrow \gamma g$ ,  $R_i^g$ )



Radyushkin hep-ph/9803316

DFJK hep-ph/9811253

Huang-K-Morii hep-ph/0110208

# GPD analysis - what can be done?

DFJK hep-ph/0408173 (similar Guidal et al hep-ph/0410251)  
analogue to PDF analyses

use **all** available data on  $G_M^p, G_M^n, G_E^p, G_E^n (\Rightarrow F_1^p, F_1^n, F_2^p, F_2^n), F_A$

exploit sum rules at  $\xi = 0$

$$F_1^{p(n)}(t) = \int_0^1 dx \left[ e_{u(d)} H_v^u(x, t) + e_{d(u)} H_v^d(x, t) \right] \quad F_2 \Rightarrow E_v$$

$$F_A(t) = \int_0^1 dx \left[ \tilde{H}_v^u(x, t) - \tilde{H}_v^d(x, t) \right] + 2 \int_0^1 dx \left[ \tilde{H}^{\bar{u}}(x, t) - \tilde{H}^{\bar{d}}(x, t) \right]$$

$$H_v = H^q - H^{\bar{q}}$$

$s - \bar{s}, c - \bar{c}$  and sea quark contribution to  $F_A$  neglected, probably very small  
in order to determine  $H_v^{u,d}, \tilde{H}_v^{u,d}, E_v^{u,d}$

in a strict mathematical sense an ill-posed problem

**BUT**

# Motivation of the ansatz for GPDs

**ANSATZ:**  $H_v^q(x, t) = q_v(x) \exp [f_q(x)t]$   
 $f_q = [\alpha' \log(1/x) + B_q] (1 - x)^{n+1} + A_q x(1 - x)^n$   
 $\alpha' = 0.9 \text{ GeV}^{-2}$  (fixed)  $n = 1, 2$  (favored, confinement)  
 $q_v(x)$  from CTEQ (**INPUT**)

Motivation:

for large  $-t$  and  $x$ : overlaps of Gaussian LC wavefunctions

$$H_v^q(x, t) \rightarrow \exp \left[ a^2 t \frac{1-x}{2x} \right] q_v(x)$$

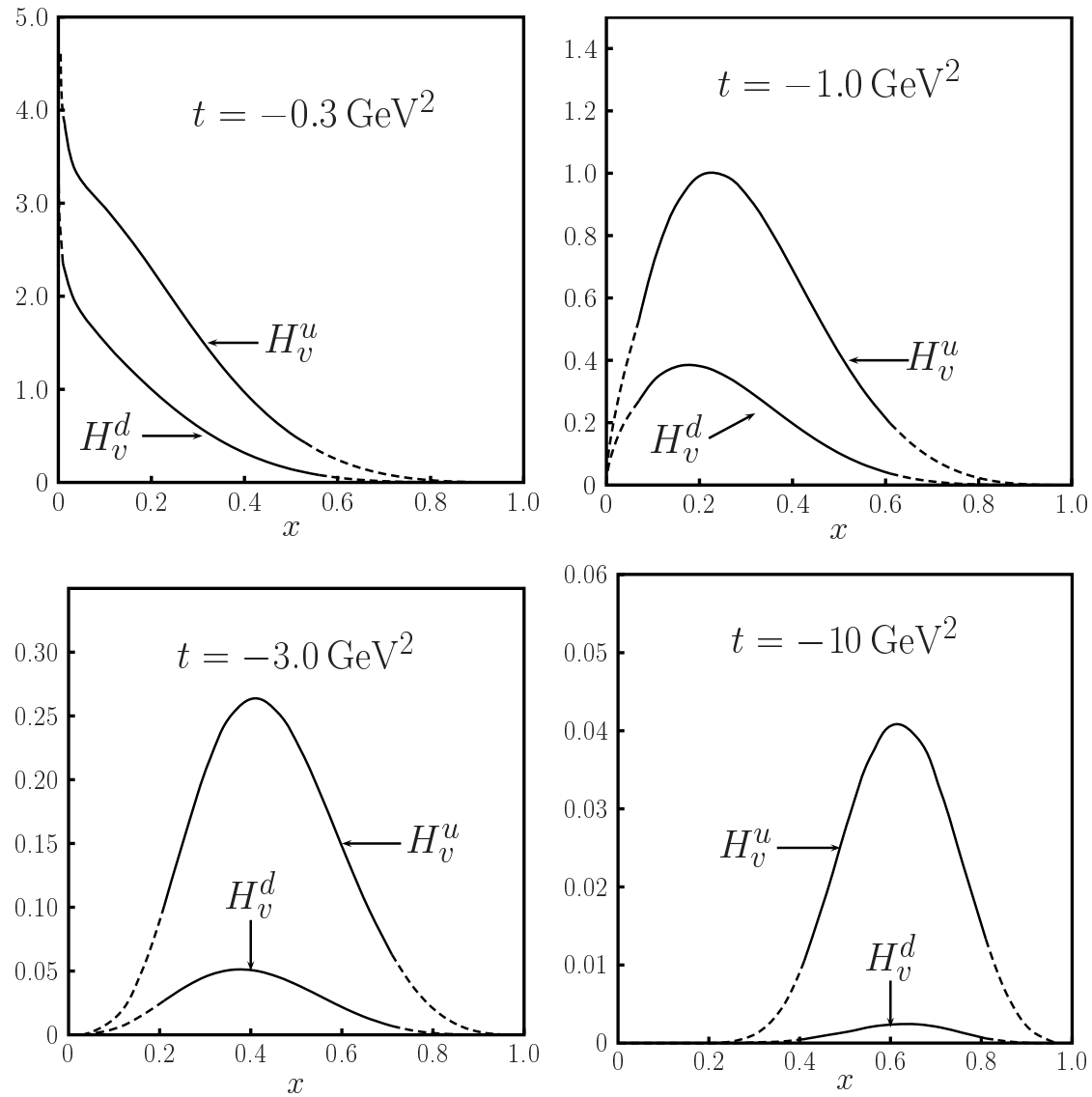
low  $-t$ , very small  $x$ : Regge behaviour expected

$$H_v^q(x, t) \rightarrow x^{-\alpha(0)} \exp [\alpha' t \log(1/x)]$$

criteria for good parameterization (met by ansatz):

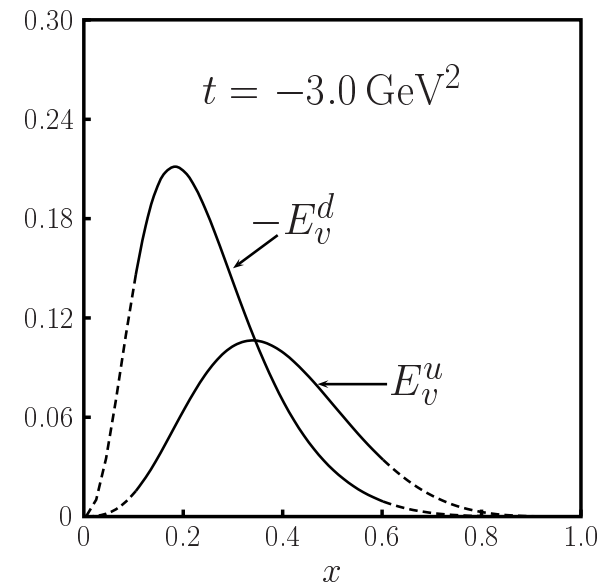
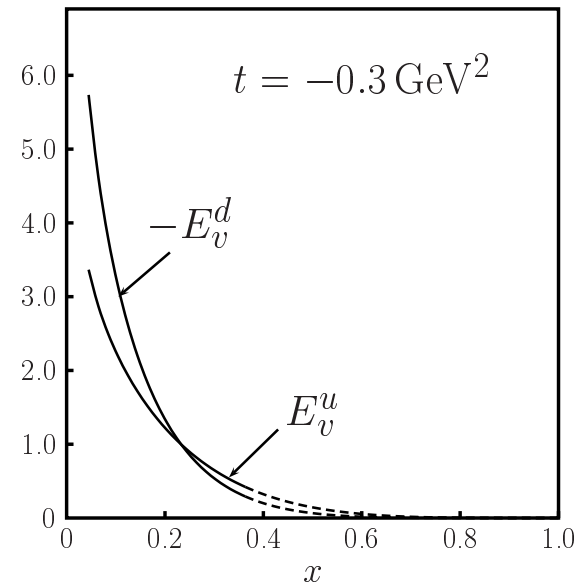
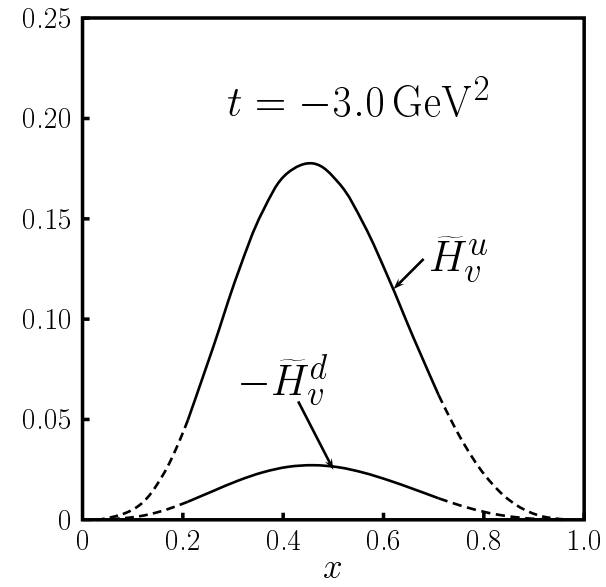
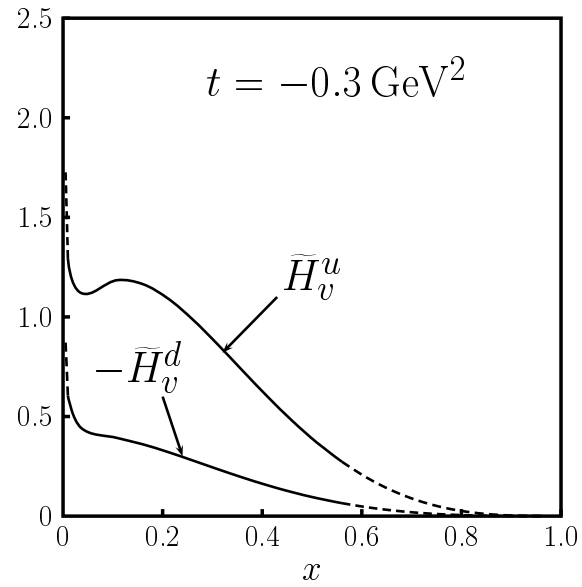
- simplicity
- consistency with theor. and phenom. constraints
- plausible interpretation of parameters (if possible)
- stability with respect to variation of PDFs
- stability under evolution (scale dependence of GPDs can be absorbed into parameters)

# The GPD $H$ ( $\mu = 2 \text{ GeV}$ )



at large  $t$  only a narrow range of large  $x$  contributes to sum rule

# The GPDs $\widetilde{H}$ , $E$ ( $\mu = 2 \text{ GeV}$ )



# Feynman mechanism

$k, k'$  momenta of active parton (before and after it is struck)

$l$  momentum of spectator system;  $\Lambda$  typical hadronic scale

**soft region:**  $1 - x \sim \Lambda/\sqrt{|t|}$ ,  $|k^2|, |k'^2| \sim \Lambda\sqrt{|t|}$       Feynman mechanism applies

**ultrasoft:**  $1 - x \sim \Lambda/|t|$ ,  $|k^2|, |k'^2| \sim \Lambda^2$

large  $t \Leftrightarrow$  large  $x$ : approx.:  $q_v \sim (1 - x)^{\beta_q}$ ,  $f_q \sim A_q(1 - x)^n$

Saddle point method:  $1 - x_s = \left(\frac{n}{\beta_q} A_q |t|\right)^{-1/n}$ ,  $h_{1,0}^q \sim |t|^{-(1+\beta_q)/n}$

(similar to Drell-Yan)

$n = 2$ :  $x_s$  in soft region and in sensitive  $x$ -region  $\Rightarrow$  early onset of power beh. ( $t \simeq 5 \text{ GeV}^2$ )

$n = 1$ :  $x_s$  in ultrasoft region (suspect - confinement!)

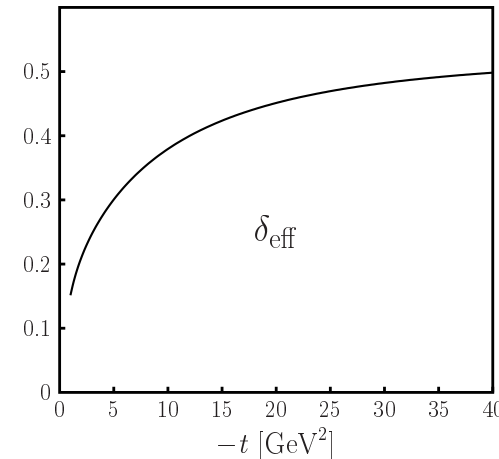
requires large  $t$  in order to have  $x_s$  in sensitive region

power behaviour of  $h_{1,0}^q$  does not set in before

$-t \simeq 30 \text{ GeV}^2$

Testing the power laws:

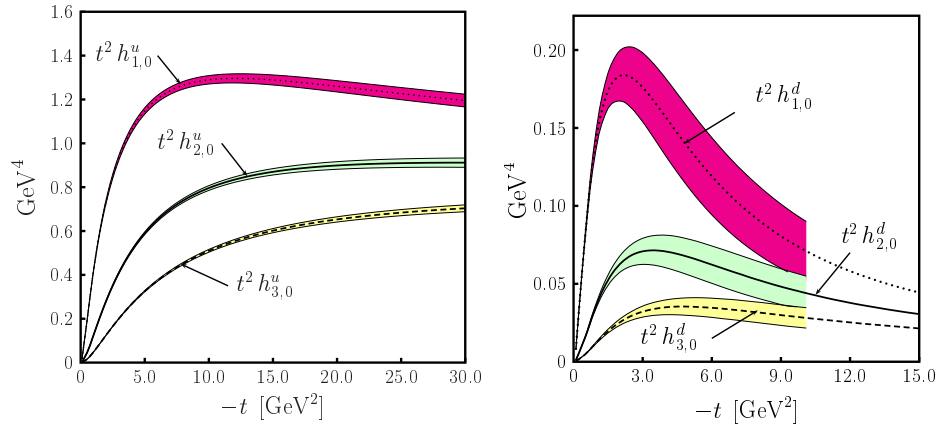
**eff. power**  $\delta_{\text{eff}} = t \frac{d}{dt} \log[1 - \langle x \rangle_t]$



**soft region:**  $\delta_{\text{eff}} = 1/2$       **ultrasoft:**  $\delta_{\text{eff}} = 1$        $n = 1, 2$  practically same  $\delta_{\text{eff}}$  in fit

fit implies dominance of Feynman mechanism

# Moments



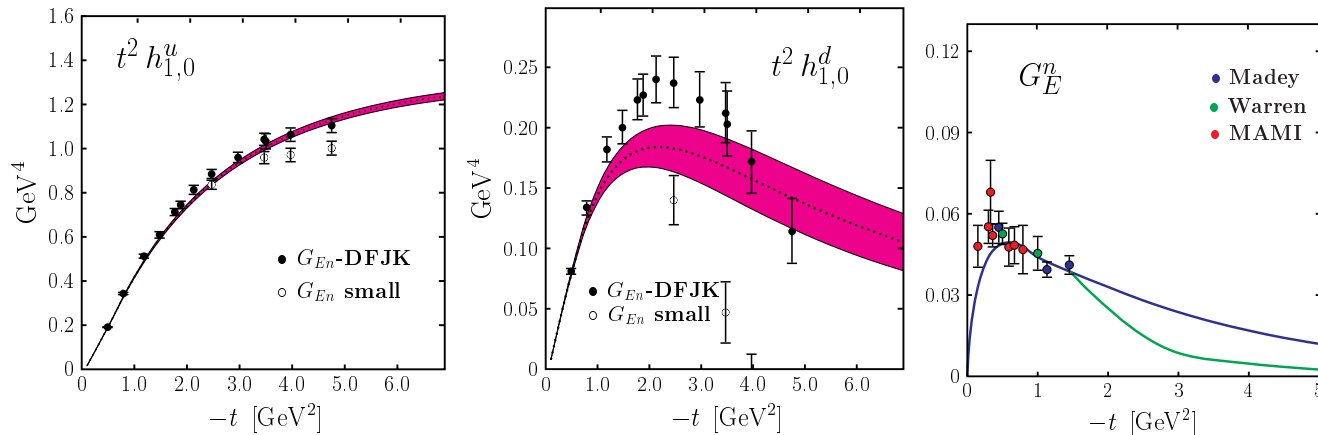
$$h_{1,0}^q \sim |t|^{-(1+\beta_q)/n}$$

CTEQ PDFs:

$$\beta_u \simeq 3.4, \beta_d \simeq 5$$

dimensional counting?

'pQCD'?

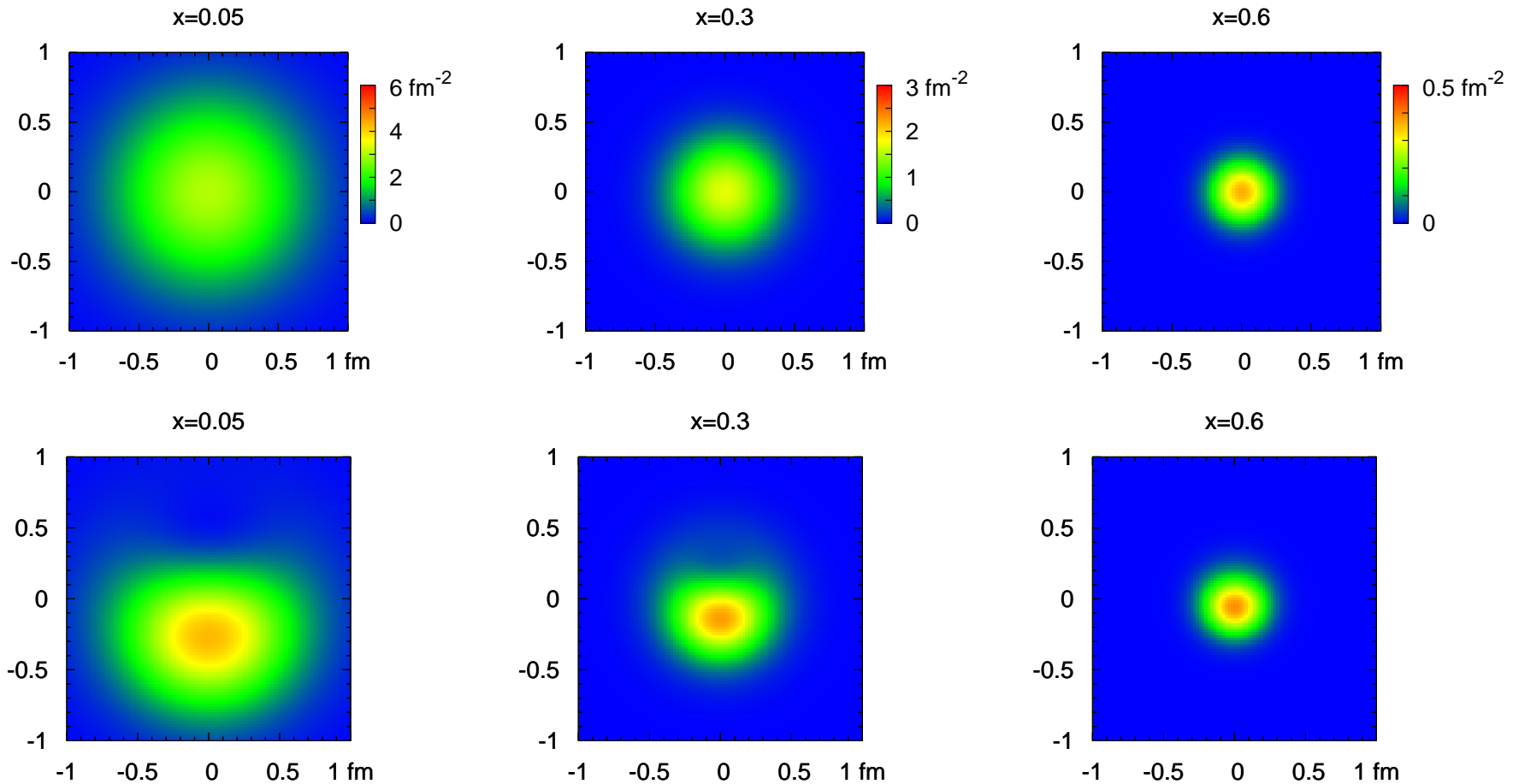


(preliminary CLAS data on  $G_M^n$  used)

dominance of  $u$  over  $d$  in FF at large  $t$  corresponds to that in PDFs at large  $x$

except  $G_E^n$  is much larger than expected wait for JLab

# Tomography of $d_v$ quarks



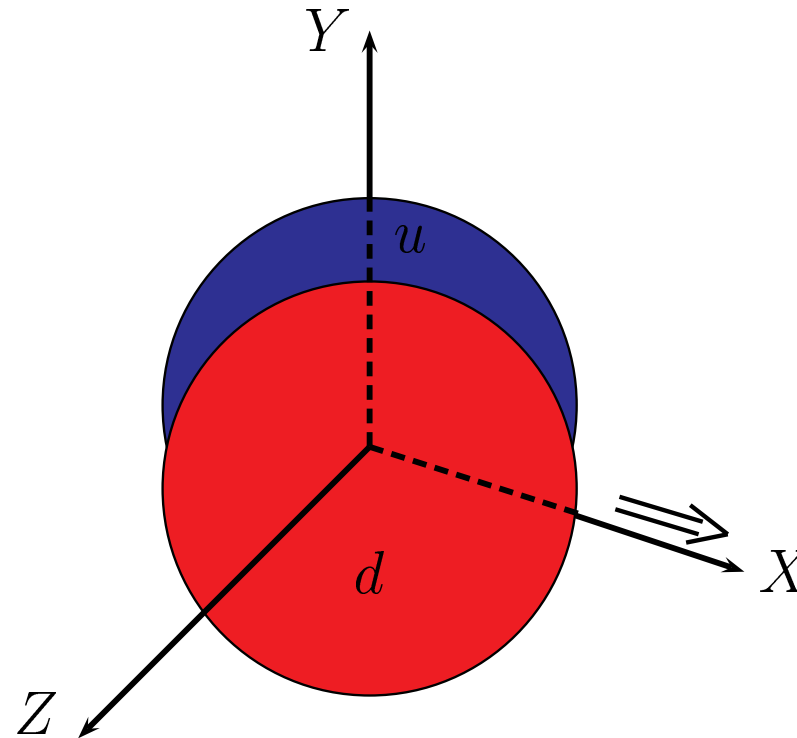
Fourier transform, e.g.:  $q(x, \xi, \mathbf{b}) = \int \frac{d^2 \Delta}{(2\pi)^2} e^{-i\mathbf{b} \cdot \Delta} H^q(x, \xi, t = -\Delta^2)$

$q(x, \xi = 0, \mathbf{b})$  probability to find a quark  $q$  with long. momentum fraction  $x$  at transverse position  $\mathbf{b}$  (Burkardt)

$$q_v^X(x, \mathbf{b}) = q_v(x, \mathbf{b}) - \frac{b^y}{m} \frac{\partial}{\partial \mathbf{b}^2} e_v^q(x, \mathbf{b})$$

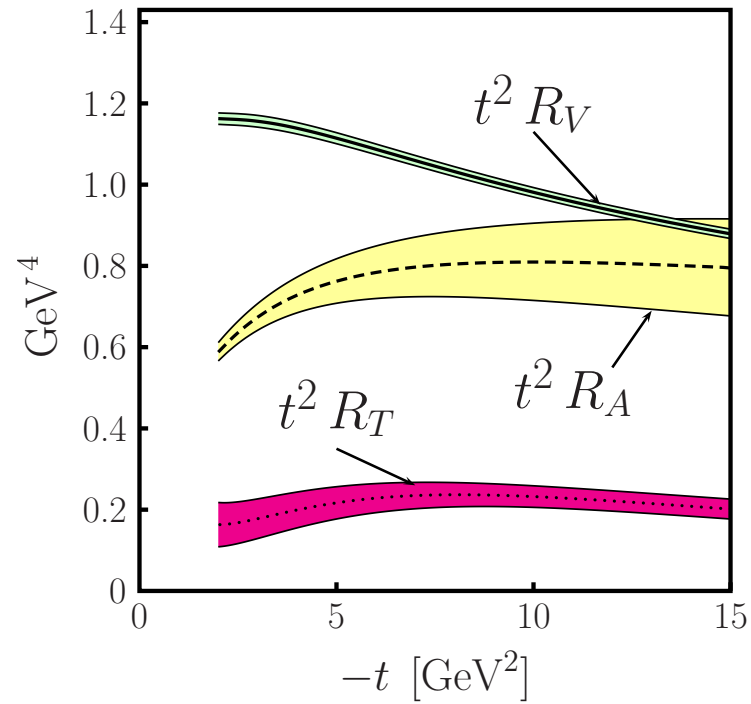
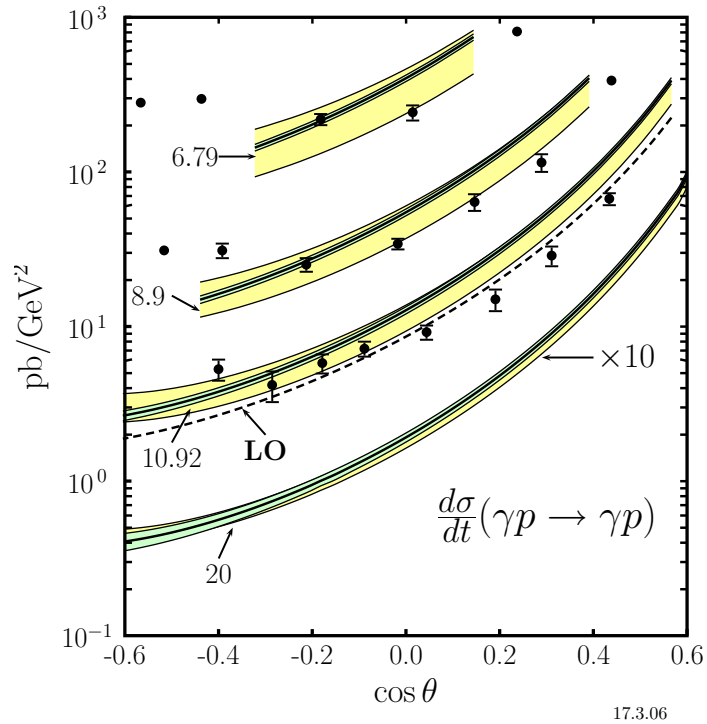
# flavor segregation

in transversely polarized proton



responsible for asymmetries in e.g.  $p \uparrow p \rightarrow \pi^\pm$ ?

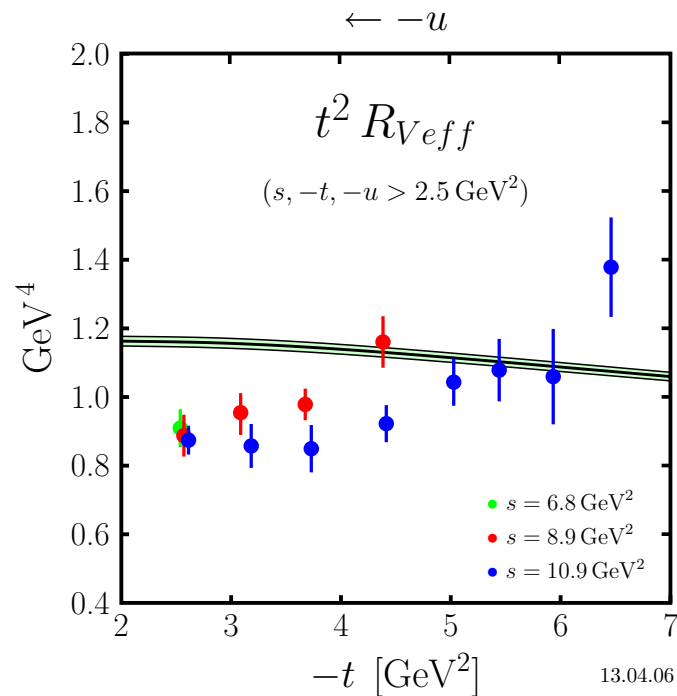
# The Compton cross section



$$\frac{d\sigma}{dt} = \frac{d\hat{\sigma}}{dt} \left\{ \frac{1}{2} \frac{(s-u)^2}{s^2+u^2} [R_V^2(t) + \frac{-t}{4m^2} R_T^2(t)] + \frac{1}{2} \frac{(s+u)^2}{s^2+u^2} R_A^2(t) \right\} + \mathcal{O}(\alpha_s)$$

$\frac{d\hat{\sigma}}{dt}(s, t)$  Klein-Nishina cross section      data: JLab E99-114

# The onset of factorization



extract from Jlab E99-114 data

$$R_V^{\text{eff}} = R_V \sqrt{1 + \frac{-t}{4m^2} \frac{R_T^2}{R_V^2}}$$

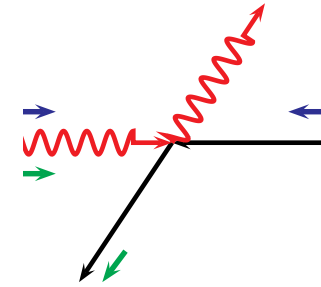
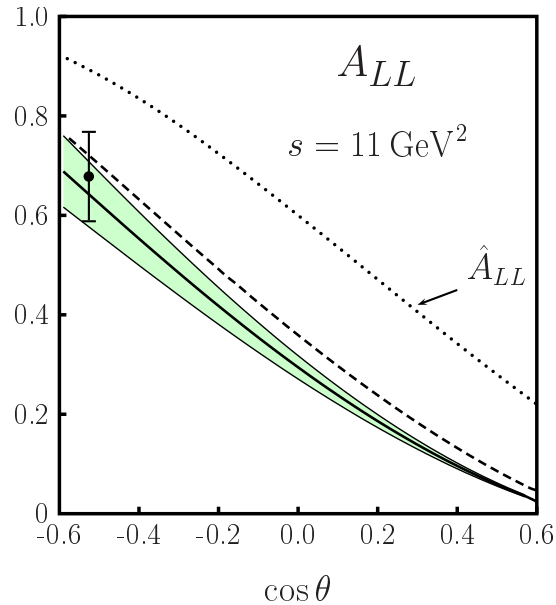
FACTORIZATION:

$R_V^{\text{eff}}$  should not depend on  $s$   
provided  $-t, -u$  are sufficiently large  
seems to hold for  $\lesssim 2.5 \text{ GeV}^2$   
target mass corr. not shown

Comparison with result from GPD analysis - not too good at small  $-t$   
possible reasons:  $\langle x \rangle$  too small, power corrections?

Feynman mechanism (exponential  $t$  dependence) seems to be favored

# Spin correlation $A_{LL}, K_{LL}, A_{LS}, K_{LS}$



$$\hat{A}_{LL} = \frac{s^2 - u^2}{s^2 + u^2}$$

$$A_{LL} = K_{LL} \simeq \hat{A}_{LL} \frac{R_A}{R_V}$$

JLab E99-114 data at  $E_\gamma = 3.23 \text{ GeV}$ :  $\cos \theta = -0.5$ ,  $t = -4 \text{ GeV}^2$ ,  $u = -1.14 \text{ GeV}^2$

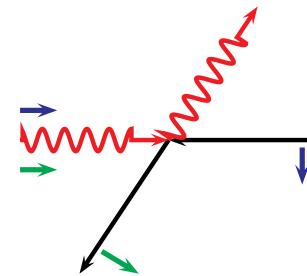
$$\hat{A}_{LS} = 0$$

$$A_{LS} = -K_{LS} \simeq \frac{R_A}{R_V} \hat{A}_{LL} \left( \frac{\sqrt{-t}}{2m} \frac{R_T}{R_V} - \beta \right)$$

$$\beta = \frac{2m}{\sqrt{s}} \frac{\sqrt{-t}}{\sqrt{s} + \sqrt{-u}}$$

$$K_{LS} = 0.111 \pm 0.078 \pm 0.04 \quad (\text{exp})$$

$$= 0.10 \pm 0.02 \quad (\text{theory})$$



# Summary

- There are many applications of the handbag approach to space- and time-like wide-angle exclusive process; seems to work reasonable well for **momentum transfers of the order of  $10 \text{ GeV}^2$**
- First attempt to extract **GPDs from form factor data** ( $F_1^{p,n}, F_2^{p,n}, F_A$ ) in analogy to analyses of PDFs
- On the basis of a physically motivated parameterization information on  $H, \tilde{H}, E$  for valence quarks and at  $\xi = 0$  has been extracted
- **Improvements required:** need  $F_1^n, F_2^n$  (CLAS prel)  
 $F_2^p$  at larger  $t$  (present, upgraded Jlab)  
other moments as input: WACS at upgraded Jlab  
lattice QCD (reliable extrapol. to chiral limit required)
- predictions for WACS with **soft form factors known from recent GPD analysis** in good agreement with experiment
- the handbag approach also applies to time-like processes  
 $\gamma\gamma \rightarrow B\bar{B}, M\bar{M}, p\bar{p} \rightarrow \gamma\gamma, \gamma M$